Abstract

Algebraic effect handlers, are recently gaining in popularity as a purely functional approach to modeling effects. In this article, we give an end-to-end overview of practical algebraic effects in the context of a compiled implementation in the Koka language. In particular, we show how algebraic effects generalize over common constructs like exception handling, state, iterators and async-await. We give an effective type inference algorithm based on extensible effect rows using scoped labels, and a direct operational semantics. Finally, we show an efficient compilation scheme to common runtime platforms (such as JavaScript, the JVM, or .NET) using a type directed selective CPS translation.

1. Introduction

Algebraic effects (introduced by Plotkin and Power in 2002 [32]) and algebraic effect handlers (introduced by Plotkin and Pretnar in 2009 [31]), are recently gaining in popularity as a purely functional approach to modeling effects. As a restriction on general monads, algebraic effects come with various advantages: they can be freely composed, and there is a natural separation between their interface (as a set of operations) and their semantics (as a handler).

At this time, implementations are usually based on libraries [17, 18, 47], or interpreted run-times [3, 16]. This is unfortunate, because we believe that algebraic effect handlers have wide applicability and should be considered as a basic mechanism for handling effects and control-flow in a wide range of languages – including languages like JavaScript and C#, which have added various specialized constructs over the year for concepts that are naturally expressed using algebraic effects.

In this article, we give an end-to-end overview of practical algebraic effects in the context of a compiled implementation in the Koka language. In particular:

- In Section 2 we present a language design for algebraic effects, and show how algebraic effects subsume many control-flow constructs that are specialized in other languages, e.g. exceptions, state, iterators, async-await, etc. In particular, iterators and async-await are complex constructs that can lead to subtle interactions with other features and require complex compilation mechanisms [4]. Being able to generalize over them using a single well-founded abstraction is a huge win.
- Typing algebraic effects, such that we can check what effects functions can have, and can check that all effects are handled in a program, is a challenge. We show in Section 3 how we can leverage the row-types of Koka, based on scoped labels [21], to implement sound and complete type inference for algebraic effects. A problem with many effect systems is that the inferred types become very large or difficult to understand – we have extensive experience with large effectful programs that suggests that the row-type approach of Koka works well in practice.
- In Section 3.2 we show a novel approach to simplify polymorphic effect types. This turns out to be beneficial for an efficient CPS translation too.
- Operational semantics for algebraic effects in the literature are usually given in a continuation style calculus [3, 17] – this simplifies semantics and is convenient when reasoning about effects. In contrast, we give a more direct operational semantics to algebraic effects using syntactical contexts [46] in Section 4. This does not use continuations but captures the execution context explicitly. For compilation purposes we believe our approach is more convenient. We also prove that well-typed programs cannot go ‘wrong’ under these semantics.
- Section 5 describes efficient compilation of algebraic effects to common runtime platforms (like JavaScript) where we do not have full control over the runtime stack. We show how we can use a type directed selective CPS translation to compile effect handlers efficiently. It turns out that the standard CPS translation does not work for functions with polymorphic effect variables, and in Section 5.3.2 we show a novel technique where we use polymorphic code duplication to dynamically pick the correct runtime representation of such functions.

There is a full implementation of algebraic effects in Koka, see [24] for detailed instructions on how to download it and program with algebraic effects – please try it out.

2. Overview

We are going to demonstrate algebraic effects in the context of Koka – a call-by-value programming language with a type inference system that tracks effects. The type of a function has the form \( \tau \rightarrow \epsilon \tau' \) signifying a function that takes an argument of type \( \tau \), returns a result of type \( \tau' \) and may have a side effect \( \epsilon \). We can leave out the effect and write \( \tau \rightarrow \tau' \) as a shorthand for the total function without any side effect: \( \tau \rightarrow (\epsilon) \tau' \). A key observation on Moggi’s early work on monads [28] was that values and computations should be assigned a different type. Koka applies that principle where
effect types only occur on function types; and any other type, like \(\text{int}\), truly designates an evaluated value that cannot have any effect.

Koka has many features found in languages like ML and Haskell, such as type inference, algebraic data types and pattern matching, higher-order functions, impredicative polymorphism, open data types, etc. The pioneering feature of Koka is the use of row types with scoped labels to track effects in the type system, striking a balance between conciseness and simplicity. The system works very well in practice and has been used to write significant programs [23]. In this article we extend the original system [22] to use algebraic effects and handlers to define new effect types.

In the following sections we give various examples of programming with algebraic effects, where we give particular attention to cases where algebraic effects subsume control-flow constructs that are specialized in many other languages, such as exceptions, iterators, and async-await. The interested reader may take a quick look ahead at Figure 4 to see the precise operational semantics of algebraic effect handlers. For the sake of concreteness, we show all examples in the current Koka implementation but we stress that the techniques shown here apply generally and can be applied in many other languages.

There are various ways to understand algebraic effects and handlers. As described originally [31, 32], the signature of the effect operations forms a free algebra which gives rise to a free monad. Free monads provide a natural way to give exceptional computations into \(\text{maybe}\) values:

\[
\text{fun zeroDiv}(x,y) \{ \\
\quad \text{catch} \{ \text{safediv}(x,y), \text{fun}(s)\} \ (0) \}
\]

has type \((\text{int, int}) \rightarrow (\text{int})\) and is a total function. Note that the Koka syntax \(\{\text{safediv}(x,y)\}\) denotes an anonymous function that takes no arguments.

Besides clauses for each operation, each handler can have a \text{return} clause too: this is applied to the final result of the handled action. In the previous example, we just passed the result unchanged, but in general we may want to apply some transformation. For example, we can transform any exceptional computations into \(\text{maybe}\) values:

\[
\text{fun to-maybe}(\text{action}) \{ \\
\quad \text{handle}(\text{action}) \{ \\
\quad\quad \text{return} x \rightarrow \text{Just}(x) \\
\quad\quad \text{raise}(s) \rightarrow \text{Nothing} \\
\quad \} \\
\}
\]

with the inferred type \((() \rightarrow (\text{exc} \ e \ a) \rightarrow e \text{ maybe}(a))\).

The \text{handle} construct is actually syntactic sugar over the more primitive \text{handler} construct:

\[
\text{handler}(\text{action}) \{ \ldots \} \equiv (\text{handler} \{ \ldots \} )(\text{action})
\]

A \text{handler} just takes a set of operation clauses for an effect, and returns a function that discharges the effect over a given action. This allows us to express \text{to-maybe} more concisely as a \text{function} value:

\[
\text{val to-maybe = handler} \{ \\
\quad \text{return} x \rightarrow \text{Just}(x) \\
\quad \text{raise}(s) \rightarrow \text{Nothing} \\
\}
\]

with the same type as before.

