CUSTOM ARITHMETIC FOR HIGH-SPEED, LOW-RESOURCE ASR SYSTEMS

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ABSTRACT
With the skyrocketing popularity of mobile devices, new processing methods tailored for low-resource systems have become necessary. We propose the use of custom arithmetic, arithmetic logic tailored to a specific application. In a system with all parameters quantized to low precision, such arithmetic can be implemented through a set of small, fast table lookups. We present here a framework for the design of such a system architecture, and several heuristic algorithms to optimize system performance. In addition, we apply our techniques to an automatic speech recognition (ASR) application. Our simulations on various architectures show that on most modern processor designs, we can expect a cycle-count speedup of at least 3 times while requiring a total of only 59kB of ROMs to hold the lookup tables.

1. INTRODUCTION
The burgeoning development of mobile devices has brought about a great need for a more friendly and convenient user interface. Automatic speech recognition (ASR) will undoubtedly become a dominant method since it provides convenient human-machine interaction. However, unlike desktop applications with ample memory and a perpetual power supply, portable devices suffer from limited computational and memory resources and strict power consumption constraints. Consequently, the development of a high-speed, low-resource ASR system becomes crucial to the prevalence of speech technologies on mobile devices.

In the literature, there are many techniques to speed up computation at the software level. Vector quantization (VQ) and subvector quantization (SVQ) are some of the most successful methods. They are applicable to both observation features and model parameters [1]. As a result, the expensive state likelihood computation can be more efficiently realized via quantized arithmetic. But VQ or SVQ methods have not been extended beyond the observation features and model parameters, and full precision is used. Also, aside from the initial lookups, all calculations are made at full precision.

The problem can also be approached from the hardware side. With 32-bit computing having reached the embedded market and after years of finding ways to make general purpose chips more powerful, the use of custom logic seems a rather curious choice. For some applications, though, such decisions may be warranted. Floating point operations are quite slow, and require a rather large chip area when implemented. Additionally, speech recognizers typically need a large dynamic range, but do not use the precision of a floating point representation efficiently. Fixed point arithmetic offers only a partial solution. Operations can be much faster typically need a large dynamic range, but do not use the precision of speech technologies on mobile devices.

heuristic algorithms to optimize system performance. In addition, we apply our techniques to an automatic speech recognition (ASR) application. Our simulations on various architectures show that on most modern processor designs, we can expect a cycle-count speedup of at least 3 times while requiring a total of only 59kB of ROMs to hold the lookup tables.

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Once the codeword values for the inputs and the output are known, all possible values for a function can be precomputed and stored in a table. Each address in the table is determined by the indices of the input operand codewords, and the output is the integer index of the result’s codeword. If the output and the two inputs have bit-widths of \( n_1 \) and \( n_2 \), respectively, then the table requires a total storage of \( \frac{2^{n_1+n_2}}{n_1 n_2} \) bits. We will refer to the table created for a function \( F_{\theta}(\cdot) \) as \( T_{F_{\theta}} \).

The final step in designing this custom arithmetic system is to replace all floating-point values in the program with the corresponding integer indices, providing approximated computation for all values. The calculation \( z = F_{\theta}(x, y) \) would therefore become

\[
I_{V_k} = T_{F_{\theta}}(I_{V_i}, I_{V_j}).
\]

By storing the integer index of the codeword of the output value, we reduce the storage requirements of the table. We can also use the output index directly as the input of the next table lookup, so that all data flow and storage are represented as low-precision integers and all complex expressions become a series of simple table lookups.

### 2.2. Design for ASR

The nature of the equations for decoding with a mixture of Gaussians CHMM (Continuous Hidden Markov Model) makes that task particularly suited to our new method. For instance, part of calculating the Mahalanobis distance for the likelihood evaluation requires the equation given earlier, \( V_i = (V_i - V_j)^2 \). Rather than a floating point subtraction followed by a floating point multiplication, this entire calculation could be completed with a single table lookup.

Similarly, many ASR systems use log values to store probabilities. The addition of probabilities therefore requires log addition. Representing \( z = x + y \) in the log domain gives \( \bar{z} = \bar{x} + \log(1 + e^{\bar{y} - \bar{x}}) \), where \( \bar{x}, \bar{y} \) and \( \bar{z} \) are the logarithms of their unlogged counterparts. Again, this calculation is a function with two input operands meaning that a lookup can replace many operations, including the expensive calls to the log and exponential library functions.

