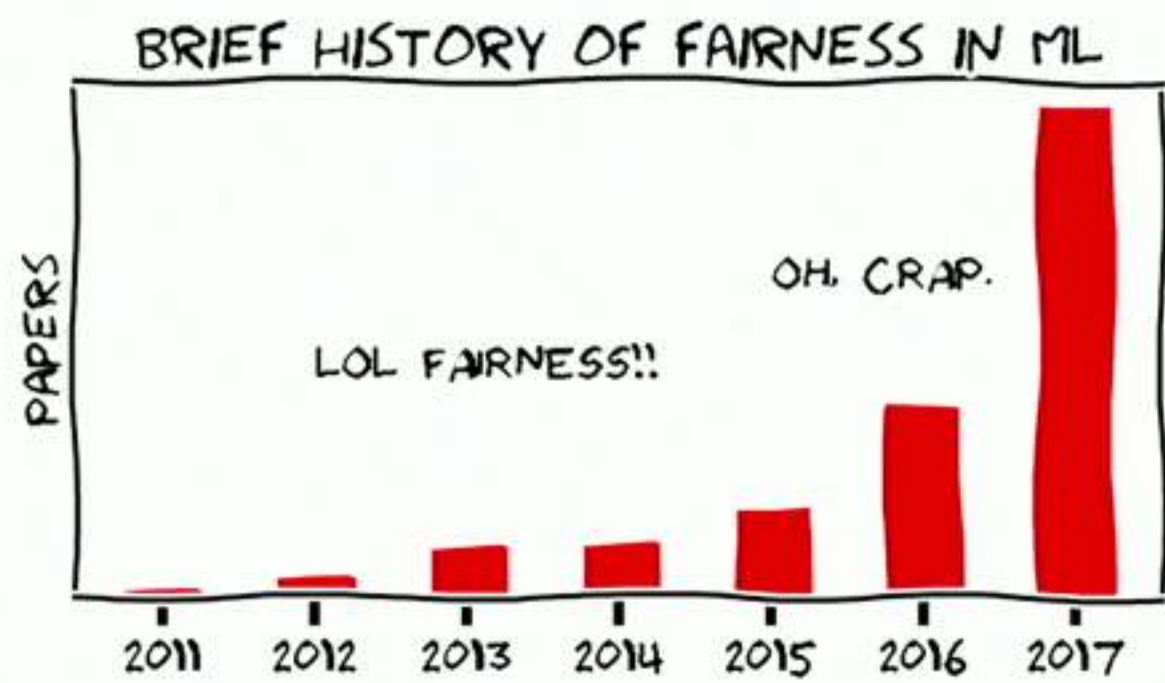


DELAYED IMPACT OF FAIR MACHINE LEARNING

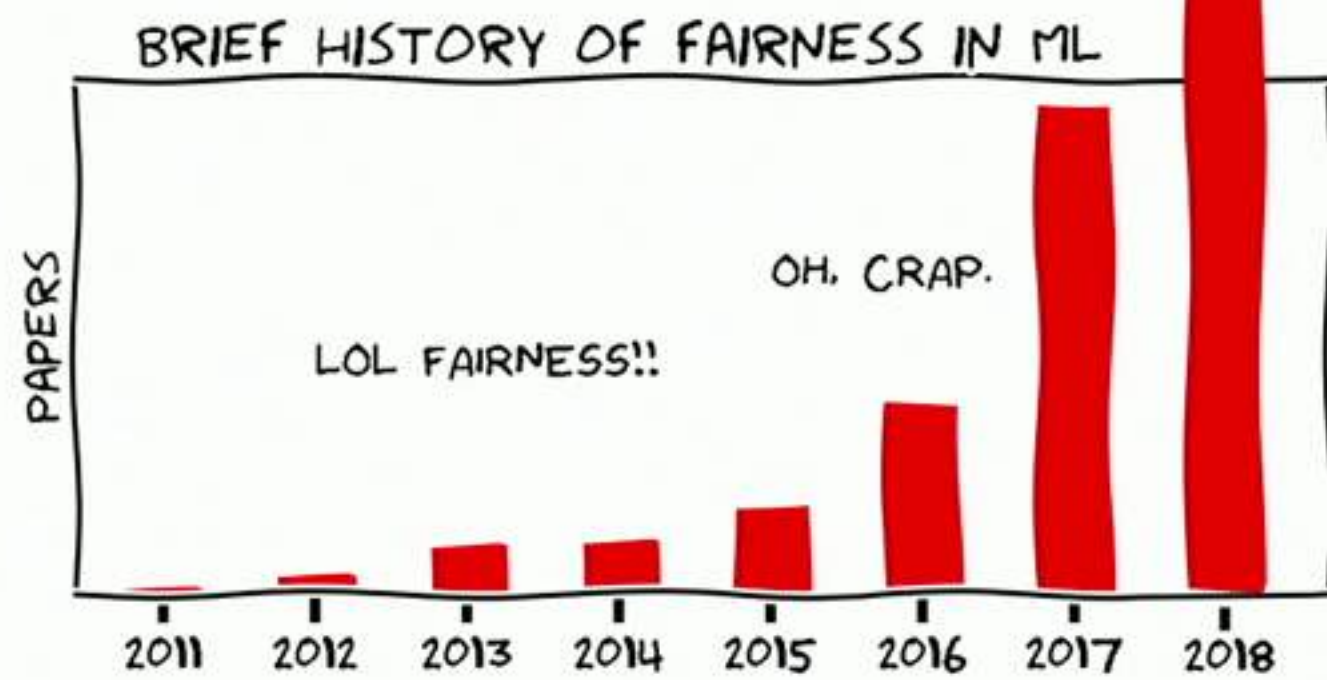
Lydia T. Liu (UC Berkeley)



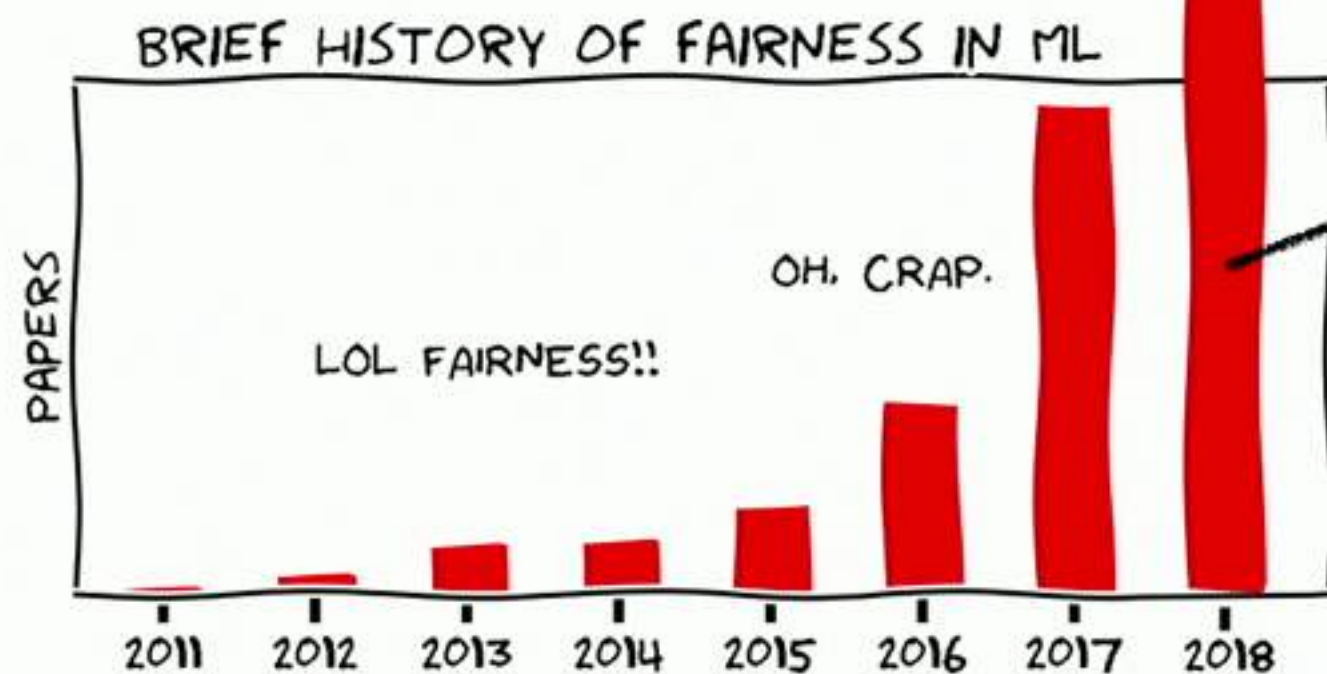
Joint work with **Sarah Dean, Esther Rolf, Max Simchowitz, Moritz Hardt**



