

PRESS: A Novel Framework of Trajectory Compression in Road Networks

Renchu Song^{†*} Weiwei Sun^{†*} Baihua Zheng[‡] Yu Zheng[§]

[†]Fudan University, Shanghai, China, {songrenchu, wwsun}@fudan.edu.cn

^{*}Shanghai Key Laboratory of Data Science, Fudan University, Shanghai, China

[‡]Singapore Management University, Singapore, bhzheng@smu.edu.sg

[§]Microsoft Research, Beijing, China, yuzheng@microsoft.com

ABSTRACT

Location data becomes more and more important. In this paper, we focus on the trajectory data, and propose a new framework, namely PRESS (*Paralleled Road-Network-Based Trajectory Compression*), to effectively compress trajectory data under road network constraints. Different from existing work, PRESS proposes a novel representation for trajectories to separate the spatial representation of a trajectory from the temporal representation, and proposes a *Hybrid Spatial Compression* (HSC) algorithm and error *Bounded Temporal Compression* (BTC) algorithm to compress the spatial and temporal information of trajectories respectively. PRESS also supports common spatial-temporal queries without fully decompressing the data. Through an extensive experimental study on real trajectory dataset, PRESS significantly outperforms existing approaches in terms of saving storage cost of trajectory data with bounded errors.

1. INTRODUCTION

The advance in location-acquisition technologies has led to a huge volume of spatial trajectories, e.g., the GPS trajectories of vehicles, each of which is comprised of a sequence of time-ordered spatial points. As the trajectories are in huge volume and some points in a trajectory are redundant, application systems on trajectories have to bear high communication loads and expensive data storage. This is calling for trajectory compression technologies that can reduce the storage cost while keeping the utility of a trajectory. In this paper, we propose a trajectory compression framework under the road network constraints, namely PRESS (*Paralleled Road-Network-Based Trajectory Compression*). The main objective is to achieve a spatial lossless and temporal error-bounded compression, and meanwhile provide support to popular LBS applications.

The PRESS framework has five components, namely *map matcher*, *trajectory re-formatter*, *spatial compressor*, *temporal compressor*, and *query processor*, as shown in Fig. 1. Taking raw GPS trajectories as input, map matcher maps

each trajectory into a sequence of edges in the road network, which will be reformatted into a spatial path and a temporal sequence via trajectory re-formatter. Thereafter, the compression takes place in parallel. The spatial path is compressed by spatial compressor based on *Hybrid Spatial Compression* (HSC) algorithm; and the temporal sequence is compressed by temporal compressor based on *Bounded Temporal Compression* (BTC) algorithm. The compressed spatial path and compressed temporal sequence are then passed to query processor to support different application needs.

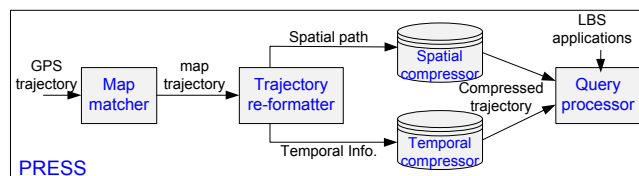


Figure 1: PRESS framework

Different from existing works, we consider both the compression ratio and the utility of the compressed trajectories. In general, the higher the compression ratio, the lower the quality of the compressed trajectory, which directly affects data utility. Consequently, it is challenging to propose a novel approach to achieve a high compression ratio with high quality compressed trajectories, especially under road network constraints.

PRESS tackles this issue from three different angles. First, it observes that the spatial path and the temporal information of a trajectory have different features and hence it strategically separates the spatial path from the temporal information when presenting a trajectory. The clear separation allows us to compress the spatial path and the temporal information separately. Second, a lossless spatial compression algorithm HSC is proposed to effectively compress the spatial path using significantly less space without losing any spatial information. It has two stages. The first stage compression is based on shortest paths. Given a sub-trajectory T_{sub} from edges e_i to e_j , if T_{sub} is exactly the same as the shortest path from e_i to e_j , T_{sub} will be replaced by (e_i, e_j) . As in many cases we tend to take shortest paths in real life, this compression can effectively reduce the number of edges we have to maintain for each trajectory. The second stage compression is based on frequent sub-trajectory (FST) coding. The main idea is to decompose a trajectory into a sequence of FSTs, each of which is represented by a unique code (e.g., Huffman code). The more popular the FST, the shorter the corresponding code and the more the

space savings. Meanwhile, PRESS designs a temporal compression algorithm BTC to compress temporal information with bounded errors. BTC is very flexible, and it can compress the temporal information based on the error bounds specified by different applications. As a summary, the lossless nature of the spatial compression and the error-bounded nature of the temporal compression guarantee the high quality of the compressed trajectories. Last but not the least, PRESS also supports many popular spatial-temporal queries commonly used in location-based services (LBSs) such as *where_{at}*, *when_{at}* and *range* queries without fully recovering the compressed trajectories.

An extensive experimental study has been conducted on a real trajectory dataset to validate the effectiveness and efficiency of PRESS. According to the results, PRESS can save up to 78.4% of the original storage cost. Let $|T|$ be the length of a trajectory T . Both HSC and BTC have the compression time complexity of $O(|T|)$, and hence the compression time complexity of PRESS is $O(|T|)$. As compressed temporal sequences share the same format as original ones, BTC does not require any decompression process. In other words, the decompression time complexity of PRESS is equal to that of HSC, i.e., $O(|T|)$. In addition, PRESS can significantly accelerate spatial-temporal queries. In brief, PRESS outperforms the state-of-the-art approaches in terms of the compression ratio, the time consumption and the acceleration of spatial-temporal queries.

The rest of the paper is organized as follows. Section 2 presents our new approach to represent a trajectory. Section 3 and Section 4 introduce the detailed spatial compression and temporal compression respectively. Section 5 explains how to support some common queries via compressed trajectories. Section 6 presents our experimental studies. Section 7 reviews related work. Finally, Section 8 concludes this paper with some directions for future work.

2. TRAJECTORY REPRESENTATION

In our work, a road network is defined as a directed graph $G = (V, E)$, where V is the vertex set and E is the edge set. The weight on an edge e , denoted as $w(e)$, can be physical distance, travel time or other costs according to different application context. A trajectory is the path that a moving object follows through space as a function of time. Consequently, it contains both spatial information and temporal information. Traditional approaches represent trajectories via a sequence of n triples in the form of $((x_1, y_1, t_1), (x_2, y_2, t_2), \dots, (x_n, y_n, t_n))$, where (x_i, y_i) is the position in the 2D Euclidean space at time stamp t_i .

We propose a different representation of trajectories in the road network. Instead of combining positions and time stamps together like existing approaches do, we separate the locations from time stamps. In other words, a trajectory is represented by a spatial path and a temporal sequence. This clear separation enables us to design different compression approaches for spatial information and temporal information respectively, so that both spatial compression and temporal compression can achieve high compression effectiveness without constraining each other. In the following, we will explain how to represent the spatial information and temporal information via spatial path and temporal sequence, respectively.

The spatial path of a trajectory in a road network is a sequence of consecutive edges. As shown in Fig. 2, a trajec-

tory sequentially passes edges e_{15} , e_{16} , e_{13} , e_6 , and e_3 . Consequently, it can be represented by a spatial path, in the format of $\langle e_{15}, e_{16}, e_{13}, e_6, e_3 \rangle$. Note trajectories can start from and/or end at any point of an edge, not necessarily an endpoint. For example, the example path ends at a point along edge e_3 . We will tackle this issue via the temporal sequence presented in the following.

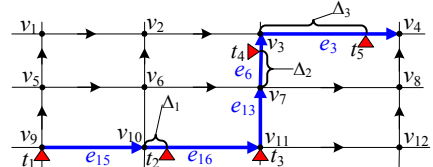


Figure 2: Sample trajectory in a road network

The temporal information of a trajectory defines the time when an object locates at a specific location. For example, the triple (x_i, y_i, t_i) used in the traditional representation tells that the object is located at position (x_i, y_i) at time stamp t_i . However, this representation does not facilitate the spatial queries in road networks. Consider a common query that asks for the average moving speed of an object *obj* during a period $[t_i, t_j]$ with $1 \leq i < j \leq n$. Positions (x_i, y_i) and (x_j, y_j) do not capture any distance information and we have to explore the road network to calculate the distance traveled by *obj* from t_i to t_j . Consequently, we propose to use the tuple (d_i, t_i) to capture the temporal information. To simplify the discussion, d_i in this paper represents the network distance the object has traveled at the time stamp t_i since the start of the trajectory. More generally, d_i can represent other weight information of the edges, e.g., travel time or other costs based on application needs.

Back to the example trajectory shown in Fig. 2. There are five time stamps denoted as t_1, t_2, t_3, t_4 , and t_5 , respectively. Based on our newly proposed temporal sequence representation, the temporal information of our example trajectory will be represented by five tuples. They are $\langle 0, t_1 \rangle$, $\langle w(e_{15}) + \Delta_1, t_2 \rangle$, $\langle w(e_{15}) + w(e_{16}), t_3 \rangle$, $\langle w(e_{15}) + w(e_{16}) + w(e_{13}) + \Delta_2, t_4 \rangle$, and $\langle w(e_{15}) + w(e_{16}) + w(e_{13}) + w(e_6) + \Delta_3, t_5 \rangle$, as shown in Fig. 3(a). The first tuple means the object starts the trajectory at time stamp t_1 and the corresponding distance it has traveled since start is zero (i.e., $d_1 = 0$), the second tuple means the object has traveled $w(e_{15}) + \Delta_1$ distance at time stamp t_2 with $w(e_{15})$ representing the distance of edge e_{15} , and so on. Note the last tuple does not locate at any endpoint, and the same can happen to the first tuple too.