Just like monadic programming, algebraic effects allows us to conveniently program with exceptions without having to explicitly plumb \(\text{maybe}\) values around. When using monads though we have to provide a \text{Monad} instance with a \text{bind} and \text{return}, and we need to create a separate discharge function. In contrast, with algebraic effects we only define the \text{operation} interface and the discharge is implicit in the handler definition.

### 2.2. State: resuming operations

The exception effect is somewhat special as it never resumes: any operations following the \text{raise} are never executed. Usually, operations will \text{resume} with a specific result instead of cutting the computation short. For example, we can have an \text{input} effect:

\[
\text{effect input} \{ \\
\quad \text{getstr}() : \text{string} \\
\}
\]

where the operation \text{getstr} returns some input. We can use this as:

\[
\text{fun checkInput} \{ \\
\quad \text{getstr}() \ 	ext{raises} \rightarrow \text{terminate} \\
\quad \text{otherwise} \rightarrow \text{return} \}
\]

The \text{handle} construct for an effect takes an \text{action} to evaluate and a set of operation clauses. In the above example, the inferred type of \text{catch} is:

\[
\text{catch} : (\text{action} : () \rightarrow (\text{exc} \ e) \ a, h : \text{string} \rightarrow e \ a) \rightarrow e \ a
\]

The type is polymorphic in the result type \(a\) and its final effects \(e\), where the action argument can have the \(\text{exc}\) effect and possibly more effects \(e\). As we can see, the \text{handle} construct discharged the \(\text{exc}\) effect and the final result effect is just \(e\). For example,

\[
\text{fun zerodiv}(x,y) \{ \\
\quad \text{catch}(\{ \text{safediv}(x,y), \text{fun}(s)\} \ (0)) \}
\]

The \text{handle} construct discharged the \(\text{exc}\) effect and the final result effect is just \(e\). For example,
fun hello() {
    val name = getstr()
    println("Hello " + name)
}

An obvious implementation of getstr gets the input from the user, but we can just as well create a handler that takes a set of strings to provide as input, or always returns the same string:

val always-there = handler {
    return x -> x
    getstr() -> resume("there")
}

Every operation clause in a handler brings an identifier resume in scope which takes as an argument the result of the operation and resumes the program at the invocation of the operation – if the resume occurs at the tail position (as in our example) it is much like a regular function call. Executing always-there(hello) will output:

> always-there(hello)
Hello there

As another example, we will define a stateful effect:

effect state(s) {
    get() : s
    put(x : s) : ()
}

The state effect is polymorphic over the values s it stores. For example, in

fun counter() {
    val i = get()
    if (i <= 0) then () else {
        println("hi")
        put(i - 1);
        counter()
    }
}

the type becomes () → ⟨state(int).console.div|e⟩ () with the state instantiated to int. To define the state effect we could use the built-in state effect of Koka, but a cleaner way is to use parameterized handlers. Such handlers take a parameter that is updated at every resume. Here is a possible definition for handling state:

val state = handler(s) {
    return x -> (x,s)
    get() -> resume(s,s)
    put(s') -> resume(s',())
}

We see that the handler binds a parameter s (of the polymorphic type s), the current state. The return clause returns the final result tupled with the final state. The resume function in a parameterized handler takes now multiple arguments: the first argument is the handler parameter used when handling the resumption, while the last argument is the result of the operation. The get operation leaves the current state unchanged, while the put operation resumes with its passed-in state argument. The function returned by the handler construct now takes the initial state as an extra argument:

state : (x: s, action : ()) → ⟨state(s) | e⟩ a → e(a,s)

and we can use it as:

> state(2,counter)
hi
hi

2.3. Iterators

Many contemporary languages, like JavaScript or C#, have special syntax and compilation rules for iterators and the yield statement [41]. Algebraic effects generalize over this where the yield effect can be defined as:

effect yield(a) {
    yield(item : a) : ()
}

The yield effect generalizes over the values a that are yielded. For example, we can define an “iterator” over lists as:

fun iterate(xs : list(a)) : yield(a) () {
    match(xs) {
        Nil -> ()
        Cons(x,xx) -> { yield(x); iterate(xx) }
    }
}

and similarly for many data structures. Orthogonal to the iterators, we can define handlers that handle the yielded elements. For example, here is a generic foreach function that applies a function f to each element that is yielded and breaks the iteration when f returns False:

fun foreach(f : a → e bool, action : () → ⟨yield(a) | e⟩ () : e) {
    handle(action) {
        return x -> ()
        yield(x) → if (f(x)) then resume() else ()
    }
}

Note how we can stop the iteration simply by not calling resume – and that we can define this behavior orthogonal to the definition of any particular iterator.

2.4. Ambiguity: multiple resumptions

You can enter a room once, yet leave it twice.
— Peter Landin [19, 20]

In the previous examples we looked at abstractions that never resume (e.g. exceptions), and abstractions that resume once (e.g. state and iterators). Such abstractions are common in most programming languages. Less common are abstractions that can resume more than once. Examples of this behavior can usually only be found in languages that implement some variant of callcc [43]. A nice example to illustrate multiple resumptions is the ambiguity effect:

effect amb {
    flip() : bool
}

where we have a flip operation that returns a boolean. As an example, we take the exclusive or of two flip operations:

fun xor() : amb bool {
    val p = flip()
    val q = flip()
    ((p || q) & & ! (p & & q))
}

There are many ways we may assign semantics to flip. One handler just flips randomly:

val coinflip = handler {
    flip() → resume(random-bool())
}
with type \( (\text{action}: () \rightarrow (\text{amb} \cdot \text{ndet} \cdot e) \cdot a) \rightarrow (\text{ndet} \cdot e) \cdot a \)
where \( \text{random}-\text{bool} \) induced the (built-in) non-deterministic effect \( \text{ndet} \). A more interesting implementation though is to return all possible results, resuming twice for each \( \text{flip} \) once with a \( \text{False} \) result, and once with a \( \text{True} \) result:

```plaintext
val amb = handler {
    return x \rightarrow [x]
    flip() \rightarrow resume(\text{False}) + resume(\text{True})
}
```

with type \( (\text{action}: () \rightarrow (\text{amb} \cdot e) \cdot a \rightarrow e \cdot \text{list}(a)) \),
discharging the \( \text{amb} \) effect and lifting the result type \( a \) to a \( \text{list}(a) \) of all possible results. The return clause wraps the final result of the action in a list, while in the \( \text{flip} \) clause we append the results of both resumptions (using \( + \)). Since each resume is handled by the same handler, the results of each resumption will indeed be of type \( \text{list}(a) \). For example, executing \( \text{amb}(:\text{xor}) \) leads to:

```plaintext
> \text{amb}(:\text{xor})
[\text{False}, \text{True}, \text{True}, \text{False}]
```