source: mrtz.org



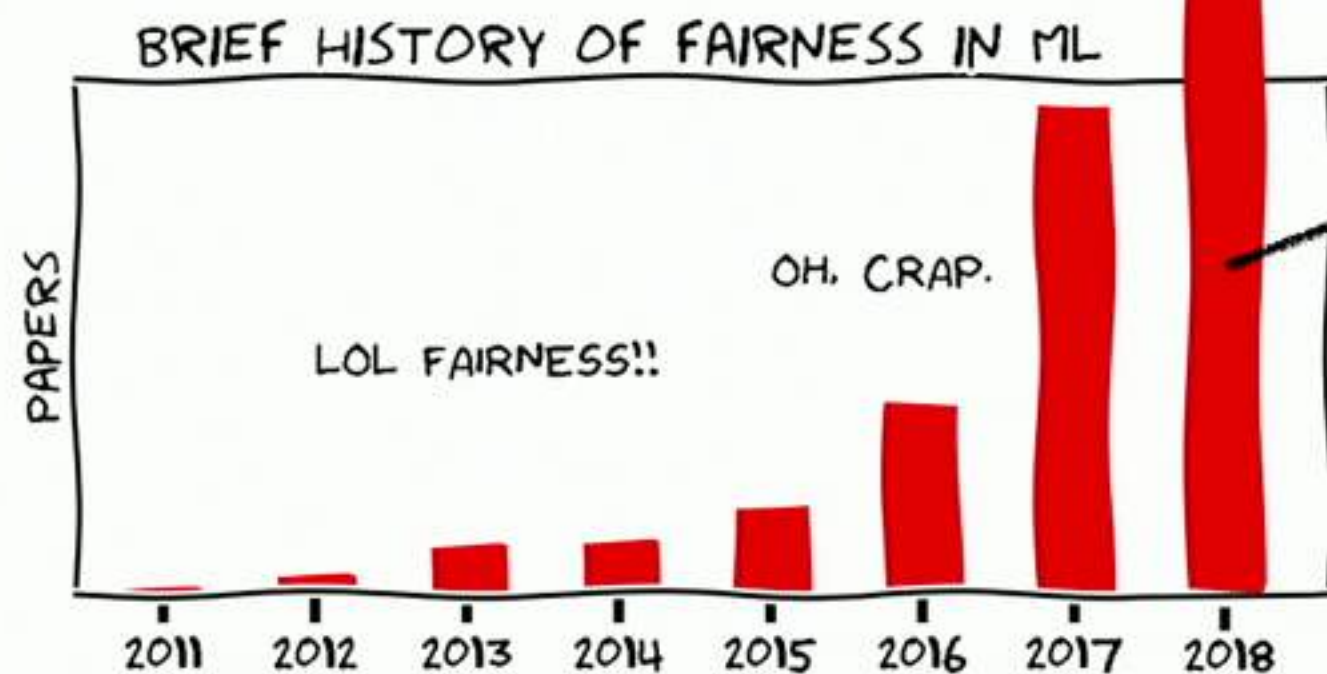
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“21 DEFINITIONS OF FAIRNESS” [Narayanan 2018]

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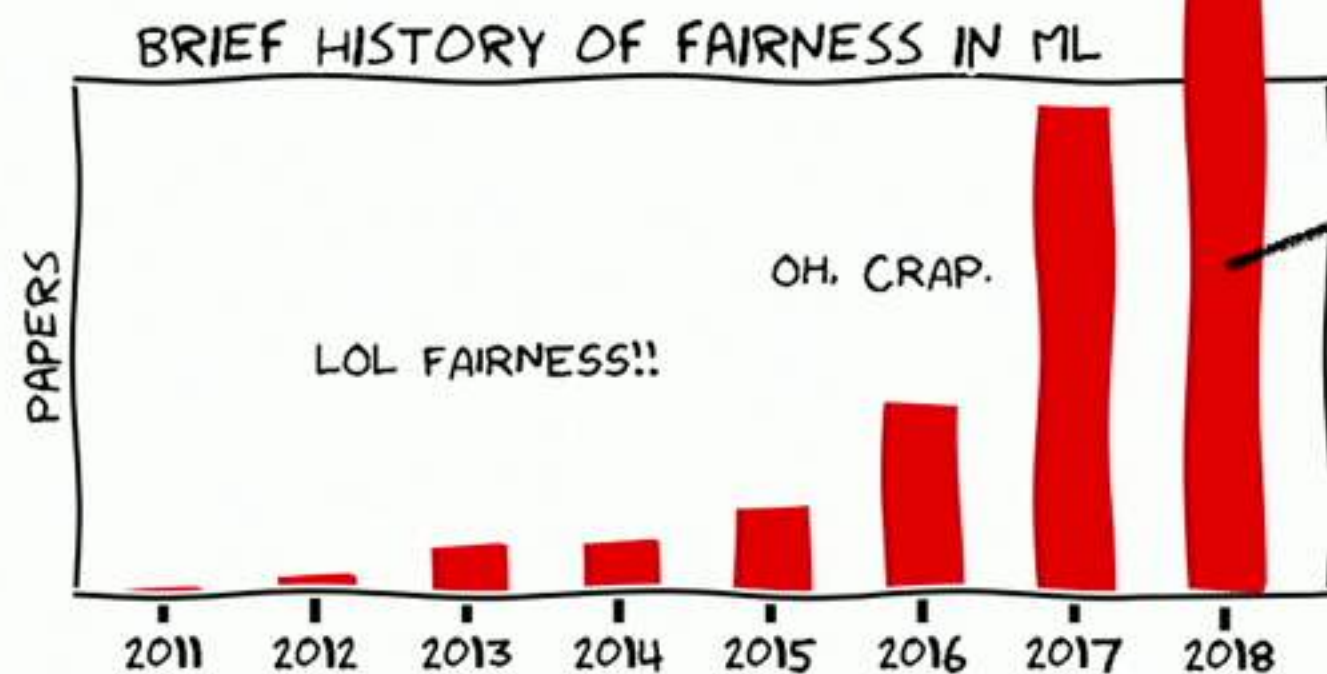


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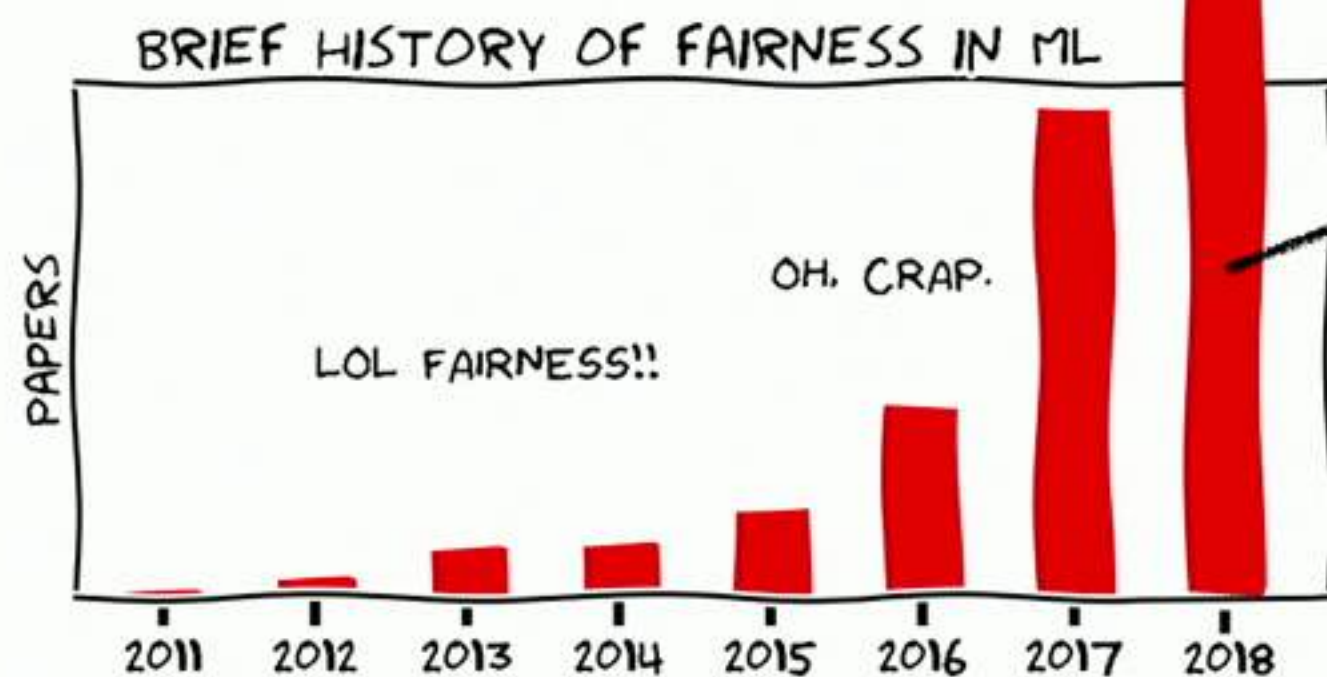


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- **But typically impossible to satisfy simultaneously**
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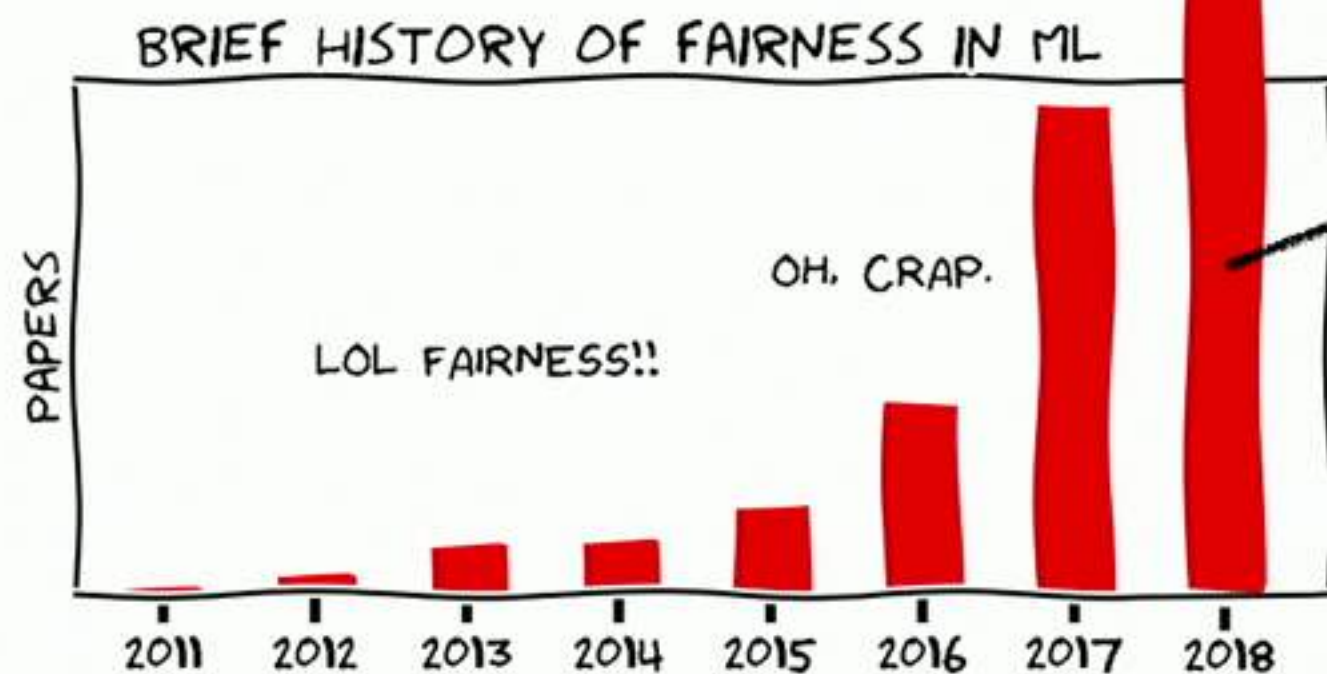