Although we are not the first one to represent the spatial path of a trajectory via edges, we want to highlight that our approach to separating the spatial information from the temporal information when representing trajectories is very *unique*. Former approach [10] uses the vertices in a road network (i.e., the endpoints of edges) to capture the spatial information of trajectories, together with the time when the object passes those vertices. However, the time stamps when the object passes those vertices do not cover the entire temporal information. For example, a taxi might stop for a long time somewhere between two vertices. By retaining two time stamps of the vertices, we can only assume that the taxi drives at a low uniform speed on the edge, which is not the real case. Our approach can easily tackle this issue. As illustrated in Fig. 3(b), we understand that the taxi moves slowly from t_1 to t_2 , gets stuck from t_2 to t_3 , and then moves

slowly again from t_3 to t_4 .

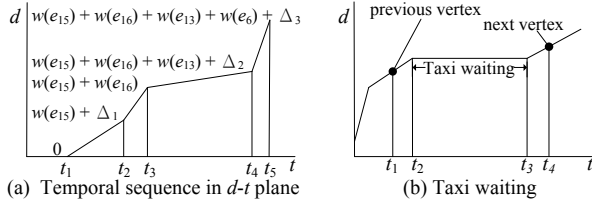


Figure 3: Temporal sequence

3. SPATIAL COMPRESSION

After presenting the formal representation of trajectories, we are ready to present *Hybrid Spatial Compression* (HSC), the two-stage spatial compression algorithm. It takes an initial spatial trajectory $T = \langle e_1, e_2, \dots, e_n \rangle$ as an input, and performs shortest path compression on the first stage and then frequent sub-trajectory compression on the second stage. Existing works use n original sampled positions to keep track of a trajectory, and propose to use m ($< n$) positions for capturing the trajectory in order to cut down the storage cost. However, all the existing approaches based on this idea cannot *fully* capture the spatial path traveled by the trajectory. Consider our sample trajectory. Its spatial path can be represented by six vertices, i.e., $v_9, v_{10}, v_{11}, v_7, v_3$, and v_4 . If we reduce the vertex number from original six to three and represent the trajectory by v_9, v_{11} , and v_4 , we can only tell that in this trajectory, object *obj* moves from v_9 to v_4 via vertex v_{11} but we cannot tell how the object *obj* moves from v_9 to v_{11} , and then from v_{11} to v_4 . Consider the movement from v_{11} to v_4 , the object *obj* could take path $(v_{11}, v_{12}, v_8, v_4)$, or (v_{11}, v_7, v_3, v_4) , or (v_{11}, v_7, v_8, v_4) , which is uncertain.

Although existing works propose various metrics to guarantee the similarity between the compressed trajectories and the original ones, *none* is error-free. They trade in the accuracy of the trajectories' spatial information for the saving of the storage cost. Alternatively, our two-stage HSC approach is *error-free*. The compressed trajectory returned by HSC, although taking less space, captures the spatial path of the original trajectory as it is. In HSC, we make two assumptions. i) Objects tend to take the shortest path instead of longer ones in most if not all cases; and ii) the trajectories are not uniformly distributed in the road network and there are certain edge sequences which are passed through more frequently.

3.1 Shortest path compression

Given a source s and a destination e , most of the time we will take the shortest path (SP) between s and e if all the edges roughly share the similar traffic condition. Under this assumption, we can predict that most, if not all, of the trajectories consist of a sequence of shortest paths. Our first compression is motivated by this observation, and takes full advantage of shortest paths.

We assume that all-pair shortest path information is available via a pre-processing of the road network. This can be achieved by any of the well known shortest path algorithms. If there are several shortest paths between a pair of edges, we only record one of them to eliminate any ambiguity during compression. We assume $SP(e_i, e_j)$ denotes the shortest path from edge e_i to edge e_j , and maintain a structure $SP_{end}(e_i, e_j)$ recording the last edge (the edge right before

e_j) of $SP(e_i, e_j)$ for each pair of edges. Take the partial road network shown in Fig. 4 as an example. Assume the number in the middle of each edge indicates the network distance of the edge, then $SP(e_{15}, e_7) = \langle e_{15}, e_{12}, e_9, e_{10}, e_7 \rangle$, $SP_{end}(e_{15}, e_7) = e_{10}$, $SP_{end}(e_{15}, e_{10}) = e_9$, and so on.

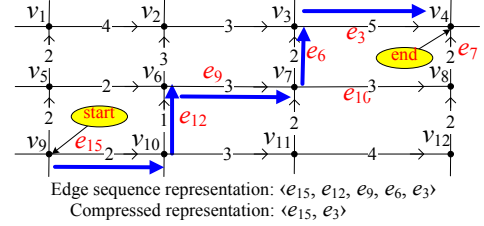


Figure 4: Example of shortest path compression

Due to the space limitation, we use a running example to illustrate the SP compression. The main idea is to skip the detailed sub-trajectory $\langle e_i, e_{i+1}, \dots, e_j \rangle$ if it matches exactly the shortest path from e_i to e_j , i.e., replacing $SP(e_i, e_j)$ with e_i and e_j only. As shown in Fig. 4, the original trajectory $T = \langle e_{15}, e_{12}, e_9, e_6, e_3 \rangle$. Initially, the SP compression algorithm enrolls the first edge e_{15} into T' . Thereafter, it scans the subsequent edges one by one. For the second edge e_{12} , e_{15} and e_{12} are adjacent and the process continues. For the third edge e_9 , $SP_{end}(e_{15}, e_9) = e_{12}$, so edge e_{12} can be skipped. For the fourth edge e_6 , $SP_{end}(e_{15}, e_6) = e_9$ and hence e_9 is also skipped. Next, $SP_{end}(e_{15}, e_3) = e_6$, so e_6 is skipped. Finally, the algorithm enrolls the last edge e_3 into T' to finish the process and replaces T with $T' = \langle e_{15}, e_3 \rangle$. As it scans each edge in T once, its complexity is $O(|T|)$. The main idea of SP compression is to replace the shortest path between two pair of edges with those two edges, and there are multiple ways to implement it. The SP algorithm proposed in this work is based on greedy algorithm, and it actually generates the largest compression ratio during shortest path compression, as stated in Theorem 1.

Theorem 1. *The greedy algorithm is the optimal algorithm resulting in the largest compression ratio during SP compression.*

Proof. Please refer to the Proof of Theorem 1 in our technique report [22]. ■

The decompression process is straightforward. Given a compressed trajectory $T' = \langle e_1, e_2, \dots, e_m \rangle$, we sequentially scan each pair of edges (e_i, e_{i+1}) . If they are not adjacent, we complement the trajectory with the shortest path $SP(e_i, e_{i+1})$. As (e_{15}, e_3) is the only pair and e_{15} is not adjacent to e_3 , we complement T with $SP(e_{15}, e_3) = \langle e_{15}, e_{12}, e_9, e_6, e_3 \rangle$. In order to obtain $SP(e_i, e_j)$, we only need to visit $SP_{end}(e_i, e_j)$, $SP_{end}(e_i, SP_{end}(e_i, e_j))$ and so on. This step takes as many times as the length of the shortest path and hence the time complexity of the decompression process is also $O(|T|)$.

3.2 Frequent sub-trajectory compression

As we assume previously, trajectories are not evenly distributed within the road network and edges in a road network are not accessed uniformly. In other words, certain edge sequences are much more popular than others in terms of frequency. If we are able to locate the very popular sub-trajectories, named *frequent sub-trajectory* (FST), then we can use certain coding scheme to compress them and to replace them in the trajectories with the corresponding codes.

Given a large set of trajectory data, the concept of FST makes sense. Consequently, the compression based on FST

is not effective if the underlying dataset is small. In addition, we also assume the trajectory dataset is periodical. That means if we collect all the trajectories of all the cars moving within a city for a duration of several months, the dataset of one day should be similar to the dataset of another day. Under this assumption, we can locate FSTs based on a subset of the complete trajectory dataset, which corresponds to the training process in data mining. Note that the input training dataset is a subset of the complete trajectory dataset after the SP compression. For example in our experiments, we take the trajectories corresponding to one day as a training dataset, perform SP compression for each trajectory in the training dataset, and then pass them to the second stage for FST mining. In the following, we explain how to mine FSTs, how to decompose a trajectory based on the mined FSTs, and the detailed decoding process, the three main steps of FST compression.

3.2.1 FSTs mining

The problem of mining FSTs is similar to the frequent pattern mining problem [6, 14, 25] in data mining. In this work, we propose a novel approach to locate FSTs. We treat sub-trajectories as *strings* and use Huffman coding [8] to compress them. The more frequent a sub-trajectory is (based on its frequency in the training set), the shorter the corresponding code is and hence more savings in terms of storage cost are expected when compressing the trajectories. The basic idea is to first build a *Trie* [9] based on the training set to represent sub-trajectories as strings, next form an Aho-Corasick automaton [1] to enable a decomposition of a trajectory into a set of sub-trajectories, and then use Huffman coding to compress the trajectories.

In order to facilitate the understanding of our approach, we assume that an input set TD returned by the first-stage SP compression has three compressed trajectories, as shown in Fig. 5. Theoretically, we can locate all the sub-trajectories with length ranging from minimum 1 to maximum trajectory length (e.g., ranging from 1 to 6 in our example). However, we set a threshold θ to only consider the sub-trajectories with their length not exceeding θ . Take the real dataset used in our simulation as an example. On training dataset, by setting θ as any number from 1 to 20, our approach is able to save around 50% to 70% storage consumption but the time complexity of our approach is proportional to θ . Although we cannot formally find an optimal setting for θ as it is highly dependent on the training dataset and real trajectory dataset, a small value of θ already can achieve significant storage saving with reasonable time complexity. In the following discussion, we set $\theta = 3$, which is the optimal length for our trajectory dataset.