Multiple resumptions should be used with care though as the composition with other effects can sometimes be surprising. As an example, consider a program that uses both \( \text{state} \) and ambiguity:

```plaintext
fun surprising() : (\text{state}(\text{int}), \text{amb}) \rightarrow \text{bool} {
    val p = flip()
    val i = get()
    put(i+1)
    if (i \geq 1 \&\& p) then \text{xor}() else \text{False}
}
```

We can use our earlier handlers to handle the state and ambiguity effects, but we can compose them in two ways, giving rise to two different semantics. First, we can handle the state outside the ambiguity handler, giving rise to a “global” state that is shared between each ambiguous assumption:

```plaintext
> \text{state}(0, \{ \text{amb}(:\text{surprising}) \})
([\text{False}, \text{True}, \text{True}, \text{True}, \text{False}], 2)
```

The final result is a tuple of a list of booleans and the final state. Since the state is shared, only the first time \( (i \geq 1 \&\& p) \) is evaluated the result will be \( \text{False} \) (the first element of the result list). On the second resumption, \( \text{xor}() \) will be evaluated leading to the other 4 elements. If we change the order of the handler, we effectively make the state local to each ambiguous resumption:

```plaintext
> \text{amb}(: \{ \text{state}(0, \text{surprising}) \})
([\text{False}, \text{True}, \text{True}, \text{True}, \text{False}], 2)
```

and the result is now a list of tuples. In both resumptions of the first \( \text{flip} \) the \( i \) will be the initial state leading to two \( \text{False} \) elements in the result list. Note how, in contrast to general monads, algebraic effects can be composed freely (since they are restricted to the free monad). This is quite an improvement over previous work \([39, 45]\) where composing different monads required implementing a combined monad by hand.

### 2.5. Asynchronous programming

Similarly to iterators, many programming languages are adding support for async-await style asynchronous programming \([42]\). For example, web servers written in JavaScript using NodeJS are highly asynchronous and without language support the resulting programs are difficult to write and debug due to excessive callbacks (e.g. the so-called “pyramid of doom”). However, extending a language with async-await is non-trivial, both in terms of semantics, as well as compilation complexity where async methods need to be translated into state-machines to simulate co-routine behavior \([4]\).

Again, algebraic effect handlers generalize naturally over this pattern. In contrast to the earlier examples we can generally not implement this directly in our language but need to use primitives of the host system. For concreteness, we assume NodeJS as our host with a primitive to call readline:

```plaintext
def readstring(onInput : string \rightarrow (\text{promise})) \rightarrow \text{io}() {
    \text{prim-readline} : (\text{oninput} : \text{string} \rightarrow (\text{promise})) \rightarrow \text{io}()
}
```

which calls its argument callback on successful input. We can now define a asynchronous effect as:

```plaintext
def async {
    \text{readline}() \rightarrow \text{prim-readline}(\text{resume})
}
```

We see that the \text{readline} clause just returns and exits the program to the outer NodeJS event loop. However, it registered \text{resume} as the callback – effectively resuming with the result input when available. In the Koka implementation the core library defines \text{async} as an abstract effect with a predefined handler around the \text{main} function. The handled operations are more generic such that library writers can easily wrap any asynchronous primitives provided by the host system.

Using asynchronous operations is straightforward now:

```plaintext
fun ask-age() {
    println("what is your name?")
    val name = \text{readline}()
    println("hello "+name)
}
```

Moreover, since it is just another effect, it composes naturally with any other algebraic effects the user defines, such as state and exceptions. In async-await style programming an async call site is signaled by an \text{await} keyword and each asynchronous method with an \text{async} keyword. This can be helpful for understanding the code. With our effect typing though, the \text{type} signifies the effects code can have and the asynchronicity is immediately apparent through the inferred types of any expression.

```plaintext
ask-age : () \rightarrow (\text{async}, \text{console})()
```

In future work we are planning to write highly robust asynchronous web servers using algebraic effect handlers. A similar technique as shown here is used in multi-core OCaml where one-shot algebraic effects are used to implement concurrency \([11]\).

### 3. Type rules

In this section we give a formal definition of our polymorphic row-based effect system for the core calculus of Koka. The calculus and its type system has been in use for many years now and has been developed from the start using effect types based on rows with scoped labels \([21]\). Originally, user-
defined effects were described using a monadic approach [45] but it turns out that algebraic effects fit the original type system very well with almost no changes. The new system based on algebraic effects is much simpler and allows for free composition of user defined effects.

Figure 1 defines the syntax of expressions, types, and kinds.

![Figure 1. Syntax of expressions, types, and kinds](image)

The type rules for our calculus is given in Figure 3. A type environment \( \Gamma \) maps variables to types and can be extended using a comma: if \( \Gamma \) equals \( \Gamma, x : \tau \), then \( \Gamma' = \sigma \) and \( \Gamma'(y) = \Gamma(y) \) for any \( x \neq y \). A type rule \( \Gamma \vdash \tau : \Sigma \) states that under environment \( \Gamma \), the expression \( e \) has type \( \tau \) with possible effects \( \epsilon \).

The type rules are quite standard. The rule \( \text{var} \) derives the type of a variable with an arbitrary effect \( \epsilon \). We may have expected to derive only the total effect \( \{ \} \) since the evaluation of a variable has no effect at all. However, there is no rule that lets one upgrade the final effect and instead we need to pick the final effect right away. Another way to look at this is that since the variable evaluation has no effect, we are free to assume any arbitrary effect.

The \( \text{lam} \) rule is similar in that it assumes any effect \( \epsilon \) for the result since the evaluation of a lambda is a value. At this rule, we also see how the effect derived for the body \( \{ \} \) shifts to the derived function type \( \tau_1 \rightarrow \tau_2 \). Rule \( \text{app} \) standard and derives an effect \( \epsilon \) requiring that its premises derive the same effect as the function effect.

Finally rules \( \text{inst} \) and \( \text{gen} \) instantiate and generalize types. The generalization rule has an interesting twist as it requires the derived effect to be total. When combining our calculus with polymorphic mutable reference cells, this is required to ensure a sound semantics. This is the semantic equivalent to the syntactic value restriction in ML. In our core calculus we cannot define polymorphic reference cells directly so the restriction is not necessary persé but it seems good taste to leave it in as it required for the full Koka language.