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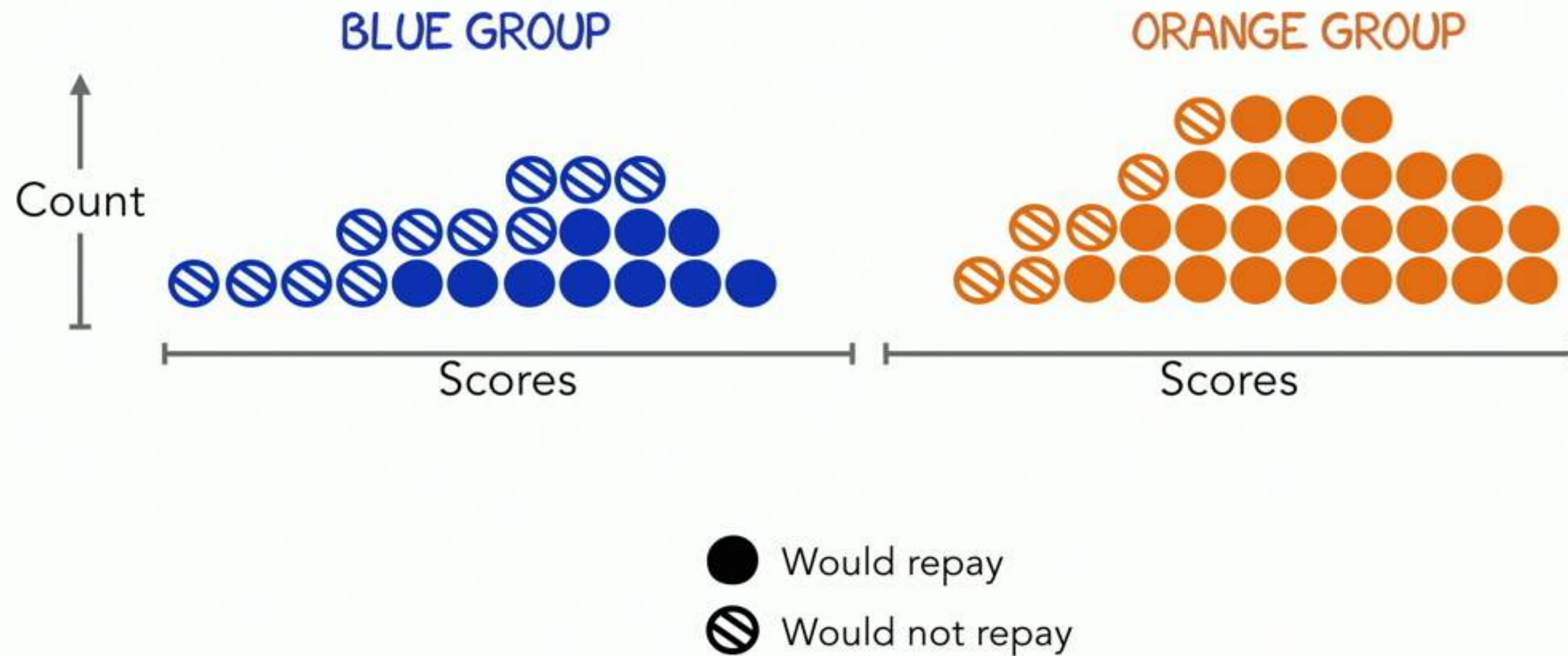
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Machine learning
systems are “fair”

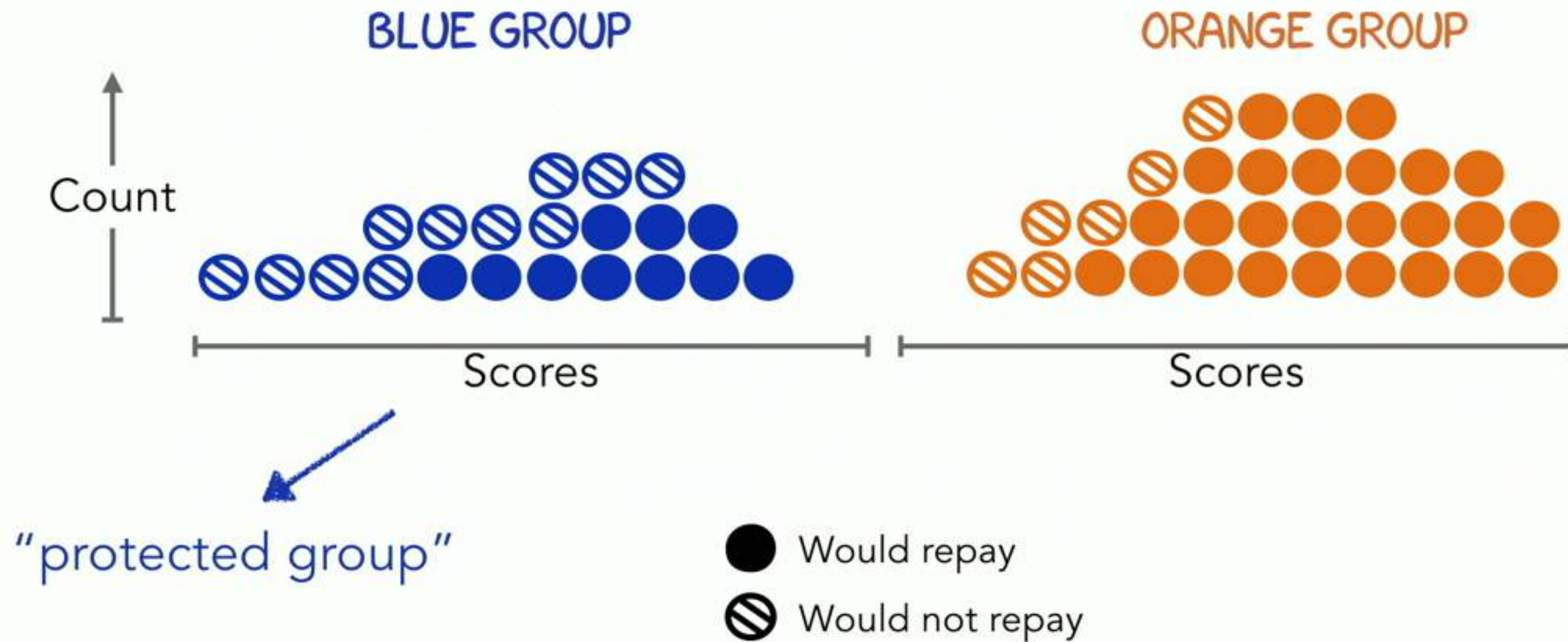


Protected groups
are “better off”

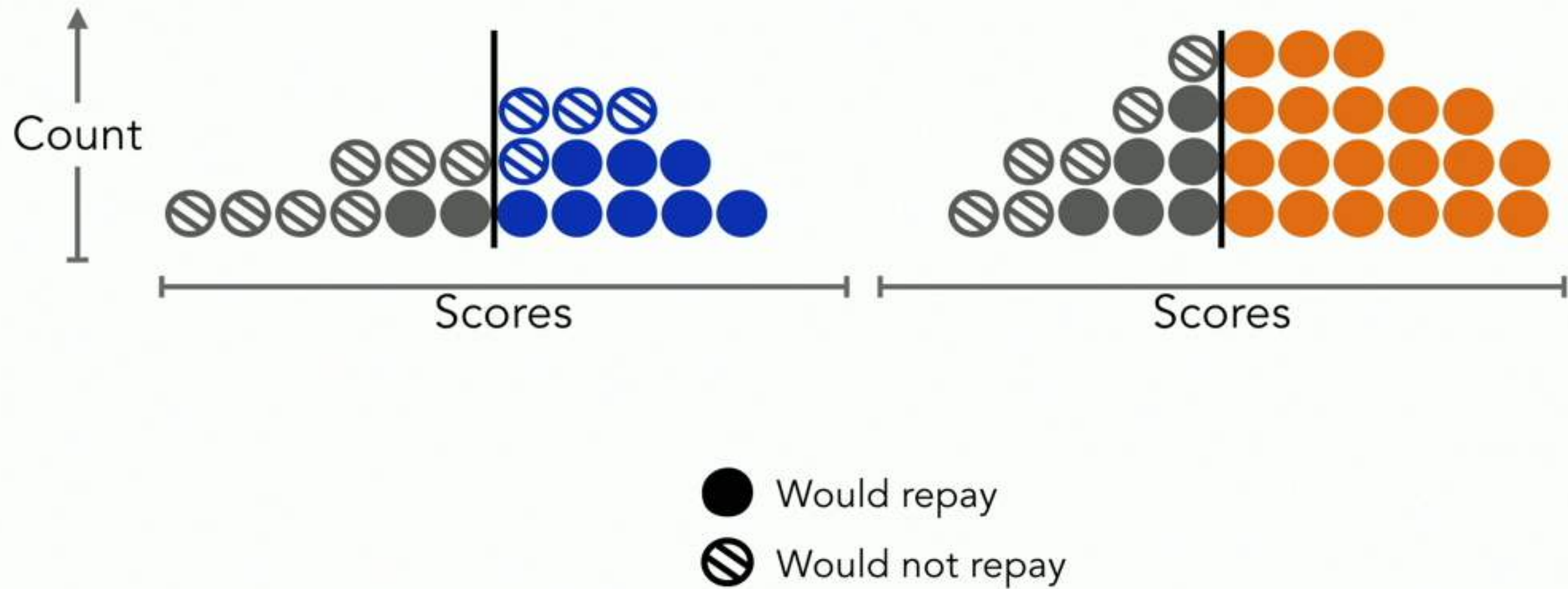
Two groups with different score distributions (e.g. credit scores)