$TD = \{ T_{11} = \langle e_1, e_3, e_8, e_6, e_3 \rangle, \text{ Sub-trajectories} = \{ \langle e_1, e_3, e_3 \rangle, \langle e_3, e_8, e_6 \rangle, \langle e_8, e_6, e_3 \rangle, \langle e_6, e_3 \rangle, \langle e_3 \rangle, \langle e_1, e_3, e_2 \rangle, \langle e_5, e_2, e_1 \rangle, \langle e_2, e_1, e_4 \rangle, \langle e_1, e_4, e_8 \rangle, \langle e_4, e_8 \rangle, \langle e_8 \rangle, \langle e_2, e_1, e_4 \rangle, \langle e_1, e_4, e_6 \rangle, \langle e_4, e_6 \rangle, \text{ and } \langle e_6 \rangle \}$

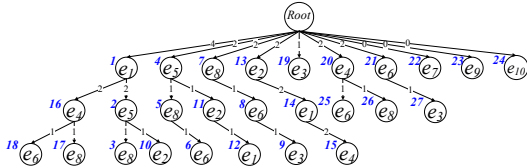


Figure 5: Example Trie

For the given input dataset TD , we first locate all the sub-trajectories with length not exceeding θ (i.e., 3). Note we locate one sub-trajectory starting from each edge, so

those sub-trajectories near the tail of each trajectory may be shorter than θ . As illustrated in Fig. 5, they are $\langle e_1, e_3, e_8 \rangle$, $\langle e_5, e_8, e_6 \rangle$, $\langle e_8, e_6, e_3 \rangle$, $\langle e_6, e_3 \rangle$, $\langle e_3 \rangle$, $\langle e_1, e_3, e_2 \rangle$, $\langle e_5, e_2, e_1 \rangle$, $\langle e_2, e_1, e_4 \rangle$, $\langle e_1, e_4, e_8 \rangle$, $\langle e_4, e_8 \rangle$, $\langle e_8 \rangle$, $\langle e_2, e_1, e_4 \rangle$, $\langle e_1, e_4, e_6 \rangle$, $\langle e_4, e_6 \rangle$, and $\langle e_6 \rangle$. We then build a Trie based on all identified sub-trajectories. For any node n in the Trie, the path from $root$ to n represents a sub-trajectory T_{sub} with the number shown in the link from its parent node indicating the frequency of T_{sub} . Here, the number next to each node is the unique ID for the node. Take node 18 as an example. The string formed by the nodes along the path from $root$ to node 18 is $e_1e_4e_6$, i.e., corresponding to the sub-trajectory $\langle e_1, e_4, e_6 \rangle$. The number 1 shown in the link from node 16 to node 18 represents the frequency of $\langle e_1, e_4, e_6 \rangle$, i.e., it only appears once in the training dataset. In addition, we want to make sure that the nodes in the first level (the level right below $root$) correspond to all the edges in the original road network. This design is to facilitate the later decomposition process which will be explained later. Take our sample Trie as an example. Assume our original road network consists of 10 edges (i.e., e_1, e_2, \dots, e_{10}), only edges $e_1, e_2, e_3, e_4, e_5, e_6$, and e_8 present as the first edge in the located sub-trajectories. Consequently, we add the rest edges (i.e., e_7, e_9 , and e_{10}) to the first level with the corresponding frequency set to zero, as shown in Fig. 5.

Trajectory decomposition. Once FSTs are identified and the Trie is constructed, we need to decompose an input trajectory into a set of identified FSTs. We borrow the basic idea from Aho-Corasick string matching algorithm. Informally, the algorithm constructs a finite state machine that resembles a trie with additional links between the various internal nodes. The automaton is depicted in Fig. 6, with all the extra links represented by dashed lines. To be more specific, each extra link issued from a node n_1 to another node n_2 that is the longest possible suffix of the string corresponding to n_1 . For example, for node 15 ($e_2e_1e_4$), its suffixes are $\langle e_1e_4 \rangle$ and $\langle e_4 \rangle$. The longest of these that exists in our example is $\langle e_1e_4 \rangle$, i.e., node 16. That is why the extra link issued from node 15 points to node 16.

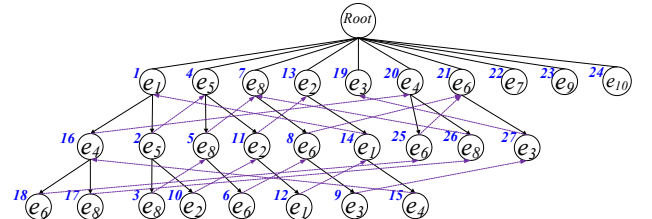


Figure 6: Aho-Corasick automaton

Now we explain how to decompose an input trajectory into a sequence of identified sub-trajectories. It treats the trajectory as a string, and scans the characters (i.e., edges) one by one sequentially. At each step, the current node is extended by finding its children, and if none of the children matches the character, finding its suffix's children, and so on, finally ending in the $root$ node if nothing has been before.

Algorithm 1 lists its pseudo code. First, it initializes all the parameters. Here, n indicates the current node of the automaton A , i indicates the position of the edge of the trajectory currently evaluated, S is an auxiliary stack holding all the matched nodes in A , and Res is the result set which consists of a sequence of the sub-trajectories decomposed

Algorithm 1 Trajectory decomposition

Input: Aho-Corasick automaton A , a compressed trajectory $T' = \langle e_1, e_2, \dots, e_j \rangle$;

Output: a sequence of sub-trajectories;

Procedure:

```

1:  $n \leftarrow \text{root}(A)$ ;  $i \leftarrow 1$ ;  $S \leftarrow \emptyset$ ;  $Res \leftarrow \emptyset$ ;  $l \leftarrow 0$ ;
2: while  $i \leq |T'| (= j)$  do
3:    $child \leftarrow \text{Match}(n, e_i)$ ;
4:   if  $child \neq -1$  then
5:      $push(S, child)$ ;  $n \leftarrow child$ ;  $i++$ ;
6:   else if  $n.Link_{extra} \neq NULL$  then
7:      $n \leftarrow n.Link_{extra}$ ;
8:   else
9:      $n \leftarrow \text{root}(A)$ ;
10: while  $n \leftarrow pop(S) \neq \emptyset$  do
11:   if  $l = 0$  then
12:      $insert(Res, T_{sub}(n))$ ,  $l \leftarrow |T_{sub}(n)| - 1$ ;
13:   else
14:      $l--$ ;
15: return  $Res$ ;

```

from the input trajectory T' . It then scans the edges in T' one by one sequentially. For each edge e_i , it first checks whether a child of the current node matches e_i via the function $Match(n, e_i)$. If a match occurs, $Match(n, e_i)$ returns the child node. We then push it to S , set it as the current node, and proceed to the next edge by increasing i (lines 4-5). If a mismatch occurs indicated by -1 returned by $Match(n, e_i)$, we continue the checking at n 's suffix node if any via the extra link $Link_{extra}$ (lines 6-7) or the $root$ node (lines 8-9). Recall that for each edge in the original road network, our automaton has a corresponding node in its first level. Consequently, a match can be definitely achieved for each edge in the input trajectory and our decomposition is converged. After the first WHILE-loop (lines 2-9), stack S shall have $|T'| (= j)$ nodes, with each corresponding to an edge in T' .

Next, we recover the sub-trajectories represented by the nodes in S . Note that the initial Aho-Corasick string matching algorithm is a kind of dictionary-matching algorithm that locates elements of a finite set of strings (the ‘‘dictionary’’) within an input text. As it matches all patterns simultaneously, the returned patterns may have overlaps. However, our purpose for sub-string searching is to decompose the trajectory T' into a sequence of sub-trajectories and hence each edge in T' shall present exactly once in one sub-trajectory. The reason that, when a matched node is found, we do not output the corresponding string but maintain it in the stack S is to avoid the overlapping among different sub-trajectories. As each node in S matches one edge in T' , our basic idea is to find the longest matched sub-trajectory from each edge backward. In other words, given a node n with $|T_{sub}(n)| = l$, the next $(l-1)$ nodes in S can be ignored. This process is performed by the second WHILE-loop (lines 10-14). Finally, the algorithm returns the sub-trajectories maintained in Res to complete the decomposition. The time complexity of this decomposition process is $O(|T'|)$.

We use an example to illustrate the trajectory decomposition process. Assume $T' = \langle e_1, e_4, e_7, e_5, e_8, e_6, e_3, e_1, e_5, e_2, e_{10} \rangle$. First, for e_1 , the first edge in T' , it finds a match at node 1, and pushes node 1 to S with $S = \{1\}$. Second, for e_4 , the second edge in T' , it finds a match at node 16 and pushes node 16 to S with $S = \{16, 1\}$. For e_7 , the third edge of T' , it cannot find a match with any child

of node 16, and even the child of node 20 (node 16's suffix node). Consequently, we trace-back to the $root$ node and find a match at node 22 and update S to $\{22, 16, 1\}$. The process repeats until all the edges are processed with $S = \{24, 10, 2, 1, 9, 6, 5, 4, 22, 16, 1\}$. Next, we start the sub-trajectory recovery step by popping out nodes from S . First, node 24 is popped out, and $T_{sub}(24) = \langle e_{10} \rangle$ is added to Res . As $|T_{sub}(24)| = 1$, it does not skip any other node in S . Second, node 10 is popped out and $T_{sub}(10) = \langle e_1, e_5, e_2 \rangle$ is added to Res . As its length is three, it skips the next two nodes popped out from S , i.e., nodes 2 and 1, but evaluates node 9. It adds $T_{sub}(9) = \langle e_8, e_6, e_3 \rangle$ to Res . Again, the next 2 nodes (i.e., nodes 6 and 5) are skipped and we evaluate node 4 which triggers the insertion of $\langle e_5 \rangle$. This process also continues until S is empty. Finally, $Res = \{\langle e_1, e_4 \rangle, \langle e_7 \rangle, \langle e_5 \rangle, \langle e_8, e_6, e_3 \rangle, \langle e_1, e_5, e_2 \rangle, \langle e_{10} \rangle\}$. Accordingly, T' is decomposed into six sub-trajectories, corresponding to nodes 16, 22, 4, 9, 10, and 24, respectively, as shown in Table 1.