### 3. BIT ALLOCATION SEARCH ALGORITHMS

So far, we have discussed table construction, but have not addressed how to determine the size of each table. The goal is to come up with a system-wide optimization algorithm to allocate resources among all variables. We aim to find the bit-width allocation scheme which minimizes the cost of the resources while maintaining baseline performance.

The algorithms will be presented for a system with \( L \) variables \( \{V_i\}_{i=1}^L \). We now make the following definitions:

- \( bw_i \) – the bit-width of \( V_i \), \( bw_i \) can take on any integer value below 32 (the number of bits used for single-precision floating-point representation);
- \( fp \) – when \( bw_i = fp, V_i \) is unquantized. Typically, \( fp = 32 \);
- \( bw = (bw_1, bw_2, ..., bw_L) \) – a bit-width allocation scheme;
- \( \Delta bw_i \) – an increment of 1 bit for variable \( V_i \), where \( \Delta bw_i = (bw_1, ..., bw_{i-1}, bw_{i} + 1, ..., bw_L) \);
- \( wer(bw) \) – the word error rate (WER) evaluated at \( \bar{bw} \);
- \( cost(bw) \) – total cost of resources evaluated at \( \bar{bw} \).

Note that the cost function can be arbitrarily defined depending on the specific goals of the allocation. In this paper, we use the total storage of the tables as the \( cost \). Additionally, we define the gradient \( \delta_i \) as the ratio of the decrease in WER to the increase in cost evaluated in the direction of \( bw_i \).

\[
\delta_i(bw_i) \triangleq \frac{wer(bw_i) - wer(bw + \Delta bw_i)}{cost(bw + \Delta bw_i) - cost(bw)}
\]

Equation (1) reflects the rate of improvement along the \( bw_i \) direction. We can extend this definition to the gradient along multiple directions. For example,

\[
\delta_{ij}(bw_i) \triangleq \frac{wer(bw_i) - wer(bw_i + \Delta bw_i + \Delta bw_j)}{cost(bw_i + \Delta bw_i + \Delta bw_j) - cost(bw_i)} \quad (2)
\]

is the gradient in the joint direction of \( bw_i \) and \( bw_j \).

Assuming the baseline system gives a WER of \( BWER \), the cost of \( \bar{bw} \) is clearly exponential in \( L \). Even constraining the bit-width of each variable to a restricted range of possible values gives a very large search space. In the following subsections, we present several heuristics that work well experimentally. The basic idea is that we start with a low-cost \( \bar{bw} \) that has low enough a WER that gradients are not meaningless (they provide no information if bit widths are too low) and greedily increase the bit-widths of one or a small group of variables until we find an acceptable solution.

This is similar to the method used in [6] to optimize floating-point bit-widths.

#### 3.1. Single-variable quantization

Finding a reasonable starting point is an important part of these algorithms. One logical place to start is with the results of single-variable quantization, since the results of those quantizations are needed in order to create the tables. Specific methods for quantizing the variables are beyond the scope of this paper. For those interested in several quantization techniques specific to ASR that we developed, see [5].

In general, it is expected that the noise introduced into the system by quantizing an additional variable will produce a result that is not better than without the extra variable quantized. For that reason, we take the starting point to be the minimum number of bits needed to quantize a single variable to produce baseline WER results. We call that result \( m_i \), the minimum bit-width of variable \( V_i \). We determine an upper bound \( M_i \) based on inspection.

Once we determine the boundaries for each single variable we have constrained our search for an optimal point to the hypercube bounded by \( m_i \leq bw_i \leq M_i, i = 1...L \). It then makes sense to start each of the following algorithms at \( bw_{init} = (bw_1 = m_1, bw_2 = m_2, ..., bw_L = m_L) \). In all cases, it is assumed that \( wer(bw_{init}) > BWER \) since the algorithms are designed to stop when they have found a \( \bar{bw} \) with a WER as close as the target rate.
3.2. Single-dimensional increment based on static gradients
This is the simplest, most naive algorithm. In it, we allow one variable’s bit-width to increment by 1 each iteration, based on static gradients, \( \delta_i(bw_i) = \delta_i(bw_i)|_{bw_i = fp} \). The static gradients are obtained from the results of single-variable quantization, with all other variables at \( fp \). The algorithm is:

1. Compute the static gradients \( \delta_i(bw_i), i = 1..L \) at point \( bw \), based on the WERs of the single-variable quantization. Choose the direction \( k = \arg \max \delta_i(bw_i) \), and increase \( bw_k \) by one if it does not exceed the upper bound \( M_k \);
2. Run a test to get the new \( \text{wer}(bw) \). If \( \text{wer}(bw) \leq \text{BWER} \), return \( bw_* = bw \) or, if there is no improvement in WER observed, undo the increment before returning \( bw_* = bw \); otherwise repeat step 1.