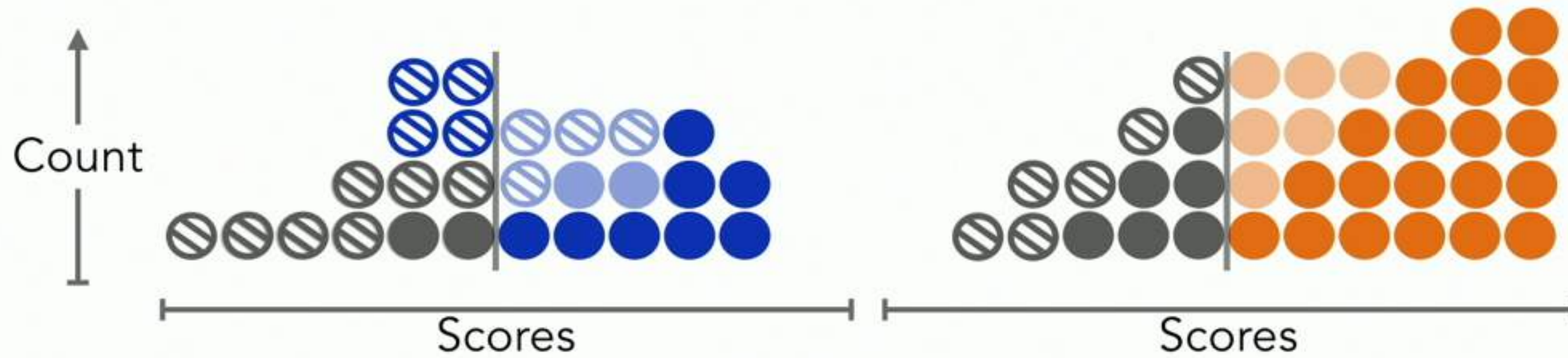
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Approve loans according to **DEMOGRAPHIC PARITY**.

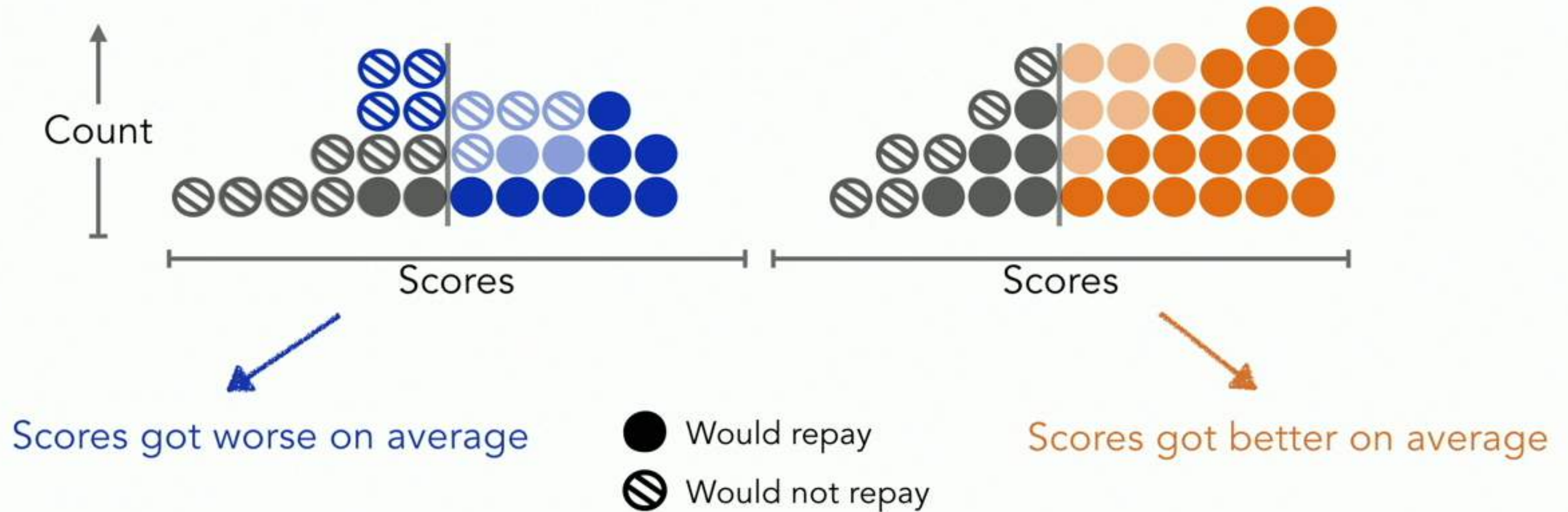


Credit scores change with repayment (+) or default (-).



- Would repay
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WHAT HAPPENED?

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Fairness criteria didn't seem to *help* the protected group,
once we considered the *impact* of loans on scores.

OUR WORK

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2. Provide a **complete characterization** of the delayed impact of 3 different fairness criteria
3. Show that fairness constraints **may cause harm** to groups they intended to protect

SCORE DISTRIBUTION WITHIN A GROUP

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- **Monotonicity assumption**: Higher scores implies **more likely** to repay

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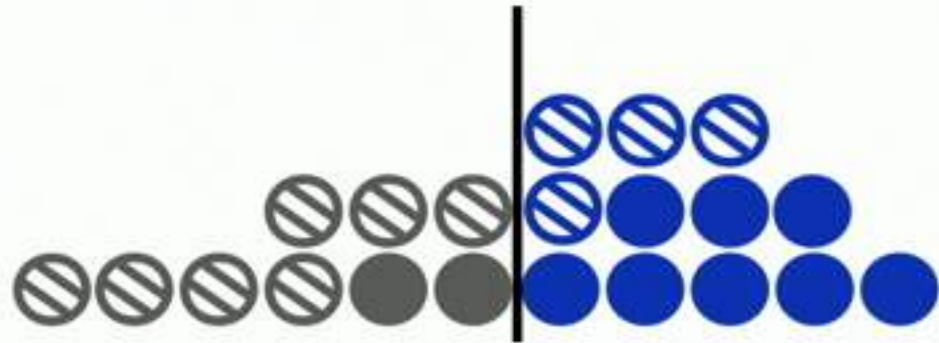
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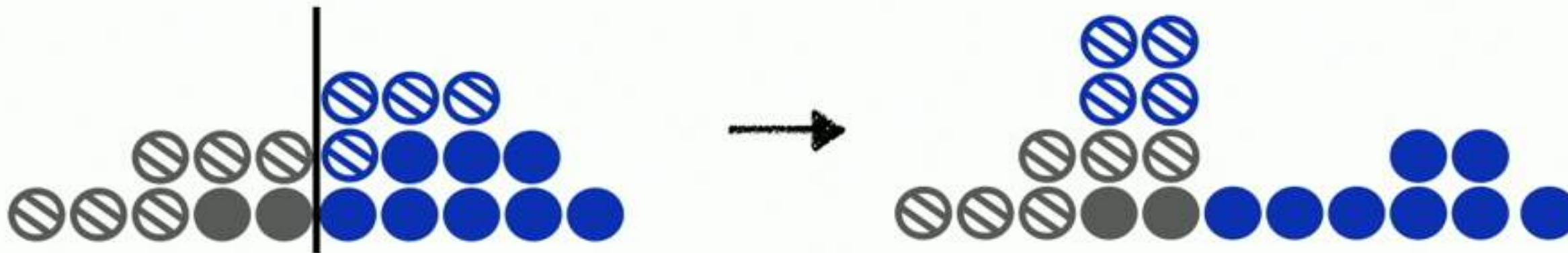
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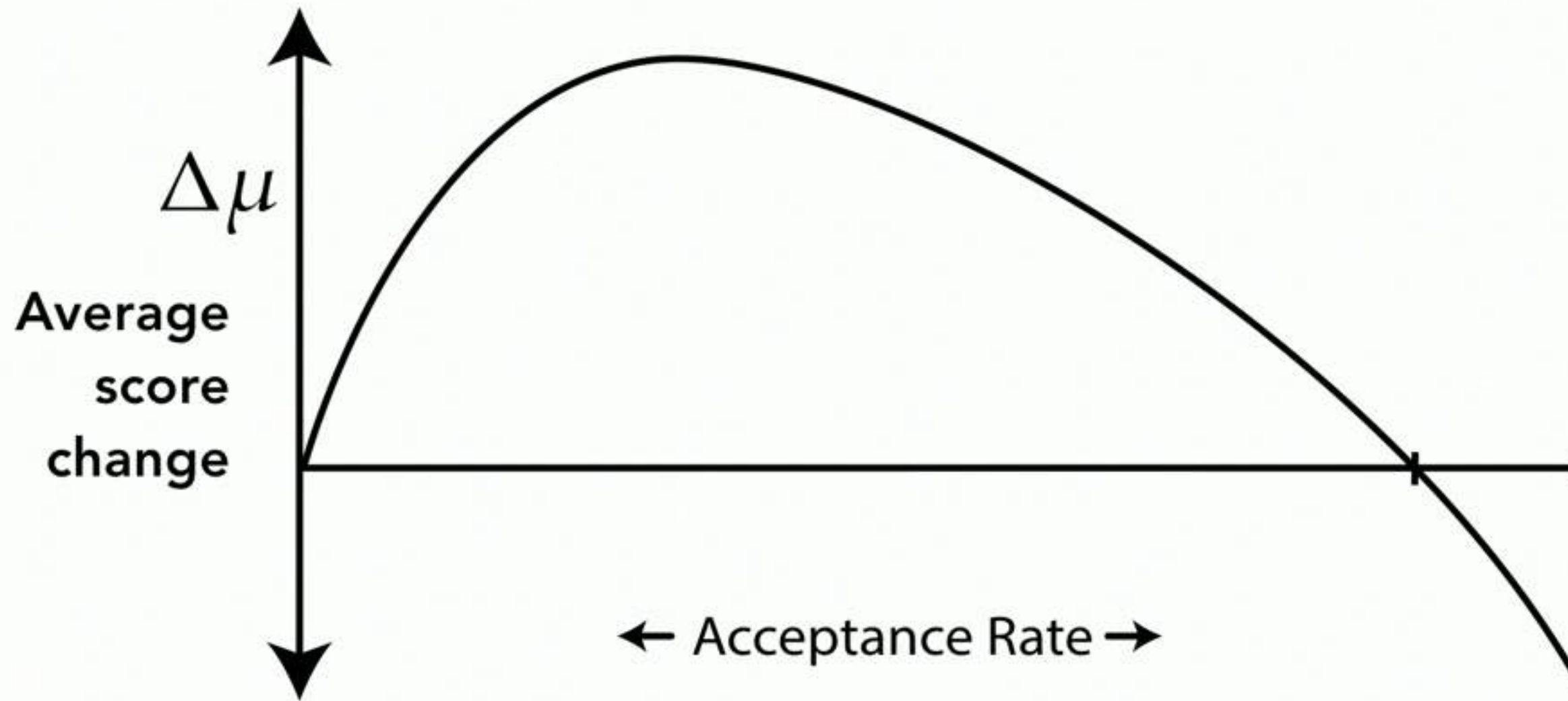
- The average change in score of each group is the **delayed impact**:

$$\Delta\mu = \mathbb{E}[R_{\text{new}} - R_{\text{old}}]$$

OUTCOME CURVE

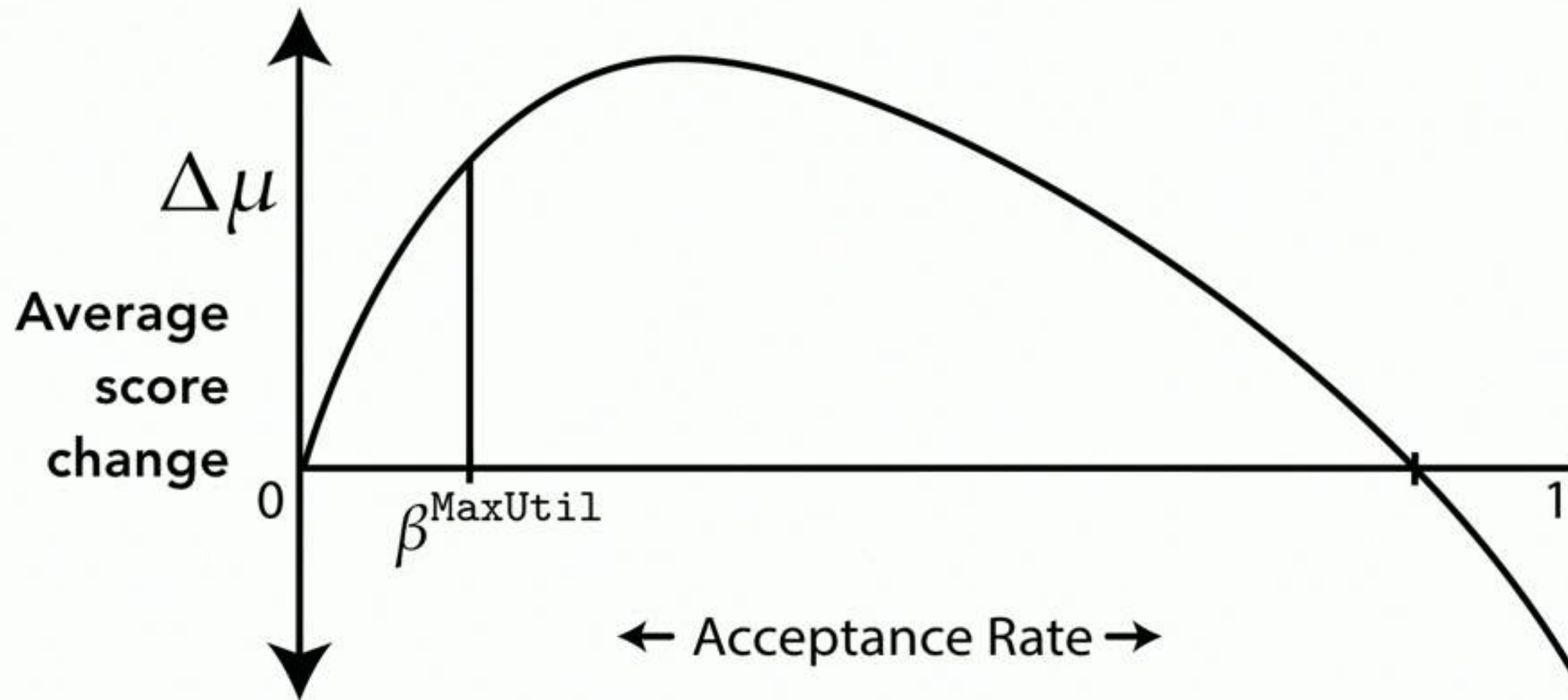
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Lemma: $\Delta\mu$ is a **concave** function of acceptance rate β under mild assumptions.