3.1. Type inference

![Figure 2. Row equivalence](image)
Finally, the handle rule types effect handlers. We assume that effect declarations populate an initial environment $\Gamma_0$ with the types of declared operations, and also a signature environment $\Sigma$ that maps declared effect labels to the set of operations that belong to it. We also assume that all operations have unique names, such that given the operation names, we can uniquely determine to which effect $l$ they belong.

The rule handle requires that all operations in the signature $\Sigma(l)$ are part of the handler, and we reject handlers that do not handle all operations that are part of the effect $l$. The return clause is typed with $\Gamma \vdash \text{val} \, x : \tau \, \epsilon$, where $\tau$ is the result type of the handled action. All clauses must have the same result type $\tau_i$ and effect $\epsilon$. For each operation clause $\text{op}_i$(x) → e1 we first look up the type of $\text{op}_i$, find the environment $\tau_i \rightarrow \langle \epsilon \rangle$, and bind $x$ to the argument type of the operation, and bind resume to the function $\tau'_i \rightarrow \tau_i$ where the argument type of resume is the result type of the operation. The derived type of the handler is a function that discharges the effect type $l$.

### 3.2. Simplifying types

The rule app is a little surprising since it requires both the effects of the function and the arguments to match. This only works because we set up things to always be able to infer the effects of functions that are ‘open’ – i.e. have a polymorphic $\mu$ in their tail. For example, consider the identity function:

$$\text{id} = \lambda x. x$$

If we assign the valid type $\forall \, \alpha . \, \alpha \rightarrow \langle \epsilon \rangle \, \alpha$ to the id function, we get into trouble quickly. For example, the application $\text{id}(\text{raise}("ht"))$ would not type check since the effect of $\text{id}$ is total while the effect of the argument contains $\epsilon$. Of course, the type inference algorithm always infers a most general type for $\text{id}$, namely $\forall \, \alpha . \, \alpha \rightarrow \mu \alpha$ which has no such problems.

In practice though we wish to simplify the types more and leave out ‘obvious’ polymorphism. In Koka we adopted two extra type rules to achieve this. The first rule opens closed effects of function types:

$$\Gamma \vdash e : \tau_i \rightarrow \langle \epsilon_i, ..., \epsilon_n \rangle \, \tau_2 \, \epsilon$$

With this rule, we can type the application $\text{id}(\text{raise}("ht"))$ even with the simpler type assigned to $\text{id}$ as we can open the effect type of $\text{id}$ using the open rule to match the effect of $\text{raise}("ht")$. We combine this with a closing rule (which is just an instance of inst/gen):

$$\Gamma \vdash e : \forall \mu . \, \tau_i \rightarrow \langle \epsilon_i, ..., \epsilon_n \rangle \, \tau_2 \, \epsilon$$

During inference, the rule close is applied (when possible) before assigning a type to a let-bound variable. In general, such technique would lead to incompleteness where some programs that were well-typed before, may now be rejected since close assigns a less general type. However, due to open this is not the case: at every occurrence of such let-bound variable the rule open can always be applied (possibly surrounded by inst/gen) to lead to the original most general type – i.e. even though the types are simplified, the set of typeable programs is unchanged.

We have significant experience with the Koka type system in practice with several large programs (up to 14.000 loc) and type simplification works very well in practice. As we will see later in Section 5, the open actually proves essential for an efficient CPS translation of algebraic effects.

### 3.3. Type inference

The type system as defined is closely related to the core type system originally presented for Koka [22], with the main differences that this paper uses a simpler presentation without treating isolated state, and we added the rule for handlers. Since the handler rule is straightforward and can be encoded using regular applications and lambdas, the results in [22] carry over directly.

In particular, we can define syntax directed type rules that are sound and complete with respect to the rules in Figure 3, and there exists a sound and complete type inference algorithm. Due to this, it was very straightforward to change the Koka compiler to type check algebraic effects and handlers as there were no changes to the core type inference algorithm. The main difficulties that needed to be overcome were found in an efficient compilation to common runtime platforms as described in Section 5.

### 4. Operational semantics

In this section we define a precise semantics for our core language with algebraic effect handlers, and show that well-typed programs cannot go ‘wrong’. Even though algebraic effects are originally conceived with a semantics in category theory, we will give a more regular operational semantics. The main reason to do so is that a direct operational semantics is more useful as a guidance for efficient compilation as described in Section 5. Moreover, using a direct operational semantics may help exposing algebraic effects to a wider audience and allows us to use a traditional style proof of soundness.

The operational semantics of our calculus is given in Figure 4 and consists of just five evaluation rules. We use two evaluation contexts: the $E$ context is the usual one for a call-by-value lambda calculus. The $X_{op}$ context is used...
for handlers. In particular, it evaluates down through any
handlers that do not handle the operation \( op \). This is used
to express concisely that the ‘nearest enclosing handler’
handles particular operations.

The first three reduction rules, \((\delta)\), \((\beta)\), and \((let)\) are
the standard rules of call-by-value evaluation. The final two
rules evaluate handlers. Rule \((return)\) applies the return
clause of a handler when the argument is fully evaluated.
Note that this evaluation rule subsumes both lambda- and
let-bindings and we can define both as a reduction to a
handler without any operations:

\[
(\lambda x. e_1)(e_2) \equiv \text{handle(}return x \rightarrow e_1\text{)}(e_2)
\]

and

\[
\text{val } x = e_1; e_2 \equiv \text{handle(}return x \rightarrow e_2\text{)}(e_1)
\]

The next rule, \((handle)\), is where all the action is. Here
we see how algebraic effect handlers are closely related to
delimited continuations as the evaluation rules captures a
delimited ‘stack’ \( X_{op}[op(v)] \) under the handler \( h \). Using a
\( X_{op} \) context ensures by construction that only the innermost
handler containing a clause for \( op \), can handle the operation
\( op(v) \). Evaluation continues with the expression \( e \) but besides
binding the parameter \( x \) to \( v \), also the \( resume \) variable is
bound to the continuation: \( \lambda y. \text{handle}(h)(X_{op}[y]) \). Applying
\( resume \) results in continuing evaluation at \( X_{op} \) with the
supplied argument as the result. Moreover, the continued
evaluation occurs again under the handler \( h \).