Encoding procedure. Finally, we present an encoding procedure which uses Huffman coding to represent the identified FSTs. The main idea is to code each node in Trie. The more frequent a node is, the shorter the code is expected to be. Consequently, we construct a Huffman tree based on all the nodes according to the node frequency, except the $root$ node. Huffman tree is a binary tree. A node can be either a leaf node or an internal node. An internal node contains a weight that is a summation of its child nodes' weights, and two links to two child nodes. As a common convention, bit ‘0’ represents following the left child and bit ‘1’ represents following the right child. Assume the initial Trie has n nodes, a corresponding Huffman tree has up to n leaf nodes and $n - 1$ internal nodes.

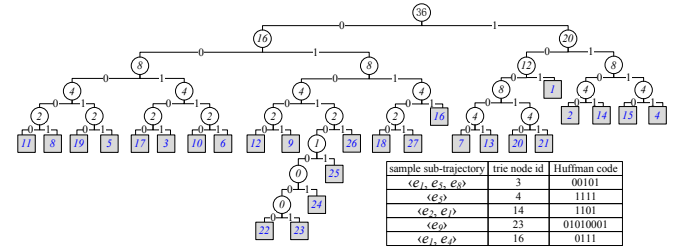


Figure 7: Example Huffman tree

Initially, all nodes are leaf nodes, and the process essentially begins with the leaf nodes containing the frequencies of the Trie nodes they represent. Then, a new node whose children are the two nodes with smallest frequencies is created, such that the new node's weight is equal to the sum of the children's weight. With the previous two nodes merged into one node, and with the new node being now considered, the procedure is repeated until only one node remains. For the Trie shown in Fig. 5, the corresponding Huffman tree is depicted in Fig. 7. Here, a rectangle represents a leaf node which corresponds to a node in the Trie, and a circle represents an internal node with the number inside the circle indicating the weight. With the help of Huffman tree, each node of the Trie (i.e., each identified sub-trajectory) can be represented by a unique code. For easy understanding, we list some sample sub-trajectories and their unique codes in Fig. 7. For example, $\langle e_1, e_5, e_8 \rangle$ is represented by node 3 in the Trie, and its corresponding code is 00101; $\langle e_1, e_4 \rangle$ is represented by node 16 in the Trie, and its corresponding code is 0111. Based on Huffman coding, the code for the

example trajectory T' is listed in Table 1.

As a summary, FST compression first locates all the sub-trajectories with their length not exceeding θ from the training set, and constructs a Trie. It then builds an Aho-Corasick automaton and a Huffman tree based on the Trie. For a given compressed trajectory T' , it decomposes T' into a sequence of sub-trajectories with the help of the automaton, and then uses the Huffman codes of the corresponding sub-trajectories as a compressed format to represent T' . The decoding process is straightforward. Given a binary code, it first recovers the sequence of nodes in Trie represented by the binary code with the help of Huffman tree, and then retrieves the sub-trajectories represented by those Trie nodes to recover the trajectory. The time complexity of the first step is in the scale of the length of the binary code. Given the fact that the binary code has $|T|$ as the upper bound, the first step has $O(|T|)$ as the time complexity. The time consumption of the second step is the length of the SP compression result, which is up bounded by $|T|$. Consequently, the time complexity of this step is also $O(|T|)$. Combining two steps, the time complexity of decoding process is $O(|T|)$.

HSC takes advantages of above two spatial compression techniques, and is expected to further improve the compression effectiveness. We assume the all-pair shortest path, the Trie, the automaton and the Huffman tree are constructed in advance. Because the compression and decompression time complexity of both SP compression and FST compression is $O(|T|)$, the compression and decompression time complexity of HSC is $O(|T|)$.

Table 1: FST compression of trajectory T'

input T'	$\langle e_1, e_4, e_7, e_5, e_8, e_6, e_3, e_1, e_5, e_2, e_{10} \rangle$
decomposition	$\langle e_1, e_4 \rangle, \langle e_7 \rangle, \langle e_5 \rangle, \langle e_8, e_6, e_3 \rangle, \langle e_1, e_5, e_2 \rangle, \langle e_{10} \rangle$
Trie nodes	16, 22, 4, 9, 10, 24
Huffman code	0111, 01010000, 1111, 01001, 00110, 0101001
Result	011101010000111101001001100101001

4. TEMPORAL COMPRESSION

We propose to represent the temporal information of a trajectory in the form of (d_i, t_i) . This representation is storage consuming, as it suffers from the same scale as the original GPS sampling number. However, on the other hand, each tuple (d_i, t_i) describes when the object is at a specific location. The compression of this information will cause the loss of certain information. Consequently, we propose two metrics to bound the inaccuracy that could be caused by the temporal compression, namely *Time Synchronized Network Distance* (TSND) and *Network Synchronized Time Difference* (NSTD), as formally defined in Definition 1 and Definition 2. To simplify our discussion, we assume the trajectories mentioned in the following are in the format of $((d_1, t_1), (d_2, t_2), \dots, (d_n, t_n))$. For a given T and a given time stamp t_x ($\in [0, t_n]$), the corresponding distance d_x the object has moved at t_x can be approximated by linear interpolation via function $Dis(T, t_x)$. For example, $Dis(T, t_x)$ with $t_i < t_x \leq t_{i+1}$ returns $d_i + \frac{(d_{i+1} - d_i) \times (t_x - t_i)}{(t_{i+1} - t_i)}$. Similarly, for a given T and a given d_x ($\in [0, d_n]$), the corresponding time t_x when object moves d_x distance along T can be approximated by linear interpolation via function $Tim(T, d_x)$.

4.1 Error metrics

Before we present our BTC algorithm, we first introduce the error metrics TSND and NSTD in the following.

Definition 1 (Time Syn. Network Dis. (TSND)).

Given a trajectory T and its compressed one T' , TSND measures the maximum difference between the distance object travels via trajectory T and that via trajectory T' at any time slot with $TSND(T, T') = \text{Max}_{t_x} (|Dis(T, t_x) - Dis(T', t_x)|)$. \square

Definition 2 (Network Syn. Time Dif. (NSTD)).

NSTD defines the maximum time difference between a trajectory T and its compressed form T' while traveling any same distance with $NSTD(T, T') = \text{Max}_{d_x} (|Tim(T, d_x) - Tim(T', d_x)|)$. \square

To facilitate the understanding of these two metrics, we depict an example in Fig. 8. Given a sequence of temporal tuples $T = ((d_1, t_1), (d_2, t_2), \dots, (d_n, t_n))$, T can be plotted on a d - t plane. Then, TSND measures the maximum difference between T and T' along d -dimension, and NSTD measures the maximum difference between T and T' along t -dimension. We want to highlight that both TSND and NSTD are meaningful only when the compressed trajectory T' keeps exactly the same spatial information as the original trajectory T' , which is guaranteed by our HSC algorithm.

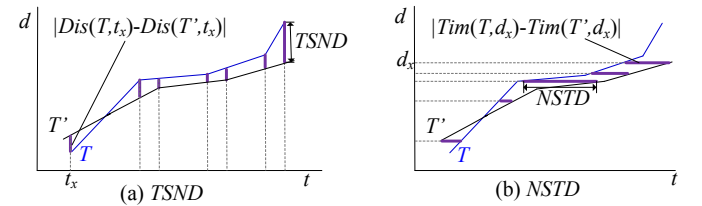


Figure 8: TSND and NSTD

The metric TSND is a variant of *Time Synchronized Euclidean Distance* (TSED) [16, 20] metric which measures the distance of two Euclidean space trajectories. Given a Euclidean space trajectory $T_e = ((l_1, t_1), (l_2, t_2), \dots, (l_n, t_n))$ and its compressed one $T'_e = ((l'_1, t'_1), (l'_2, t'_2), \dots, (l'_m, t'_m))$ with $l_i = (x_i, y_i)$ and $l'_i = (x'_i, y'_i)$ representing two Euclidean points, TSED returns the maximum Euclidean distance between a point l_i and a point l'_j with $(l_i, t_x) \in T_e$ and $(l'_j, t_x) \in T'_e$, for any $t_x \in [0, t_n]$.

Theorem 2. Given an original trajectory T and a compressed trajectory T' , if T' is compressed via previously introduced HSC algorithm, $TSND(T, T') \geq TSED(T, T')$.

Proof. Please refer to the Proof of Theorem 2 in our technique report [22]. \blacksquare

4.2 Bounded Temporal Compression

After introducing metrics TSND and NSTD, we are ready to present the *Bounded Temporal Compression* (BTC) algorithm. As $T = ((d_1, t_1), (d_2, t_2), \dots, (d_n, t_n))$ can be plotted as a polygonal line on d - t plane, it forms a Euclidean space trajectory in d - t space. Consequently, BTC can be transformed to Euclidean trajectory compression, which has been well-studied in the literature. Among available solutions, we adopt an algorithm similar to *Before Opening Window* (BOPW) [16] because of its excellent performance and the ability to address online trajectory compression issues. The only difference is that the original algorithm purely considers TSED metric, while our implementation considers TSND and NSTD metrics.

The main idea is that for a given trajectory T , maximal tolerated TSND τ and maximal tolerated NSTD η , BTC scans the tuples in T sequentially. For a tuple (d_i, t_i) , it attempts to skip (d_{i+1}, t_{i+1}) by linking (d_i, t_i) and (d_{i+2}, t_{i+2})

directly. In other words, we attempt to replace the initial sub-trajectory $T_i = ((d_i, t_i), (d_{i+1}, t_{i+1}), (d_{i+2}, t_{i+2}))$ with $T'_i = ((d_i, t_i), (d_{i+2}, t_{i+2}))$. To evaluate whether this replacement is valid, we calculate NSTD and TSND values between T_i and T'_i . If $TSND(T_i, T'_i) \leq \tau$ and $NSTD(T_i, T'_i) \leq \eta$, this attempt is valid and we can safely skip (d_{i+1}, t_{i+1}) , and then start the next attempt to skip (d_{i+2}, t_{i+2}) by linking (d_i, t_i) and (d_{i+3}, t_{i+3}) directly. Otherwise, the attempt is invalid and (d_{i+1}, t_{i+1}) cannot be skipped. An invalid attempt terminates the evaluation of tuple (d_i, t_i) , and initiates the evaluation of the last successfully attempted tuple (d_{i+1}, t_{i+1}) . The process repeats until all the edges are evaluated.