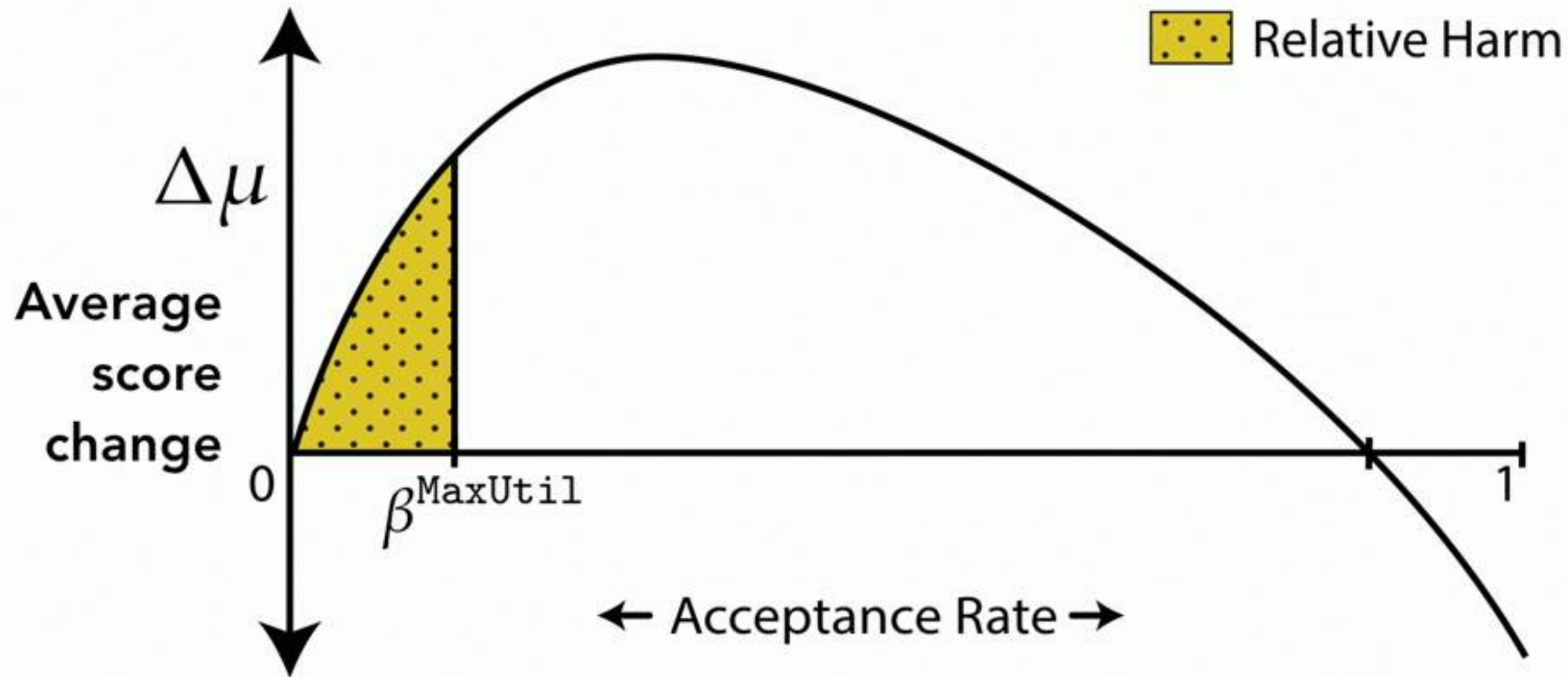
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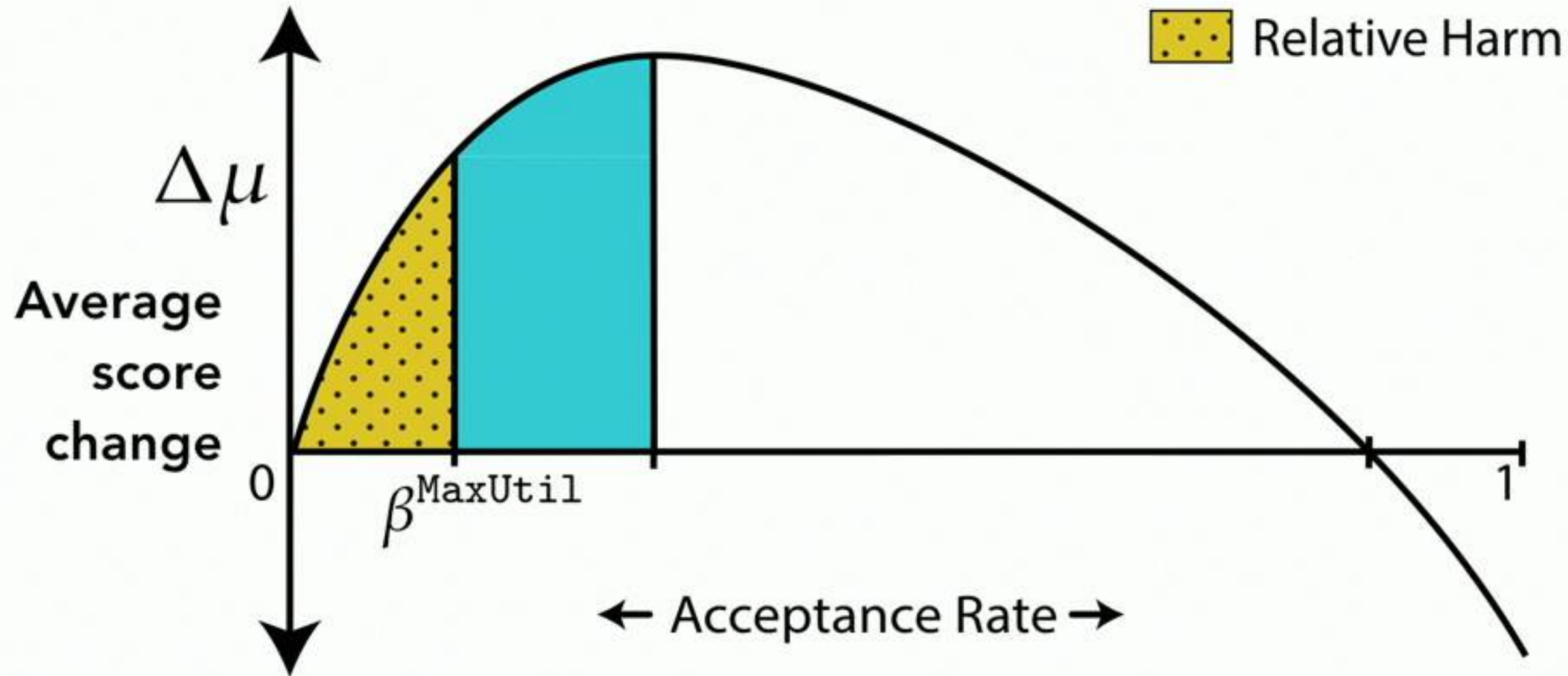
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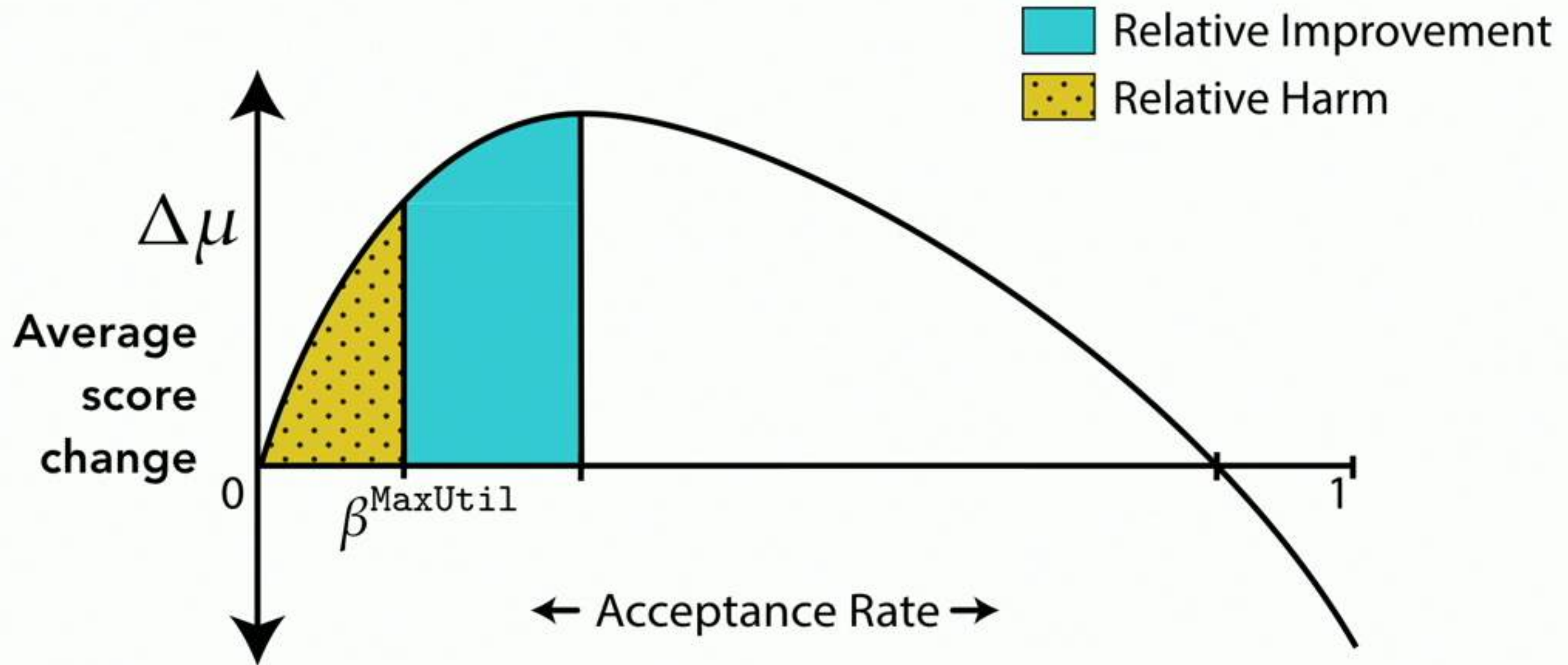
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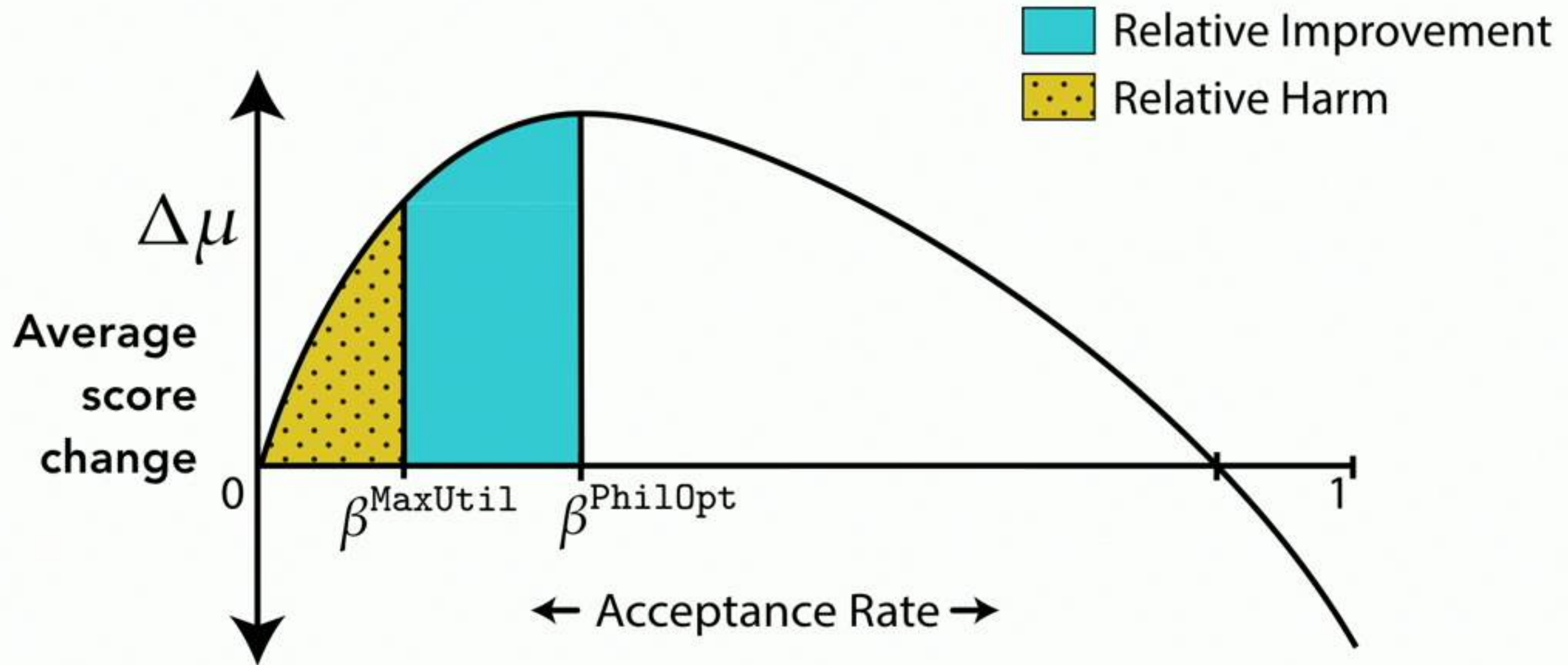