Resuming under the same handler is important as it ensures
that our semantics correspond to the original categorial
interpretation of algebraic effect handlers as a fold over
the effect algebra \( [31] \). If the continuation is not resumed
under the same handler, it behaves more like a case statement
doing only one level of the fold. Such handlers are sometimes
called shallow handlers \([17, 26]\).

For this article we do not formalize parameterized hand-
ners as shown in Section 2.2.2. However the reduction rule
is straightforward. For example, a handler with a single pa-
tern \( p \) is reduced as:

\[
\text{handle}(h)(p = v_p)(X_{op}[op(v)])
\]

\[
\rightarrow \{ \text{op}(v) \rightarrow e \in h \}\]

\[
e[x \rightarrow v], p \rightarrow v_p, resume \rightarrow \lambda q y. \text{handle}(h)(p = q)(X_{op}[y])
\]

Using the reduction rules of Figure 4 we can define the eval-
uation function \( \rightarrow \), where \( E[e] \rightarrow E[e'] \) iff \( e \rightarrow e' \). We
also define the function \( \rightarrow^* \) as the reflexive and transitive
closure of \( \rightarrow \).

### 4.1. Optimizing tail-resumptions

From the reduction rules, we can already see some possi-
ble optimizations that can be used to compiler handlers effi-
ciently. For example, if a handler never resumes, we can treat
it similarly to how exceptions are handled and do not need
to capture the execution context. An important other opti-
mization can apply to tail resumptions, i.e. a \( resume \) that
occurs in the tail position of an operation clause. Suppose
we have an operations clause \( h \) with \( op(x) \rightarrow resume(e) \in h \) and
\( resume \notin fv(e) \). In that case, we can derive:

\[
\text{handle}(h)(X_{op}[op(v)])
\]

\[
\rightarrow resume(e)[x \rightarrow v, resume \rightarrow \lambda y. \text{handle}(h)(X_{op}[y])]
\]

\[
\rightarrow (\lambda y. \text{handle}(h)(X_{op}[y])(e[x \rightarrow \ell]))
\]

\[
\rightarrow^* \{ e[x \rightarrow v] \rightarrow^* v' \}
\]

\[
(\lambda y. \text{handle}(h)(X_{op}[y])(v'))
\]

\[
\rightarrow \text{handle}(h)(X_{op}[v'])
\]

That means that in an implementation we do not need to
capture and restore the context \( X_{op} \) at all but can directly
evaluate the operation expression as if it was a regular
function call. Of course, special precautions must be taken
that any operations yielded in the evaluation of \( e[x \rightarrow v] \) are
not handled by any handler in \( \text{handle}(h)(X_{op}) \).

### 4.2. Comparison with delimited continuations

Shan \([37]\) has shown that various variants of delimited con-
tinuations can be defined in terms of each other. Following
Kammar et al. \([17]\), we can define a variant of Danvy
and Filinski’s \( [7] \) shift and reset operators, called \( shift_0 \) and
\( reset_0 \), as:

\[
\text{reset}_0(X_i[\text{shift}_0(\lambda k. e)]) \rightarrow e[k \rightarrow \lambda x. \text{reset}_0(X_i[x])]
\]

where we write \( X_i \) for a context that does not contain a
\( reset_0 \). Therefore, the \( shift_0 \) captures the continuation up
to the nearest enclosing \( reset_0 \). Just like handlers, the cap-
tured continuation is itself also wrapped in a \( reset_0 \). Unlike
handlers though, the handling is done by the \( \text{shift}_0 \) directly instead of being done by the delimiter \( \text{resume} \). From the reduction rule, we can easily see that we can implement delimited continuations using algebraic effect handlers, where \( \text{shift}_0 \) is an operation and \( X_0 \equiv X_{\text{shift}_0} \):

\[
\text{reseta}(e) = \text{handle}(\text{shift}_0(f) \rightarrow f(\text{resume}))(e)
\]

Using this definition, we can show it is equivalent to the original reduction rule for delimited continuations, where we write \( h \) for the handler \( \text{shift}_0(f) \rightarrow f(\text{resume}) \):

\[
\text{reseta}(X_0[\text{shift}_0(\lambda k. e)]) = \text{handle}(h)(X_0[\text{shift}_0(\lambda k. e)]) \rightarrow (f(\text{resume}))[f \rightarrow \lambda k. e, \text{resume} \rightarrow \lambda x. \text{handle}(h)(X_0[x])] \rightarrow (\lambda k. e)(\lambda x. \text{handle}(h)(X_0[x])) \rightarrow e[k \rightarrow \lambda x. \text{handle}(h)(X_0[x])] \equiv e[k \rightarrow \lambda x. \text{reseta}(X_0[x])]
\]

Even though we can define this equivalence in our untyped calculus, we cannot give a general type to the \( \text{shift}_0 \) operation in our system. To generally type shift and reset operations a more expressive type system with answer types is required [1, 6]. Kammar et al. [17] also show that it is possible to go the other direction and implement handlers using delimited continuations but that solution requires mutable reference cells to implement a global handler stack.

### 4.3. Soundness: well typed effect handlers cannot go wrong

Under our semantics, well-typed programs cannot go wrong:

**Theorem 1. (Semantic soundness)**

If \( \Gamma \vdash e : \tau \mid \epsilon \) then either \( e \uparrow \) or \( e \longmapsto v \) where \( \Gamma \vdash v : \tau \mid \epsilon \) and where we use the notation \( e \uparrow \) for a never-ending reduction.

The proof of this theorem consists of showing two main lemmas:

- Show that reduction in the operational semantics preserves well-typing, i.e. subject reduction, and,
- Show that faulty expressions are not typeable.

If programs are closed and well-typed we know from subject reduction that we can only reduce to well-typed terms, which are either faulty, a value, or an expression containing a further redex. Since faulty expressions are not typeable, it must be that evaluation either produces a well-type value or diverges. (Often a soundness proof is done using progress instead of faulty expressions but we use the latter technique since it turns out that for proving state isolation [22] this technique works better).

Subject reduction is stated more precisely as:

**Lemma 1. (Subject reduction)**

If \( \Gamma \vdash e_1 : \tau \mid \epsilon \) and \( e_1 \longmapsto e_2 \) then \( \Gamma \vdash e_2 : \tau \mid \epsilon \).

To show that subject reduction holds we need to establish various other lemmas. Two particularly important ones are the substitution and replacement lemmas:

**Lemma 2. (Substitution)**

If \( \Gamma, x : \forall \tau. \tau \vdash e : \tau' \mid \epsilon \) where \( x \notin \text{dom}(\Gamma) \), \( \Gamma \vdash v : \tau \mid \epsilon \), and \( \forall \tau \not\in \text{tv}(\Gamma) \), then \( \Gamma \vdash e[x \mapsto v] : \tau' \mid \epsilon \).