The original implementation of BOPW has a time complexity of $O(|T|^2)$. We improve it to $O(|T|)$ with the help of a novel concept namely *angular range*. Given two points $p_i = (d_i, t_i)$ and $p_{i+1} = (d_{i+1}, t_{i+1})$ in a d - t space, we assume BOPW keeps p_i in T' . No matter how T' looks like, it must satisfy τ and η , i.e., $TSND(T, T') \leq \tau$ and $NSTD(T, T') \leq \eta$. In other words, the difference between T and T' along d dimension at t_{i+1} is bounded by τ and the difference between T and T' along t dimension at d_{i+1} is bounded by η . Consequently, given a vertical line segment seg_v centered at d_{i+1} with $|seg_v| = 2\tau$, T' must intersect seg_v . As shown in Fig. 9(a), seg_v bounds an angular range R_1 that T' shall fall within. Similarly, given a horizontal line segment seg_h centered at t_{i+1} with $|seg_h| = 2\eta$, T' must intersect seg_h . As shown in Fig. 9(b), seg_h actually bounds an angular range R_2 that T' shall fall within. Considering both η and τ , the angular range is shrunk to the intersection between R_1 and R_2 , i.e., the shaded angular range R_A depicted in Fig. 9(c).

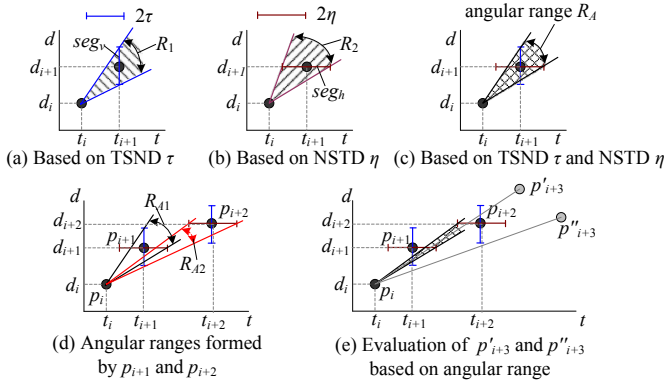


Figure 9: Illustration of angular range

In order to facilitate the presentation, we assume function $R_A(p_i, S_p, \tau, \eta)$ returns the angular range centered at point p_i formed by all the points of set S_p , i.e., $R_A(p_i, S_p, \tau, \eta) = \bigcap_{p \in S_p} R_A(p_i, \{p\}, \tau, \eta)$. Take points depicted in Fig. 9(d) as an example, $R_A(p_i, \{p_{i+1}\}, \tau, \eta) = R_{A1}$, $R_A(p_i, \{p_{i+2}\}, \tau, \eta) = R_{A2}$, and $R_A(p_i, \{p_{i+1}, p_{i+2}\}, \tau, \eta) = R_{A1} \cap R_{A2}$.

With the help of angular range, we can compress $T = \langle p_1, p_2, \dots, p_n \rangle$ based on BOPW with $O(|T|)$ time complexity, and its pseudo code is listed in Algorithm 2. It maintains a pointer *index* pointing to the last point p_{index} along T that has been enrolled into T' , and an angular range R centered at p_{index} that bounds all the possible rotations T' can make right after p_{index} . Initially, R is set to straight angle $[-\frac{\pi}{2}, \frac{\pi}{2}]$ which captures the full half-plane after p_{index} . Thereafter, R gets shrunk by the points evaluated. For each point p_i that is scanned by the algorithm, we check whether p_i is located inside the current angular range R centered

at p_{index} via the boolean function $FallInside(R, p_{index}, p_i)$ and there are two possible outputs. If p_i is within R , the points $p_{index+1}, p_{index+2}, \dots, p_{i-1}$ can be skipped. We further shrink the current range R by p_i and start the evaluation on p_{i+1} . Otherwise, p_{i-1} cannot be skipped and we append p_{i-1} to T' . Meanwhile, a new angular range centered at p_{i-1} is initiated. Take Fig. 9(e) as an example. Suppose $index = i$ and currently we are evaluating point p_{i+3} . If p_{i+3} is located at the point of p'_{i+3} , p_{i+3} is within the angular range R (i.e., the shaded area). We can shrink R based on $R_A(p_i, \{p_{i+3}\}, \tau, \eta)$ and then continue the process. If p_{i+3} is located at the point of p''_{i+3} , it is located outside the current R . Consequently, the algorithm will enroll p_{i+2} into T' , set *index* to $(i+2)$ and a new angular range R to straight angle, and then continue the process.

Algorithm 2 Bounded Temporal Compression

Input: a trajectory $T = ((d_1, t_1), (d_2, t_2), \dots, (d_n, t_n))$;

Output: a compressed trajectory T' ;

Procedure:

- 1: $index \leftarrow 1, T' \leftarrow p_{index}, R \leftarrow [-\frac{\pi}{2}, \frac{\pi}{2}]$;
 - 2: **for** $i \leftarrow 2$ **to** n **do**
 - 3: **if** $FallInside(R, p_{index}, p_i) = 1$ **then**
 - 4: $R \leftarrow R \cap R_A(p_{index}, \{p_i\}, \tau, \eta)$;
 - 5: **else**
 - 6: $Append(T', p_{i-1}); R \leftarrow [-\frac{\pi}{2}, \frac{\pi}{2}]; index \leftarrow i - 1$;
 - 7: **return** T' ;
-

5. APPLICATIONS ON COMPRESSED TRAJECTORY

The main purpose of trajectory compression is to use less space to store the trajectories. Consequently, whether the compressed trajectories can support various LBS applications is *not* the main focus of different compression approaches. As PRESS compresses the trajectories in such a way that the spatial paths are captured exactly and the temporal information loss is bounded by TSND and NSTD, we can decompress the trajectories for LBS applications. However, it is still desirable that the compressed trajectories can support certain, if not all, applications without being fully decompressed. In the following, we demonstrate in detail that the compressed trajectory can support *where_{at}*, *when_{at}* and *range*, three common queries used by many LBSs, and briefly introduce some other queries PRESS can support. *where_{at}*(T, t) returns a location along the trajectory T where an object is located at time t , *when_{at}*(T, x, y) returns a time stamp when an object is located at (x, y) while traveling along T , and *range*(T, t_1, t_2, R) checks whether trajectory T passes the region R during time period t_1 to t_2 .

where_{at} Query. Given a trajectory T , its compressed form T' returned by PRESS, and a time slot t_i , let $Dis(T, t_i) = d_i$, $Dis(T', t_i) = d'_i$, $where_{at}(T, t_i) = p_i$ and $where_{at}(T', t_i) = p'_i$. Based on the fact that $|d_i - d'_i| \leq TSND(T, T')$ guaranteed by BTC, we have $|where_{at}(T', t_i) - where_{at}(T, t_i)| = |p_i - p'_i| \leq TSND(T, T')$. This is because $|p_i - p'_i|$ refers to the shortest distance from p_i to p'_i , and $|d_i - d'_i|$ refers to the distance from p_i to p'_i along trajectory T . Obviously, $|p_i - p'_i| \leq |d_i - d'_i| \leq TSND(T, T')$.

Given one original trajectory, we assume its spatial information is represented by n edges $\langle e_1, e_2, \dots, e_n \rangle$ and its temporal information is captured by m (d_i, t_i) tuples. Query *where_{at}*(T, t) needs to first locate d based on t (i.e., $Dis(T, t) = d$) and then locate e based on d . Consequently, it visits

$\frac{m}{2}$ temporal tuples and $\frac{n}{2}$ edges on average.

Given a compressed trajectory T' , $where_{at}(T', t)$ query still needs to locate d' based on t . Assume the temporal compression ratio is $\frac{|T|}{|T'|} = \beta$, it needs to scan $\frac{m}{2\beta}$ tuples on average. Thereafter, it needs to locate the point along T' corresponding to the distance d' . As this process relies on some additional information, we first introduce the auxiliary structures. We assume certain distance information is embedded in Trie to facilitate the query processing. For each node n in Trie, it stores the distance of $T_{sub}(n)$, denoted as $T_{sub}(n).d$. For example, node 16 keeps the distance of $T_{sub}(16) = (e_1, e_4)$, and node 9 keeps the distance of $T_{sub}(9) = (e_8, e_6, e_3)$. Note that the sub-trajectories captured by Trie might not be a real sub-trajectory of any original trajectories, as Trie takes all the compressed trajectories of SP compression as input. Consequently, we need to decompress the sub-trajectory $T_{sub}(n)$ based on SP decompression in order to calculate the distance $T_{sub}(n).d$. In addition to this node distance, we also assume the distance of all-pair shortest paths is maintained by the shortest path table.