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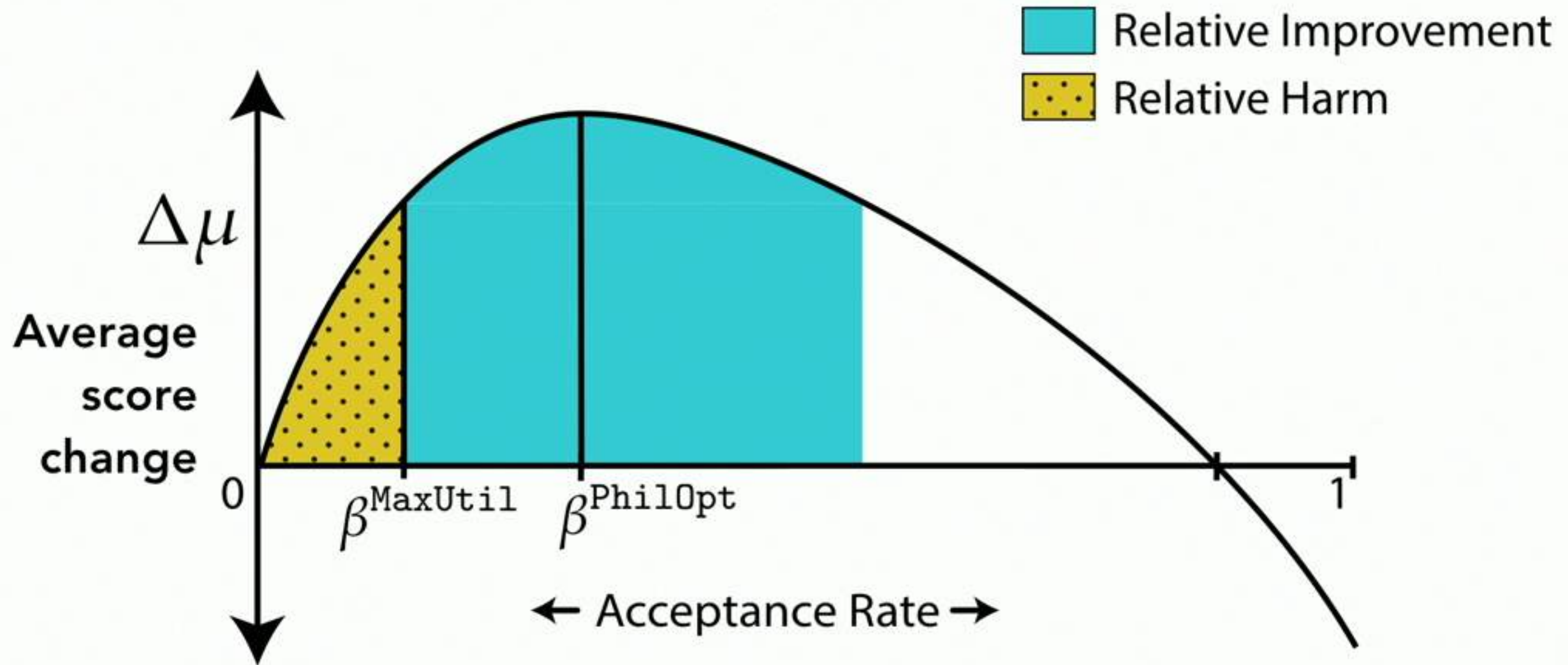
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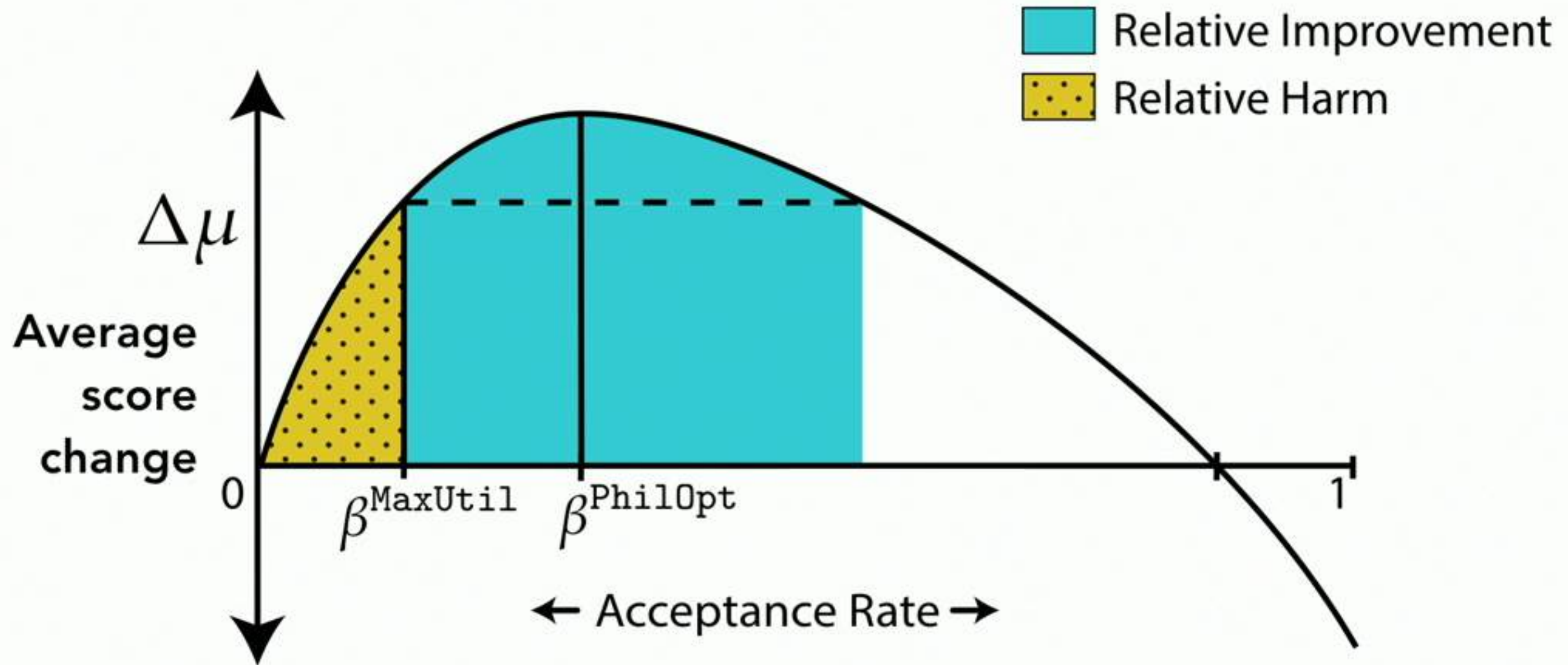
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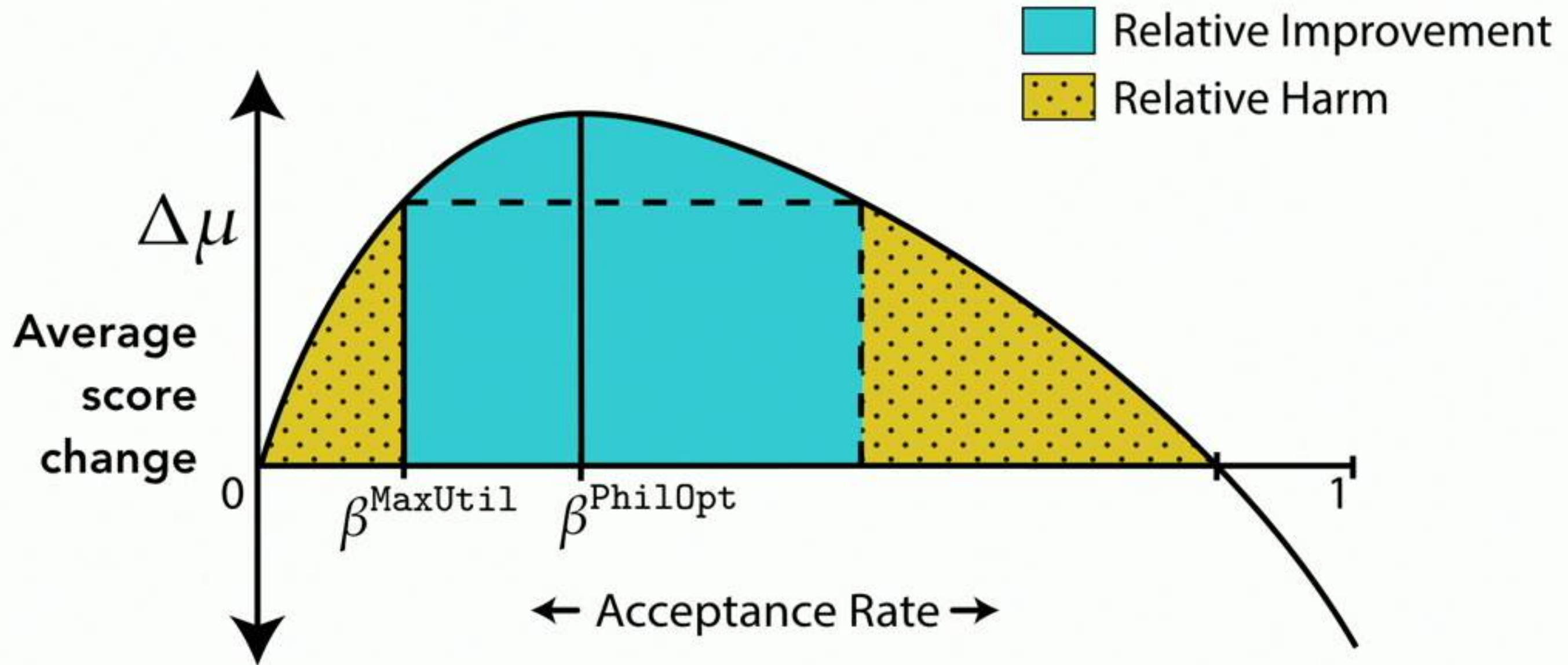
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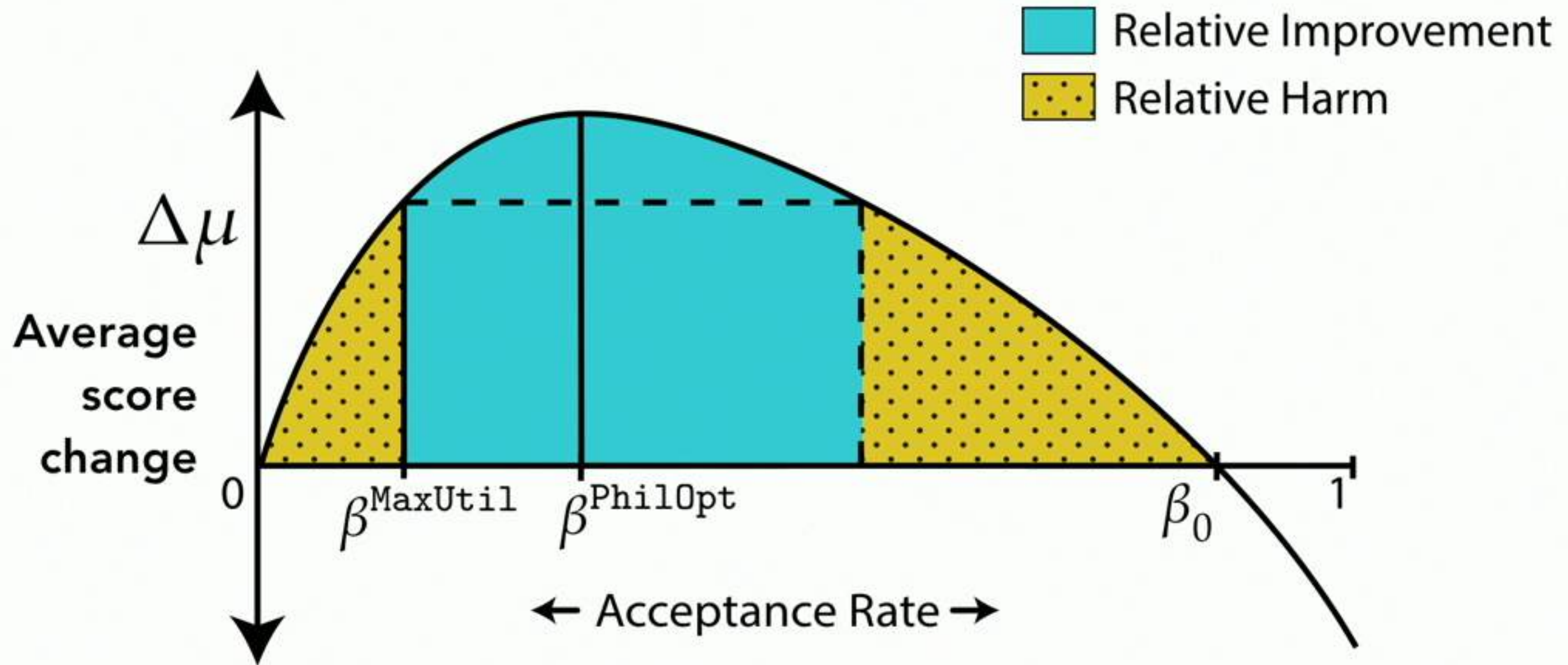