**Lemma 3. (Replacement)**

If \( D \) is a deduction ending in \( \Gamma \vdash E[e] : \tau \mid \epsilon \), and \( D' \) is a sub-deduction of \( D \) ending in \( \Gamma' \vdash e : \tau' | \epsilon' \) and occurs at the hole of \( E \), and \( \Gamma \vdash e' : \tau' | \epsilon' \), then we have that \( \Gamma \vdash E[e'] : \tau | \epsilon \).

The proofs of these lemmas carry over directly from [46]. Using these lemmas we can prove subject reduction. We focus on the interesting cases for \((\text{left}), (\text{return})\) and \((\text{handle})\):

**Proof. (Subject reduction)**

(\text{left})

We prove by induction over the reduction rules of \( \rightarrow \).

\text{case } \text{val } x = v; \: e \rightarrow e[x \mapsto v]

From \text{let} we have \( \Gamma \vdash v : \sigma | \epsilon \), and \( \Gamma, x : \sigma \vdash e : \tau | \epsilon \), and by Lemma 2, we can derive that \( \Gamma \vdash e[x \mapsto v] : \tau | \epsilon \).

\text{case } \text{handle}(h)(v) = e[x \mapsto v] \text{ with } \text{return } x \rightarrow e \in h(0)

From \text{handle} we have \( \Gamma \vdash v : \tau | \epsilon \) and \( \Gamma, x : \sigma \vdash e : \tau | \epsilon \). Using (1) and Lemma 2 we can derive \( \Gamma \vdash e[x \rightarrow v] : \tau | \epsilon \).

\text{case } \text{handle}(h)(X_0[op(v)]) = e[x \mapsto v, \text{resume} \rightarrow \lambda y. \text{handle}(h)(X_0[y])]

With \( \text{op}(x) \rightarrow \epsilon \in h(0) \): Assume \( op \in \Sigma(l) \). From \text{handle} we have \( \Gamma \vdash X_0[op(v)] : \tau | \epsilon \). By (1) we can derive \( \Gamma \vdash op : \tau_1 \rightarrow (\lambda f. \bot) | \lambda \xi. \text{but } \text{app} \text{ and } \text{op}(v) \), we derive \( \Gamma \vdash v : \tau_1 | \lambda \xi. \text{let } \text{app}(h)(X_0[op(v)]) : \tau_2 \rightarrow \epsilon | \lambda \xi. \text{handle}(h)(X_0[y]) \). Using (3) and Lemma 3, and assuming \( \vdash c : \epsilon \rightarrow \tau \), it follows \( \Gamma \vdash X_0[y] : \tau | \epsilon \). Using (1) and (2), we also have \( \Gamma \vdash \text{handle}(h)(X_0[y]) : \tau_1 | \epsilon \), and through LAM, \( \Gamma \vdash \lambda y. \text{handle}(h)(X_0[y]) : \tau_2 \rightarrow \epsilon | \lambda \xi. \text{and we conclude } \Gamma \vdash e[x \mapsto v, \text{resume} \rightarrow \lambda y. \text{handle}(h)(X_0[y]) \).}

**Proof (Lemma 4.b)**

Suppose \( \Gamma \vdash X_0[op(v)] : \tau \mid \epsilon \) with \( op \in \Sigma(l) \). To be well typed, we must have \( \Gamma \vdash op(v) : \tau_1 \mid \epsilon \) with \( l \in \epsilon' \) (due to (1)). We use induction on the structure of \( X_0 \) to show that \( l \in \epsilon' \) for any \( \Gamma \vdash X_0[op(v)] : \tau \mid \epsilon \).

**case** \( \text{app}(e'(h)) \): Due to the induction hypothesis, the premise in rule \( \text{app} \) is typeable with an effect \( e' \) with \( l \in \epsilon' \) and therefore also in the result effect \( l \in \epsilon' \).

**case** \( \text{val} \: x = X_0[e] : \tau \mid \epsilon \): Similarly to the previous cases, the premise is typed with an effect \( e' \) with \( l \in \epsilon' \) and therefore due to rule \( \text{let} \) the result effect also has \( l \in \epsilon' \).

**proof** \( \text{handle}(h)(X_0) \) with \( op \not\in h \): Since \( op \not\in h \) the handler discharges some effect \( l \) with \( l \not\in \Gamma \). Using rule \( \text{handle} \) and \( \text{app} \) we have a premise \( \Gamma \vdash X_0 : \bot | (l, \xi) \) and a result effect \( \xi(l) \) and thus \( l \in \epsilon' \).
5. Compilation

Compiling algebraic effects efficiently is not straightforward. In particular, as can be seen in the operational semantics of Figure 4, the rule for handlers captures a delimited execution context $X_\text{op}[op(v)]$ which in practice we need to capture the call stack up to the handler.

If we have full control over the runtime system, this can be done in a straightforward manner similarly how many compilers for Scheme and ML implement $callcc$. This approach does not work though when targeting a common runtime platform, like the JVM or the .NET environment. For Koka in particular, we compile to JavaScript to take advantage of the rich libraries and runtime environments (like high performance asynchronous web services in NodeJS).

In these environments we cannot capture the call stack and need to use other mechanisms to implement the effect handlers. One way to avoid capturing the stack, is to translate the program into continuation passing style (CPS) [10]. This makes the evaluation context explicit in the current continuation. For example, Scheme implementations usually use this in order to implement both proper tail-calls, as well as $callcc$, when targeting JavaScript [27, 44, 48]. This was also used in Scala to provide first-class delimited continuations on the JVM platform [36].

With a CPS translation, the evaluation context $X_\text{op}$ essentially disappears since all constructs take an explicit continuation function $k$ as a last argument. For example, the $xor$ function from the Section 2.4 would get CPS translated into:

$$\text{val } xo r = λk. \text{flip} (λp. \text{flip} (λq. kl (p||q) &c& (!p||q)))$$

We can see that an operation call $op(v)$ becomes $op(v,k)$ where $k$ is a function taking the result of the operation call. The reduction rule for handlers essentially becomes:

$$\text{handle} \{ h \} (H_\text{op}[op(v,k)]) \quad → \quad \{ op(x) → e \in h \}$$

where the context $H_\text{op}$ is now strictly a stack of handlers. In an implementation it is straightforward to maintain such 'shadow' stack explicitly.