Now, we are ready to explain how to locate the answer point along the trajectory based on a given d' . Given a binary code, we maintain an accumulative distance d_{acu} and recover the sequence nodes n_i one by one following the FST decompression process. For each recovered node n_i , we increase d_{acu} by $T_{sub}(n_i).d$. In addition, we need to check whether the hop from $T_{sub}(n_{i-1})$ to $T_{sub}(n_i)$ is seamless. To achieve this, we get the character (i.e., edge) represented by n_{i-1} (i.e., the node right before n_i), that is the last edge of $T_{sub}(n_{i-1})$; and we get the first character along the path from $root$ to n_i , that is the first edge of $T_{sub}(n_i)$. We then check the shortest-path table to get the shortest distance between them, which also contributes to d_{acu} . After recovering a node n_i , we check whether $d_{acu} < d'$. If yes, the process continues to recover the next node n_{i+1} ; otherwise, the answer point must locate in $T_{sub}(n_i)$. Assume $T_{sub}(n_i)$ is in the form of $(e_j, e_{j+1}, \dots, e_{j+u})$. We then scan the edge and its immediate follower one by one. Initially, we check e_j and e_{j+1} , get their shortest distance from the distance table, and add it to d_{acu} . If $d_{acu} < d'$, it proceeds to e_{j+1} and e_{j+2} . Otherwise, the answer point must locate at the shortest distance from e_j to e_{j+1} . We then fully recover the shortest path and find the answer point. Assume that the SP compression ratio is α , and the FST compression ratio is γ . It on average recovers $\frac{n}{2\alpha\gamma}$ Trie nodes, and checks $\frac{\gamma}{2}$ edges within the located sub-trajectory. Given the fact that $\alpha > 1$ and $\gamma > 1$, the time complexity is reduced.

when_{at} Query. Before introducing $when_{at}$, we show that $when_{at}$ is error-bounded by $NSTD$, i.e., for a trajectory T and its compressed form T' compressed via PRESS, $|when_{at}(T, x, y) - when_{at}(T', x, y)| = |t_i - t'_i| \leq NSTD(T, T')$. Given an input point $p = (x, y)$ and T , $when_{at}$ assumes p is a point along T and locates p to an edge of T . Then, it derives the network distance d traveled along T from the starting point until p , based on which the corresponding time t_i can be located along the temporal information of T . As HSC is errorfree, T' captures the exact spatial information as T and the corresponding d' derived based on T' and (x, y) equals d . As guaranteed by Definition 2, $|t_i - t'_i| \leq NSTD(T, T')$.

Similar as $where_{at}(T, t)$, $when_{at}(T, x, y)$ needs to first locate (x, y) to an edge $e_j \in T$ along the trajectory such that $(x, y) \in e_j$, derive the distance d_i traveled along T until the

input point (x, y) , and then locate t_i along the temporal representation based on d_i . On average, it visits $\frac{n}{2}$ edges and $\frac{m}{2}$ temporal tuples. Given a compressed trajectory T' , $when_{at}(T, x, y)$ is processed similarly except it actually visits fewer edges. To facilitate the process, we record an MBR (Minimum Bounding Rectangle) for each Trie node n and an MBR for the shortest path of each pair of nodes. When we recover the nodes one by one, we check whether $(x, y) \in MBR(n)$. If $(x, y) \in MBR(n)$, we scan $T_{sub}(n)$ edge by edge and check whether $(x, y) \in MBR(e_i, e_j)$, assuming e_i and e_j are two adjacent edges in $T_{sub}(n)$. Every time when $(x, y) \in MBR(SP(e_i, e_j))$, we retrieve the shortest path $SP(e_i, e_j)$ and map (x, y) back to $SP(e_i, e_j)$. This process might be repeated a few times as MBRs are much bigger than $SP(e_i, e_j)$ and the fact $(x, y) \in MBR(SP(e_i, e_j))$ does not guarantee $(x, y) \in SP(e_i, e_j)$. Once we get the distance, we can locate the time based on compressed temporal sequence. As a summary, $when_{at}(T, x, y)$ spends $\frac{n}{2\alpha\gamma} + \frac{\alpha+\gamma}{2}$ time unit on spatial process and $\frac{m}{2\beta}$ time unit on temporal process.

range Query. For boolean range query on an original trajectory T , it first locates d_1 and d_2 based on t_1 and t_2 on the temporal sequences, and then retrieves the spatial segment Seg between d_1 and d_2 . It then scans Seg edge by edge and checks whether any edge intersects the query region R . The process on a compressed trajectory T' is similar. Given t_1 and t_2 , it locates d'_1 and d'_2 as described in $when_{at}$ query, and then retrieves points corresponding to d'_1 and d'_2 . As we maintain the MBRs for all the shortest paths and the sub-trajectories captured by Trie, we can first check whether an MBR overlaps with R before recovering the original sub-trajectories. Its time complexity is the same as that under $when_{at}$ query.

Discussion. For all the three queries studied above, the processing over compressed trajectories demonstrates certain non-negligible advantages, compared with the processing over original trajectories. We agree that the gain in terms of performance has a cost of enlarged storage cost, e.g., the storage cost for maintaining the distance for all-pair shortest paths and that for maintaining the MBRs for all-pair shortest paths with both in the scale of $|V|^2$. However, all these auxiliary structures can be pre-processed and can be used for a relatively long duration unless the road network structure changes and/or the movement patterns of the underlying trajectories change significantly. Compared with the large number of trajectories generated daily and the long time period of collection we have to maintain, the extra storage cost incurred by these auxiliary structures can be well-justified. We will further demonstrate it in our simulation study to be presented in Section 6.

PRESS also supports other queries commonly used by LBSs. For instance, it can support queries inquiring trajectories passing near a location point (x, y) within distance d from t_1 to t_2 and queries calculating the minimal distance between two trajectories T_1 and T_2 . Based on these queries, PRESS can support more advanced applications, such as traffic flow analysis, behavior mining and so on [26]. We give more description of this part in our technique report [22].

6. EXPERIMENTS STUDY

In this section, we conduct extensive experiments to demonstrate the effectiveness and efficiency of PRESS. The experiments are based on real trajectory data from one of the

largest taxi companies in Singapore. Each taxi has installed GPS, and it reports its locations regularly. In our studies, we use the trajectories reported within January 2011, in total 465,000 trajectories generated by about 15,000 taxis. The original storage cost of this dataset is 13.2GB. First, we map the GPS locations using the approach proposed in [21] to get the spatial path of the trajectories. Then, we project the sample points onto the spatial path and calculate the distance from the starting point of the trajectory by linear interpolation to generate the temporal presentation of the trajectories¹.

In addition to PRESS framework, we implement *Map-matched trajectory compression* (MMTC) [10] and *Nonmaterial* [4], two state-of-the-art approaches for trajectory compression in road networks, as the representatives of existing approaches. All the algorithms are implemented with C/C++ and run on a computer with Intel Core i7-3770 CPU (3.40 GHz) and 32 GB memory. In the following, we first evaluate the effectiveness of various approaches by reporting the compression ratio; next evaluate the efficiency of various approaches by reporting the time taken; and finally report the flexibility of various approaches by demonstrating their capabilities in supporting common LBSs.

6.1 Compression Effectiveness

In the first set of experiments, we first discuss the effectiveness of our spatial compression algorithm HSC and our temporal compression algorithm BTC, then compare the compression effectiveness of various algorithms. We adopt *compression ratio* as the performance metric. Given a trajectory T and its compressed form T' , the compression ratio is defined as the ratio of T 's storage cost to T' 's storage cost, i.e., $\frac{|T|}{|T'|}$.

First, we report the effectiveness of the spatial compression algorithm HSC. As introduced in Section 3, HSC is a two-stage process, compressing the spatial path based on SP compression first and then based on FST compression. Given a spatial path in a road network, the storage cost of original trajectory T relies on the sampling rate. The higher the sampling rate, the more the points T contains with higher storage cost. However, the sampling rate does not affect SP compression that much. As shown in Fig. 10(a), we demonstrate the power of SP compression under different sampling rate. Via changing the sampling rate from 1 second/point to 60 seconds/point, the SP compression on average can achieve a compression ratio of 1.52. It is very close to the compression ratio of the sampling rate 30 seconds/point, which is also the median sampling rate of the trajectory dataset we use.

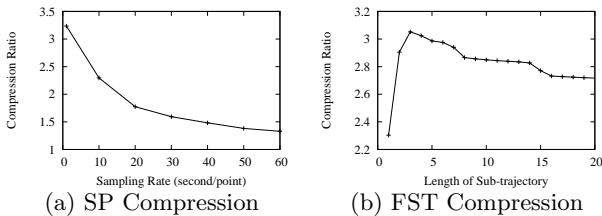


Figure 10: Compression Ratio of HSC

In the second stage, we compress the spatial path via FST, with its compression ratio under different θ (i.e., the length

of the sub-trajectories in Trie) reported in Fig. 10(b). Note, assume T is an original spatial path, T' is the compressed trajectory via SP compression, and T'' is the compressed trajectory via FST compression, the compression ratio reported here is the ratio of T'' 's storage cost to T' 's (but not T 's) storage cost. We use the trajectory set corresponding to one day as the training set, and change the θ values from 1 to 20. As shown in Fig. 11(a), the compression ratio improves initially with the increase of θ . However, when $\theta > 3$, a bigger θ does not help improve the compression ratio. This is because a larger θ corresponds to a Trie with more nodes, and hence the Huffman tree has to use more bits to represent each node. We set $\theta = 3$ in the following experiments. In real compression applications, the optimal value of θ can be obtained by attempting to compress a subset of the complete trajectory dataset. Our FST compression can achieve the optimal compression ratio of 3.05 when $\theta = 3$. In other words, by combining these two stages (i.e., SP compression and FST compression), our HSC is expected to have an optimal compression ratio of $1.52 \times 3.05 \approx 4.64$.

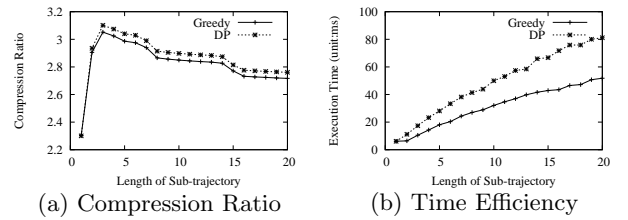


Figure 11: Performance of FST Compression

Recall that for FST compression, we propose a greedy algorithm to decompose a given trajectory into a sequence of sub-trajectories. However, there is actually an optimal approach that results in the maximum compression ratio based on dynamic programming. Given a trajectory T' compressed via SP compression, the main idea is to invoke dynamic programming to calculate the splitting solution of T' . Assume $T' = \langle e_1, e_2, \dots, e_i \rangle$ and F_k is the minimum storage cost of the prefix k edges of T' , then $F_k = \min_{\forall j < k} (F_j + Huf(e_{j+1}e_{j+2} \dots e_k))$. Here, $Huf(S_{jk})$ represents the Huffman code length of a string S_{jk} in the Trie. Initially, $F_0 = 0$. Thereafter, we can derive the optimal splitting point based on dynamic programming. Although this algorithm can generate a compressed trajectory with minimum storage cost, its time complexity is high. Alternatively, we propose a greedy algorithm, as presented in Section 3. In order to demonstrate that our greedy algorithm can achieve a performance comparable with that of dynamic programming but with a much cheaper time cost, we compare these two approaches in Fig. 11. As observed from Fig. 11(a), the compression ratio of our greedy algorithm is almost the same as that achieved by dynamic programming, with only around 1% difference. However, as shown in Fig. 11(b), our greedy algorithm is much faster, as it only incurs around 65% of dynamic programming's time on average. Consequently, our choice of greedy algorithm is well justified.