In this case, the static gradient is used to approximate the true gradient. The gradients can therefore be pre-computed from the single-variable quantization results, but may be inaccurate. This method gives a pre-determined sequence to test, so the task becomes checking the WER at each point until we have a satisfactory one.

3.3. Single-dimensional increment with dynamic gradients
This algorithm, like the first one, allows only single-dimensional increments, but it uses the true gradient \( \delta_i(bw_i) \) as a measure of improvement, requiring online evaluation. The steps are:

1. Evaluate the gradients \( \delta_i(bw_i), i = 1..L \) for the current \( bw \) according to Equation (1), where \( L \) tests are needed to obtain the WERs;
2. Choose the direction \( k = \arg \max \delta_i(bw_i) \), and increase \( bw_k \) by one if \( bw_k + 1 \leq M_k \);
3. Run a test to get the new \( \text{wer}(bw) \). If \( \text{wer}(bw) \leq \text{BWER} \), return \( bw_* = bw \) or, if there is no improvement in WER observed, undo the increment before returning \( bw_* = bw \); otherwise repeat step 1.

For speech recognition, online evaluation for a test takes a significantly higher amount of time, requiring a full test cycle (although not retraining). This algorithm consequently takes much more time to complete than the others. As this takes place during the design stage, this is not a problem; at recognition time there is no penalty.

This algorithm updates \( \delta_i(bw) \) at each step which gives true gradients in the \( L \)-dimensional space. It might be the case that no improvement exists along each of the \( L \) directions, but that one does exist with joint increments along multiple dimensions. With this algorithm, the search might become stuck in a local optimum.

3.4. Multi-dimensional increment with dynamic gradients
Finally, the bit-widths of multiple variables could be increased in parallel. Considering the computational complexity, we only allow one- or two-dimensional increments, leading to \( L + \binom{L}{2} \) possible candidates. We could extend this to include triple increments, but it would take an intolerably long time to finish. The algorithm modifies steps 1 and 2 from the above algorithm as follows:

1. Evaluate the gradients \( \delta_i(bw_i) \) and \( \delta_{ij}(bw_i) \), \( i = 1..L, j = 1..L \) on current \( bw \) according to Equations (1) and (2) respectively, where \( L + \binom{L}{2} \) tests are needed to obtain the WERs;
2. Choose the direction \( k \) or a pair of directions \( \{ k, l \} \) where \( \delta_k(bw_i) \) or \( \delta_{kl}(bw_i) \) is the maximum among all the single-dimensional and pair-wise increments. Increase the bit-width of \( V_k \) or those of \( \{ V_k, V_l \} \) by one if no one exceeds its upper bound.

This algorithm is superior to the previous two in the sense that it explores many more candidate points in the search space. It considers only one additional direction and may still fall into a local optimum, but is less likely to do so than in the previous case. Due to the measures it takes to avoid local optima, this algorithm takes substantially longer to complete. Again, this is acceptable since it happens during the design stage, not during recognition.

4. EXPERIMENTAL FRAMEWORK

4.1. Speech Recognizer
Our ASR system uses the NYNEX PhoneBook [7] database for training and testing. It is designed for isolated-word recognition tasks and consists of 93,667 isolated-word utterances recorded over a telephone channel with an 8,000 Hz sampling rate. Each sample is encoded with 8 bits via \( \mu \)-law. For details of the training and testing sets, see [8].

We use standard MFCCs plus log energy and their deltas, yielding 26-dimensional acoustic feature vectors. Each vector has mean subtraction and variance normalization applied to both static and dynamic features.

The word model is a set of phone-based CHMMs concatenated together into words based on pronunciation. These pronunciation models determine the transition probabilities between phones. Doing this provides a customizable vocabulary without the need for retraining, a desirable goal for an embedded device.