At first, we tried a full CPS translation in Koka but it turned out to slow down the code significantly. One of the larger programs written in Koka is a markdown processor called Madoko [23]. This program runs usually client-side in the browser and with a full CPS translation it started to use too much resources to run reliably. A better approach was needed.

5.1. A type-directed selective CPS translation.

It has long been recognized that one can selectively CPS transform only parts of the program that need it [8, 9, 35]. In our case, we only have to use CPS translation on those parts that may issue effectful operations. Moreover, since effects are tracked in the type system, we can use a type-directed selective CPS translation (as used by Scala [36] for example).

We built the translation on by Nielsen [9] who introduces a sound selective CPS translation for the simply typed lambda calculus extended with $callcc$ and $throw$. However, the translation by Nielsen applies to monomorphic effects only and we will see that in the presence of polymorphic effect variables the translation becomes more complex.

We define the CPS translation over an explicitly typed core calculus, defined in Figure 5. This is the internal core calculus of Koka generated by type inference. It is essentially System F [15] extended with the effect annotations. In particular, lambda's carry the effect of the body as $e$. Similarly, handlers are annotated with the handled effect type $l$. Finally, there is a special construct $\epsilon(e)$ that opens the effect of $e$ with effect $e$ – this is generated whenever the open rule is applied as discussed in Section 3.2 on simplifying types.

The type checking rules for the explicitly typed core calculus are given in Figure 6. A rule $\vdash e : σ | e$ states that a given expression $e$ has type $σ$ under a given $e$, where the effect $e$ is inherited and not synthesized. We can see this in rule $\text{lam}$ where the annotated effect determines the effect of the body.

5.1.1. Selective translation

For a selective translation we need a function $H$ (for handled effects) that determines based on the type if a CPS translation is needed. The handler function has the form $H(θ, e)$ where $θ$ is a set of 'unhandled' effect variables ($μ$):

$$H(θ, (\epsilon(e))) = H(\emptyset) \lor H(θ, e)$$

$H(θ, \epsilon) = false$

$H(θ, μ) = μ \notin θ$

We also overload $H(l)$ to determine if a particular effect $l$ may need CPS translation. For now, we assume $H(l)$ is always true. In the Koka implementation though, we distinguish built-in effects from user defined effects through the kind system. The built-in effects consist of exceptions (exn), non-termination (dis), non-determinism (ndet), polymorphic state (st/h), and general I/O operations (io). All of these are usually provided directly by the target system (like JavaScript) and can thus be directly compiled without needing CPS translation. This turns out to be a very important optimization as many (leaf) functions do not use any user defined effects and can thus be compiled directly – and implies there is no cost for effect handlers for any code that does not use them.

For any function $f$ with a function type with effect $e$ where $H(θ, e)$ is true, $f$ is translated in CPS style and will have an extra continuation parameter $k$ at runtime. When $H(θ, e)$ is false, the function is compiled as usual without a continuation parameter.

The last case of $H$ for a polymorphic effect variable $μ$ is only false if $μ$ is an element of the set $θ$. In general we always need to assume a CPS translation is needed for any $μ$ as such variable may get instantiated later on with a user-defined effect. However, as we will see, for polymorphic functions we need to generate two translations and the $θ$ set is used to force certain effect variables to be treated as needing no CPS translation.

In the case of polymorphic functions, the simplified types of Section 3.2 turn out to have a performance impact as well: many functions that would otherwise get a type with an open polymorphic effect, are now closed and thus do not need a CPS translation as $H$ will be false. In the Koka core library, this reduced the set of CPS translated functions by over 80%.
5.1.2. Translation rules

Using the $H$ function, Figure 7 defines a type directed selective CPS translation for our explicitly typed core calculus. Each rule of the form $\theta \vdash e \leadsto e$ states that expression $e$ gets translated into a "static expression" $e$ assuming a set of unhandled effect variables $\theta$ (initially empty). Following Nielsen [29], we write the translation itself in a continuation passing style; to distinguish the translation lambda's and applications from the ones in the program we write static applications as $e[e]$ and static lambda's as $\lambda \_$. In a rule $e \leadsto e$ the $e$ expression is a function that takes itself as a continuation function $k$, which takes expressions to cps expressions.

The rules translate explicitly typed core into a untyped lambda calculus. We would have liked the target calculus to be explicitly typed as well, but as we will see, that would require further type rules to deal with variadic functions. In the actual Koka implementation we do translate to an explicitly typed core though.

Most rules are standard, except for the OPEN and LAM rules. Rules CON and VAR pass the value on to the continuation. The TAPP and TLAM rules just pass on the translation of their bodies. In the VAL rule we can see why a continuation based translation works well, as we can pass the binding of $x$ as a static continuation itself. The APP rule is specialized depending on whether effect is CPS translated or not. The HANDLE rule is straightforward but and translates all its subexpressions. In practice we would need to provide a shared binding for $k$ though since the rule as state might duplicate code. The result is an application $\text{handle}_k$ which is a handler for effect $l$. On every target platform this must be implemented as a primitive.

That leaves the OPEN and LAM rules which need more explanation.

5.2. Opening: non-CPS to CPS

The OPEN and OPEN-CPS rules have an open effect. However, opening an effect type $\langle l_1, \ldots, l_n \rangle$ to $\langle l_1, \ldots, l_n \rangle[e]$ may change the runtime representation: in particular, if $l_1$ to $l_n$ are all built-in effects, but $e$ is a handled effect, the function type changes from being non-CPS to CPS translated! – the CPS translated result should now take a continuation $k$ as its last argument. The rule OPEN-CPS defines this case and wraps the non-CPS translated function in a lambda that takes a
continuation \( k \) and applies that \( k \) directly to the result of applying the translated non-CPS function. This is effectively the point where non-CPS functions are lifted into the CPS world at runtime.

### 5.3. Closing: CPS to non-CPS

With the open rules, the runtime representation can be changed directly with a small and constant cost. There is one other place where the runtime representation can change and that is due to type instantiation. Unfortunately, in this case we cannot so easily change the term at runtime. In particular, a function type may be hidden inside some other type. For example, if we define a data type as:

```haskell
type hide(c) = Hid{ f : int → e int }
```

then we can have terms of form Hide(id) : \( \forall \mu. \text{hide}(\mu) \). When this is instantiated it is not clear how to convert such term at runtime back to a non-CPS form. This is a deep problem and in other work on monadic effects [45] led to restrictions on the amount of polymorphism allowed in the effect system to avoid this situation.