After presenting the performance of spatial compression, we are ready to present the performance of temporal compression. As our temporal compression algorithm BTC takes TSND and NSTD as inputs, we report the compression ratio under different TSND and NSTD settings in Fig. 12(a). To be more specific, the value of TSND changes from 0, 10,

¹The source code is available at <https://github.com/RenchuSong/PRESS>.

20, 50, 100, 200, 400, 600, 800, to 1000 (unit: meter), and the value of NSTD changes from 0, 10, 20, 50, 100, 200, 400, 600, 800, to 1000 (unit: second). It is noticed that even when $TSND = NSTD = 0$, BTC can still achieve a compression ratio of 1.1. This is because around 10% of the trajectory sampling points tell that the taxi is not moving (e.g., waiting at a taxi drop-off point, or stuck in a traffic jam). In general, the larger the $TSND$ and/or $NSTD$ are, the higher the compression ratio is, which is consistent with our expectation. For example, when $TSND = 1000m$ and $NSTD = 1000s$, the compression ratio is as high as 6.49.

Now considering both spatial compression and temporal compression, we plot the overall compression ratio of our newly compression framework PRESS in Fig. 12(b), under various $TSND$ and $NSTD$ values. We assume the initial trajectory is represented by (x, y, t) tuples. We then re-format the trajectory as a spatial path and a time sequence, and invoke HSC to compress the spatial path and invoke BTC to compress the time sequence based on $TSND$ and $NSTD$ settings. Our approach is effective. Even when $TSND = NSTD = 0$, PRESS still achieves a compression ratio of 2.71 (i.e., can save around 63% storage cost). As $TSND$ and/or $NSTD$ increase, the compression ratio is also improved. For example, when $TSND = 1000m$ and $NSTD = 1000s$, the compression ratio is 8.52.

Finally, we present the overall compression ratio of all three algorithms (i.e., our PRESS framework and two competitors) in Fig. 13. Notice that existing works are not bounded by $NSTD$ and $TSND$ but only by $TSED$ and hence the results are presented based on various $TSED$ values. It is very obvious that our approach is able to achieve a much higher compression ratio than existing ones. The higher the $TSED$ is, the more significant the advantage of PRESS is. For example, when $TSED = 0$, our approach can improve MMTC’s compression ratio by 64% and it can improve Nonmaterial’s compression ratio by 43%; when $TSED = 600m$, our approach can improve MMTC’s compression ratio by 280% and Nonmaterial’s compression ratio by 199%. We also use the standard ZIP and RAR algorithm to compress the trajectory. The compression ratio of ZIP is 2.09, and that of RAR is 3.78. Although both algorithms are lossless, the compressed trajectories lose their utility totally. That is to say, the compressed trajectories have to be fully decompressed before use. Moreover, the compression ratio of PRESS is better than that of ZIP even when $TSND = NSTD = 0$, and it beats RAR when $TSED > 230m$. As a summary, our approach is very effective in terms of compressing trajectories, which is the main objective of the compression framework proposed in this work. The experimental results well demonstrate the power of our framework and hence justify the design.

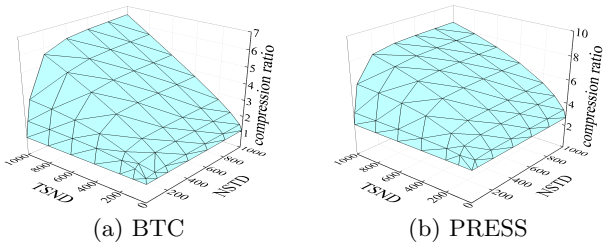


Figure 12: Compression Ratio vs. $TSND$ and $NSTD$

6.2 Compression Efficiency

Although the main objective of PRESS framework is to save space, the time complexity is also important. Ideally, we prefer a compression algorithm that can effectively cut down the storage cost and meanwhile is time efficient. Consequently, we report the time taken by each algorithm when compressing trajectories, and we also report the time taken by each algorithm for decompressing trajectories. It is noticed that MMTC does not support decompression as the compressed trajectories cannot be recovered.

In terms of trajectory compression, MMTC is the most time-consuming. The average compression time cost of MMTC is 196.5 times of PRESS. Moreover, our approach is faster than Nonmaterial, and it on average only requires 72% of Nonmaterial’s time. Furthermore, PRESS also outperforms both ZIP and RAR in terms of time efficiency. It only takes around 24.6% of ZIP’s time and 13.0% of RAR’s time. For decompression, our approach consumes 58.7% time of Nonmaterial, 56.1% time of ZIP, and 74.5% time of RAR on average. The reason behind is that Nonmaterial contains arithmetic of real numbers to calculate the timestamps during decompression, while our approach only needs to visit the Huffman tree, Trie and shortest path table for recovery of the trajectories. Consequently, we can conclude that our approach is most time efficient, for both compression and decompression operations.

Some may argue that our approach relies on auxiliary structures, namely the shortest path table, the AC automation and the Huffman tree. Here, we want to point out that these structures are static and they are only constructed once. For the real dataset we use, they take space of 452MB, 101MB and 121MB respectively, which is absolutely acceptable for modern computation platforms. Compared with the storage saving they achieve for compressing trajectories, the cost of constructing these structures and maintaining these structures is well justified.

6.3 Supporting LBS applications

As mentioned before, our framework not only can effectively compress the trajectories, but also can support some popular spatial-temporal queries commonly used by many LBSs, even when the trajectories are in the compressed form. In the following, we report their time performance for supporting different queries. For a given query q , an original trajectory dataset TD and a compressed trajectory dataset TD' , let $t(q, TD)$ and $t(q, TD')$ represent the time duration taken by processing the query q over the dataset TD and TD' respectively. We report the time performance ratio (i.e., $\frac{t(q, TD')}{t(q, TD)}$) instead of the time duration for each query.

First, we study the *where_{at}* query, with its performance shown in Fig. 14 under various distance deviations. In general, the time performance depends on the distance deviation. The higher the deviation, the higher the compression ratio and hence the faster the query processing. PRESS is most efficient, and it on average only takes 26% of the time spent in original uncompressed trajectory dataset. Compared with its two competitors, PRESS saves around 34% of MMTC’s time and roughly 28% of Nonmaterial’s time.

Second, we study the *when_{at}* query, with its performance shown in Fig. 15 under various time deviations. Again, our approach significantly outperforms the other two approaches. On average, it only incurs 30% of MMTC’s time

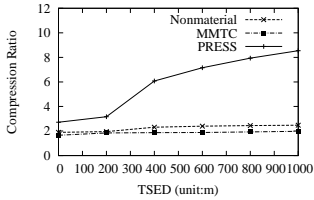


Figure 13: Compression ratio performance

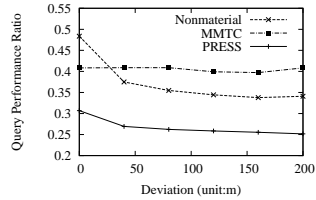


Figure 14: Performance of *where_at* query

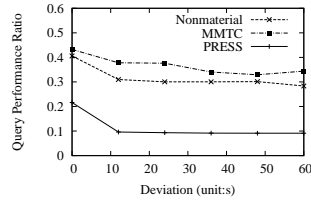


Figure 15: Performance of *when_at* query

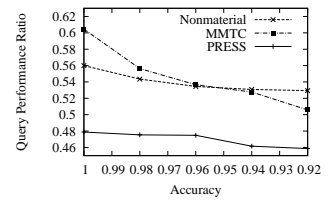


Figure 16: Performance of *range* query

and incurs around 35% of Nonmaterial’s time.

Then, we study the range query and report its performance under different accuracy in Fig. 16. Unlike previous two queries, the range query returns a boolean value and it is not error bounded under any of the compression scheme studied in this evaluation. For example, when there are a large number of trajectories located near the boundary of the queried spatial range at the queried temporal period, the lossy temporal compression of our approach and Nonmaterial may result in wrong query result. On the other hand, MMTC is even worse, as it compresses the trajectories in such a way that it loses both the spatial information and the temporal information to certain degree. Consequently, we randomly generate 2,325,000 range queries, and then cluster queries based on the accuracy. Again, PRESS works the best, and it can save around 14% of the time, compared with both MMTC and Nonmaterial.

Although PRESS demonstrates excellent performance in all the above mentioned common spatial queries, it has to maintain certain auxiliary structures. If we only consider above three queries, our new framework needs to maintain the distance information of all-pair shortest path which takes around 904MB space, the distance information between Trie nodes which takes roughly 201MB space, the MBRs for all-pair shortest path which take 904MB space, and Trie MBR information which takes another 805MB space. However, given trajectories in a real road network which is relatively stable, the overhead of these auxiliary structures is acceptable, especially when these structures can significantly improve the query performance and they can be used for a long period. We want to highlight that for fair competition, we also maintain several auxiliary structures for MMTC and Nonmaterial. We give more description of this part in our technique report [22].

7. RELATED WORK

In this section, we review related work to trajectory compression. They are roughly clustered into two groups, one to compress a trajectory using line simplification methods and the other based on map-matching algorithms.