The system has 42 phone models, each composed of 4 emitting states except for the silence model. The state probability distribution is a mixture of 12 diagonal Gaussians.

4.2. Lookup Tables
We simulated lookup table implementation using SimpleScalar [9], an architecture-level execution-driven simulator. All tables were pre-calculated by SimpleScalar at runtime. We extended the instruction set and modified the assembler to support new lookup instructions. Our tables use a total of 13 variables for 8 functions, 6 in the likelihood evaluation and 2 in the Viterbi search. In most cases, quantized bit-widths were restricted to between 1 and 10 bits.

We simulated results for a variety of architectures. The first is the SimpleScalar default configuration, roughly akin to a 3rd generation Alpha, an out-of-order superscalar processor. The second represents a more modern desktop machine; cache sizes and latencies have been updated from the defaults to reflect more current values. Our third configuration attempts to represent a typical high-end DSP chip. Since most DSP chips are VLIW, an architecture feature not replicable with SimpleScalar, we chose instead to force in-order execution as a very rough approximation of VLIW. Finally, we simulated a very simple processor with a single pipeline and no cache. In each case, we allowed multiple tables to
be accessed in parallel, although a specific table could be used by only 1 instruction at a time.

5. RESULTS

5.1. Allocation Search Algorithms

The results of running each allocation algorithm appear in Table 1. The baseline WER for the system was 2.07%.

<table>
<thead>
<tr>
<th>Algorithm</th>
<th>Min WER</th>
<th>Table Size (kB)</th>
<th>Points Tested</th>
</tr>
</thead>
<tbody>
<tr>
<td>1-D, static δ</td>
<td>3.01%</td>
<td>94.00</td>
<td>13</td>
</tr>
<tr>
<td>1-D, dynamic δ</td>
<td>3.09%</td>
<td>36.44</td>
<td>52</td>
</tr>
<tr>
<td>2-D, dynamic δ</td>
<td>2.53%</td>
<td>58.75</td>
<td>454</td>
</tr>
</tbody>
</table>

Table 1. Minimum WER, total table size, and points tested for each algorithm

Not too surprisingly, the 1-D, static gradient algorithm did not perform particularly well. It managed to reach a slightly better WER than did the 1-D dynamic gradient algorithm, but it required several times more storage to do so. It reached a local optimum quickly, after trying only 13 configurations. The 1-D dynamic gradient algorithm tested a total of 52 configurations, managing to find a fairly small ROM size. The non-linear nature of the search space posed problems for this algorithm, through, which is likely why its WER was the highest. Finally, the 2-D dynamic gradient algorithm found a much better WER than the other two algorithms, even if its total table size was not the smallest. Although the final result does not reach the baseline, it gives an acceptable WER, especially when considering the potential speedup, as is done next.

5.2. Lookup Tables

We simulated each of the target machines for a range of lookup table speeds. This is independent of WER since, assuming the table is not too large, the precision of the output of a lookup has little to do with the speed of the lookup. Because we did not try to implement a low-power front-end, a feature that would be necessary for a final realization of this system, we used pre-calculated MFCCs and subtracted initialization time when calculating speedup. Figure 1 shows the speedup obtained versus the number of cycles required for each lookup. The speedup ranges from just under 2.5 to nearly 4 when lookups take only 1 cycle, and falls off as they become more expensive. In all cases, the speedup is quite significant even when lookups cost several cycles. If the ROM tables are small enough to fit on the processor chip, which is the case using the 59kB results from Table 1, a 1-cycle lookup is quite realistic for a state-of-the-art system. Much benefit actually comes from replacing sequences of instructions with a single lookup, as the dynamic instruction count fell nearly as much as execution time.

6. DISCUSSION

In this paper, we have presented a methodology for the design of high-speed, low-resource systems using custom arithmetic. We also demonstrate several resource allocation search heuristics suitable for finding acceptable points in an otherwise intractable search space. We then applied our findings to a CHMM-based ASR system. Using the allocation search algorithms we developed, we found a table configuration giving satisfactory performance with only a small additional amount of storage. The 59kB of tables is small enough that it can be added to any chip with an access time of 1 cycle. When implementing this design on a modern processor, we show that the expected speedup is at least 3, and possibly larger. Additionally, the smaller operand size means we can make more efficient use of caches to reduce cache misses, and could even narrow the memory bus width providing savings in both chip area and power consumption.

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7. REFERENCES