Here we take another approach: we are going to try to not change the runtime representation of functions that are CPS translated, even if they are called from a non-CPS context and the continuation argument is lacking. We assume that our target environment supports some form of variadic functions and that we can check at runtime if the \( k \) argument is present or not. This is well supported in JavaScript but it works well in typed environments too. For example, for the .NET target, first-class functions are represented by function objects and we can modify to the `Apply` methods to check if the \( k \) parameter was present.

#### 5.3.1. Assume identity?

At first, we thought it is sufficient to default the continuation parameter to the identity function and assume \( k = \lambda x . x \) if the argument was not present. That approach does not work though in the presence of effect polymorphic higher-order functions. Consider the map function:

```haskell
fun map(xs : list(a), f : a → e b) : e list(b) {
  match(xs) {
    Nil → Nil
    Cons(x, xx) → Cons(f(x), map(xx, f))
  }
}
```

which is effect polymorphic. A naïve CPS translation leads to (assuming a `match` construct and tupling):

```haskell
val map_cps = λ(xs, f, k). k(Cons(x, xx) → f(x, λy. map(xx, f, λyy. k(Cons(y, yy)))) ))
```

Note in particular that \( f \) itself is called as a CPS function with a continuation argument. If we now have a call to `map` where the effect type is immediately instantiated to the empty effect, the continuation argument \( k \) will not be present. For example, the explicitly typed expression,

```haskell
map([], int, int)([1], inc)
```

where we assume \( \text{inc} : \text{int} \to \text{int} \), would get translated to:

```haskell
map([1], inc)
```

Even if `map` would detect that the \( k \) parameter is not present and substitute \( k = \lambda x . x \), this would still go wrong at runtime as `inc` is called inside `map` with a continuation argument!

### 5.3.2. Polymorphic duplication

The solution is to generate two translations of every function polymorphic in some effect \( \mu \) – one is the CPS translation (e.g. \( \text{map}_{\text{cps}} \)), and one is a plain translation (e.g. \( \text{map}_{\text{plain}} \)). We then use a wrapper that chooses either implementation at runtime based on whether the continuation argument is present. For example, the wrapper for `map` becomes:

```haskell
val map = λ(xs, f, k). if k? then map_{cps}(xs, f, k) else map_{plain}(xs, f)
```

where we assume \( k? \) tests if \( k \) was present. The implementation of the question mark operator is dependent on the particular target environment. For example, in our JavaScript backend we can simply use `k ?= undefined`.

The duplicate translation rule is \( \text{LAM-DUP} \) – here we finally use the \( \theta \) set to generate a CPS translated version of the body (using \( \theta / \{ \mu \} \)), and non-CPS version too (using \( \theta \cup \{ \mu \} \)). Finally we generate a wrapper to choose the correct version at runtime. The other two rules, \( \text{LAM} \) and \( \text{LAM-CPS} \) are used for non effect polymorphic functions.

There is a performance advantage too to this translation – similarly to the worker-wrapper transformation [30] a target platform can usually inline most call sites. Since many of these effect polymorphic functions abstract over iteration patterns (like `map`) this gives the target platform more opportunities to optimize loops since the plain versions will be more amenable to common loop optimizations.

Since only the tail of an effect row can be polymorphic, there is no risk of exponential code duplication. Even for the Koka core library which contains many of these higher-order effect polymorphic functions, the code size increased by a modest 20%.

### 5.4. The runtime system

The runtime system needs to implement the `handle` primitive. In general, the `handle` function registers the operation and return clauses and pushes a handler frame for effect \( l \) on the handler stack. When an operation is performed, it searches along the handler stack for a handler frame and calls into the appropriate operation clause with the current continuation as an argument.

In our JavaScript implementation we have refined this where we have a generic handler that implements a trampoline: operations just return to this handler loop where they are handled and resumed. This way we ensure the stack always gets unrolled for code that uses operations – this is essentially implementing proper tail calls (except that the programmer needs to call an operation every once in a while).

### 6. Related work

Algebraic effects were first described by Plotkin and Power [32] as an algebraic model of computational effects. Later Plotkin and Pretnar [31] added algebraic effect handlers to describe exceptions. Various implementations of algebraic effects exist. Kammar et al. [17] show an efficient implementation as a library in Template Haskell where they use a continuation monad to implement handlers. Using first-class patterns, Wu et al. [47] also embed algebraic effects as a library in Haskell. Brady [5] implements algebraic effects as a DSL library in the dependently typed Idris language.

The language Eff [3] is an ML-like language designed around algebraic effect handlers. It also provides support
for dynamic effect resources which can be used to model polymorphic mutable references. There are designs for an effect type system with type inference for Eff [2, 33] based sub-typing and a region system.

The Links language [25] has recently been extended with support for algebraic effect handlers. Just like we reused the original effect system of Koka, Hillerström and Lindley [16] describe how the original Links type system can be naturally extended to handle algebraic effects too. Their system is also based on row-polyiform but they use instead Remy style rows [34] where the kind system is extended to record presence or absence of effects in the row. We believe our approach based on scoped labels [21] is simpler in practice, but the Remy style can be more expressive as it can describe the absence of effects.

Frank [26] is an experimental language based solely on effect handlers where there is no primitive notion of a function: its handlers all the way down. Just like scoped labels, effects may occur multiple times in a row.

In contrast to our work, all of the previous implementations have full control over the runtime stack being implemented as an interpreter, a library, or by using specialized runtimes like OCaml. Also, many other type systems use structural types for the effects where each effect operation (and its type) occurs in the inferred types. In this paper we use a nominal system where a single effect type implies the available operations. We believe this is better in practice to keep inferred types small and understandable. For example, compare the type of the state handler in Section 2.2 with the type inferred in Links [16] (where _ denotes absence):

\[
sig\text{state} : (s) \rightarrow (\text{Comp}(\text{Get},s,\text{Put}(a) \rightarrow (1e),a) \\
\rightarrow \text{Comp}(\text{Get},\_),\text{Put}(\_),\_\_e),a)
\]

where the operations of the state effect are explicit in the type. A drawback of our approach is that an effect handler must handle all operations of a particular effect type, and cannot pick and choose arbitrarily.

There are also approaches to handling effects using monads [39, 45]. A significant drawback of these approaches is that monads do not naturally compose and combining different effects is difficult in these systems. An exception is Filinski’s work on layered monads which do support a similar style of composing effects [12, 13].

7. Conclusion

Algebraic effect handlers concisely describe many complex control-flow constructs in various programming languages. We hope that the language design, the direct operational semantics, and compilation scheme described in this article will contribute to wider adoption of algebraic effects. In the future we plan use algebraic effects to implement strongly typed asynchronous web services in NodeJS.

References