7.1 Trajectory Simplification

Line simplification is to approximate a polyline with a subset of the vertices from the original one. These algorithms are used to compress Euclidean space trajectories. Existing line simplification algorithms can be categorized as either batch model based or online compression. According to an experimental study [17] that compares the major compression approaches, no approach outperforms others under all scenarios as they have their pros and cons.

Batch Model Based. Those line simplification methods falling this category discard some locations with negligible error from an original trajectory which is already wholly

obtained before the process [26]. The uniform sampling algorithm is an efficient (but not error-bounded) simplification method that keeps every i th points and discards others. The Douglas-Peucker (DP) algorithm [5, 7] approximates a trajectory by a line segment and recursively selects the point contributing the biggest error as a split point, until the trajectory satisfies the error requirement. Quite a few variants have been proposed to improve the original DP algorithm [15], e.g., replacing the perpendicular distance with the time synchronized Euclidean distance or a time-distance ratio metric that considers both spatial and temporal information [16], and a bottom-up algorithm that starts from the consecutive sample points and approximates step by step by merging the consecutive segments into one line segment which introduces the least error [12]. The Bellman’s algorithm [2] uses dynamic programming to minimize the “area” between the original trajectory and the compressed one. However, the time complexities of the original DP method and Bellman’s algorithm are $O(|T|^2)$ and $O(|T|^3)$ respectively. Some improved implementations of DP-variants can achieve a complexity of $O(|T|\log|T|)$, and that of Bellman’s algorithm can be $O(|T|^2)$.

As compared with this category of algorithms, PRESS also works on batch model. In addition, the complexity of PRESS is $O(|T|)$, much more efficient than DP-variants and Bellman’s algorithms. Recently, a Spatial Quality Simplification Heuristic Extended approach [18] has been proposed with the time complexity of $O(|T|)$, achieving a relatively low error in Euclidean spaces. Different from this approach, PRESS works in road network spaces, in which we face more constraints. Furthermore, PRESS is spatial lossless and temporal error-bounded.

Online compression. Algorithms of this category compress the trajectories that are being generated, i.e., we need to make a decision whether the recently received point should be reserved or not online. The reservoir sampling algorithm [24] uses the replace strategy to keep no more than a maximal number of sample points to assure that each point shares the same probability to be kept at last. The sliding window approach [16, 11], on the other hand, tries to simplify the points within a sliding window with a line. The sliding window keeps growing until the simplification exceeds the error limitation. The sliding window approach also inspires other variations, such as the opening window approach [16] and Dead Reckoning [23]. Other approaches argue that a point should be included in the compression result as long as it reveals significant change of the movement. Given speed and direction error bounds, the STTrace algorithm [20] uses the concept of safe area to generate a simplified trajectory. Alternatively, work presented in [16] explores the speed information and uses the speed difference of two sub-trajectories as an error metric to determine whether to reserve a sample point.

Although PRESS focuses on batch model based trajectory compression, the compression procedure scans the spatial path and temporal sequence from head to tail without tracing back. This means PRESS can be adapted to online compression. In BTC, we propose a novel angular-range approach with a time complexity of $O(|T|)$ based on a variant of the opening window method whose original complexity is $O(|T|^2)$. Additionally, the trajectory compressed by PRESS can be directly used to answer spatial-temporal queries without being fully decompressed.

7.2 Map-Matching Based Compression

This fold of compression methods first projects a trajectory onto a road network using a map-matching algorithm [3, 13, 19, 21], and then reduces the storage of the trajectory that has been represented as a sequence of road segments. Here, we review two representatives, Nonmaterial [4] and MMTC [10]. Nonmaterial uses the street information to represent the spatial information. It calculates the timestamps of the intersections based on the timestamps of the original sampled points and the spatial locations of their snapped projections on the roads, under the assumption of uniform speed movement. MMTC uses sub-trajectories through fewer intersections to replace parts of the original trajectory. Some specific evaluation functions are introduced during the compression to guarantee the similarity between the compressed trajectory and the original one. The compressed trajectory consists of fewer intersections, thus the storage cost is reduced.

To the best of our knowledge, Nonmaterial and MMTC are the only techniques focusing on trajectory compression in road networks. Different from these two approaches, we compress the spatial component and temporal component of a trajectory separately. In the meantime, the spatial compression reduces the storage of a trajectory tremendously by using the sequential patterns mined from the trajectory corpus to encode the trajectory. As a result, our approach achieves a much higher compression ratio with a linear time complexity. According to the extensive experiments, PRESS outperforms both Nonmaterial and MMTC in terms of both effectiveness and efficiency.

8. CONCLUSION

In this paper, we propose a new framework, namely PRESS, for trajectory compression. To be more specific, PRESS represents a given trajectory using a spatial path and a temporal sequence and then employs different algorithms to compress the spatial path and temporal sequence, respectively. We have conducted extensive experiments to evaluate the performance of PRESS on a real data set, i.e., the Singapore taxi trajectories collected within one month. The simulation results demonstrate the superior compression power of PRESS. In the near future, we plan to formalize the selection of the θ value for FST compression, and we will collect more types of real trajectories (e.g., pedestrian trajectory) to evaluate how PRESS works in different application scenarios.

9. ACKNOWLEDGMENTS

This work is partially supported by the National Natural Science Foundation of China (NSFC) under grant No. 61073001 and Shanghai Leading Academic Discipline Project, Project Number: B114. Zheng Baihua was funded in the Singapore Management University through a research grant

(14-C220-SMU-001) from the Ministry of Education Academic Research Fund Tier 1.

10. REFERENCES

- [1] Alfred V. Aho and Margaret J. Corasick. Efficient string matching: an aid to bibliographic search. *CACM*, 18(6):333–340, 1975.
- [2] Richard Bellman. On the approximation of curves by line segments using dynamic programming. *CACM*, 4(6):284, 1961.
- [3] Sotiris Brakatsoulas, Dieter Pfoser, Randall Salas, and Carola Wenk. On map-matching vehicle tracking data. In *VLDB'05*, pages 853–864, 2005.
- [4] Hu Cao and Ouri Wolfson. Nonmaterialized motion information in transport networks. In *ICDT'05*, pages 173–188, 2005.
- [5] David H. Douglas and Thomas K. Peucker. Algorithms for the reduction of the number of points required to represent a digitized line or its caricature. *Cartographica*, 10(2):112–122, 1973.
- [6] Jiawei Han, Micheline Kamber, and Jian Pei. *Data mining: concepts and techniques*. Morgan Kaufmann, 2006.
- [7] John Edward Hershberger and Jack Snoeyink. *Speeding up the Douglas-Peucker line-simplification algorithm*. University of British Columbia, Department of Computer Science, 1992.
- [8] David A. Huffman. A method for the construction of minimum-redundancy codes. *IRE*, 40(9):1098–1101, 1952.
- [9] Donald E. Knuth. *The art of computer programming: Volume 3/Sorting and searching*. Addison-Wesley, 1973.
- [10] Georgios Kellaris, Nikos Pelekis, and Yannis Theodoridis. Map-matched trajectory compression. *JSS*, 86(6):1566–1579, 2013.
- [11] Eamonn Keogh, Selina Chu, David Hart, and Michael Pazzani. An online algorithm for segmenting time series. In *ICDM'01*, pages 289–296, 2001.
- [12] Eamonn J. Keogh and Michael J. Pazzani. An enhanced representation of time series which allows fast and accurate classification, clustering and relevance feedback. In *KDD'98*, pages 239–243, 1998.
- [13] Yin Lou, Chengyang Zhang, Yu Zheng, Xing Xie, Wei Wang, and Yan Huang. Map-matching for low-sampling-rate gps trajectories. In *GIS'09*, pages 352–361, 2009.
- [14] Wuman Luo, Haoyu Tan, Lei Chen, and Lionel M. Ni. Finding time period-based most frequent path in big trajectory data. In *SIGMOD'13*, pages 713–724, 2013.
- [15] Robert B. McMaster. A statistical analysis of mathematical measures for linear simplification. *The American Cartographer*, 13(2):103–116, 1986.
- [16] Nirvana Meratnia and A. Rolf. Spatiotemporal compression techniques for moving point objects. In *EDBT'04*, pages 765–782, 2004.
- [17] Jonathan Muckell, Jeong-Hyon Hwang, Catherine T. Lawson, and S. S. Ravi. Algorithms for compressing gps trajectory data: an empirical evaluation. In *GIS'10*, pages 402–405, 2010.
- [18] Jonathan Muckell, Paul W. Olsen Jr, Jeong-Hyon Hwang, Catherine T. Lawson, and S. S. Ravi. Compression of trajectory data: a comprehensive evaluation and new approach. *GeoInformatica*, pages 1–26, Published Online:July,2013.
- [19] Paul Newson and John Krumm. Hidden markov map matching through noise and sparseness. In *GIS'09*, pages 336–343, 2009.
- [20] Michalis Potamias, Kostas Patroumpas, and Timos Sellis. Sampling trajectory streams with spatiotemporal criteria. In *SSDBM'06*, pages 275–284, 2006.
- [21] Renchu Song, Wei Lu, Weiwei Sun, Yan Huang, and Chunan Chen. Quick map matching using multi-core cpus. In *GIS'12*, pages 605–608, 2012.
- [22] Renchu Song, Weiwei Sun, Baihua Zheng, and Yu Zheng. Press: A novel framework of trajectory compression in road networks (<http://arxiv.org/abs/1402.1546>). Technical report, 2014.
- [23] Goce Trajcevski, Hu Cao, Peter Scheuermann, Ouri Wolfson, and Dennis Vaccaro. On-line data reduction and the quality of history in moving objects databases. In *DEWMA'06*, pages 19–26, 2006.
- [24] Jeffrey S. Vitter. Random sampling with a reservoir. *TOMS*, 11(1):37–57, 1985.
- [25] Raymond Chi-Wing Wong and Ada Wai-Chee Fu. Mining top-k frequent itemsets from data streams. *Data Mining and Knowledge Discovery*, 13(2):193–217, 2006.
- [26] Yu Zheng and Xiaofang Zhou. *Computing with spatial trajectories*. Springer, 2011.