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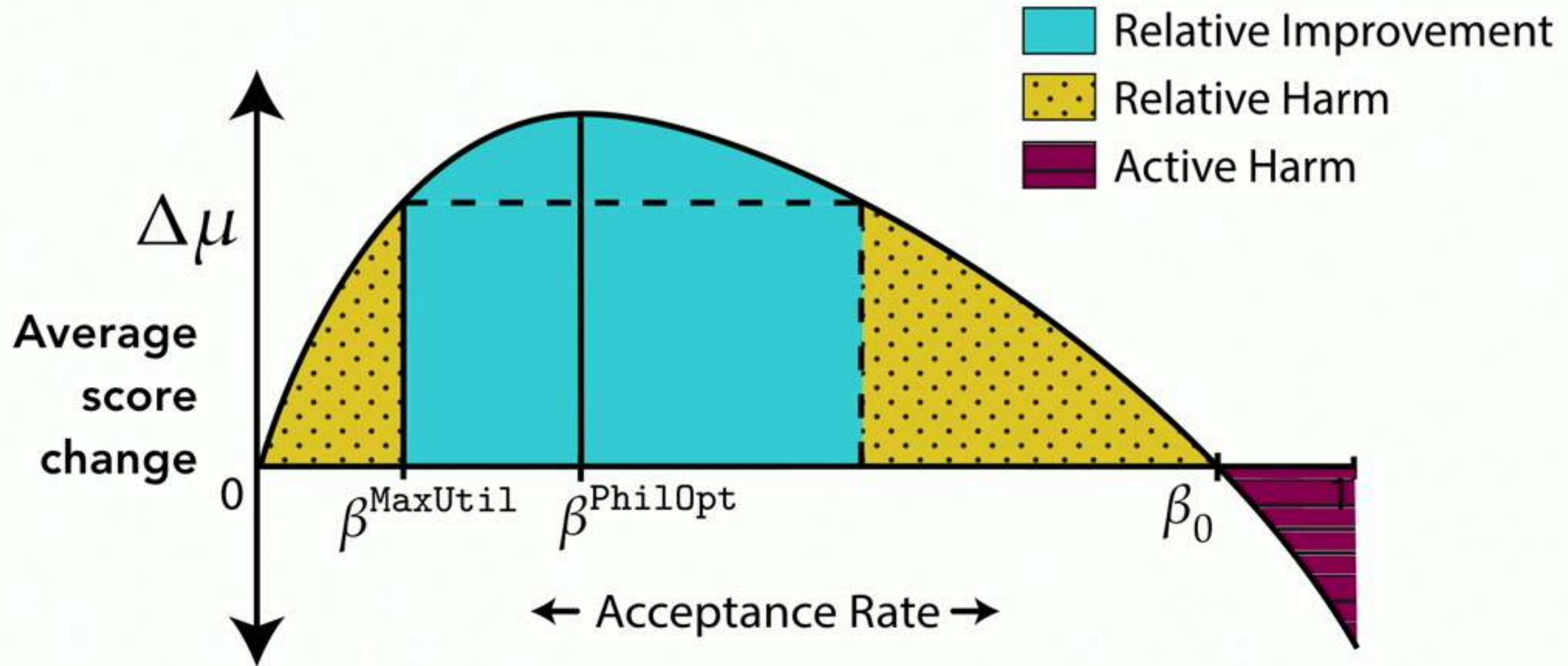
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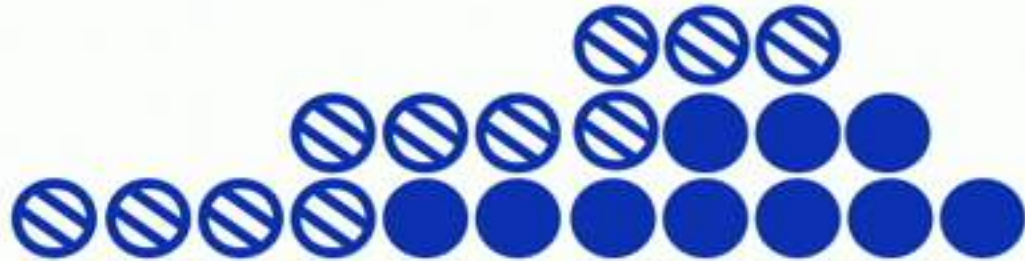
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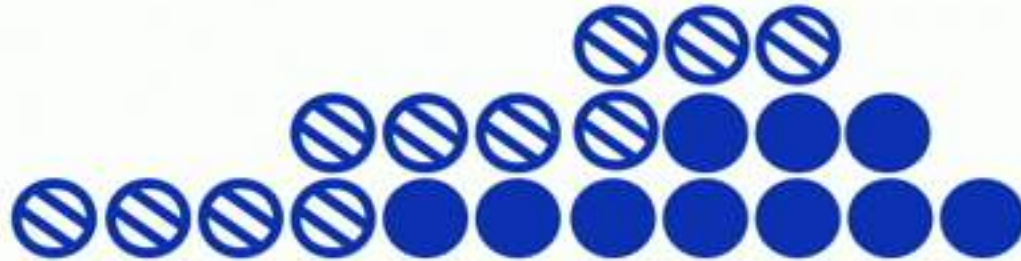
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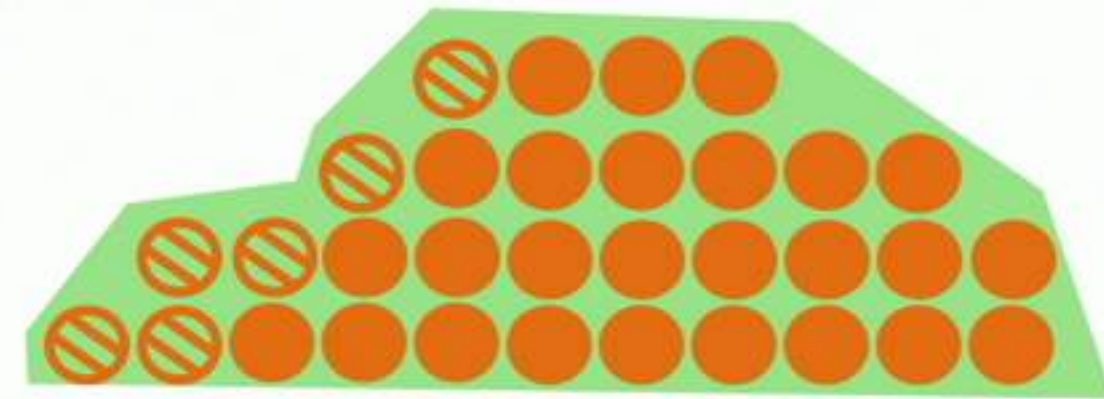
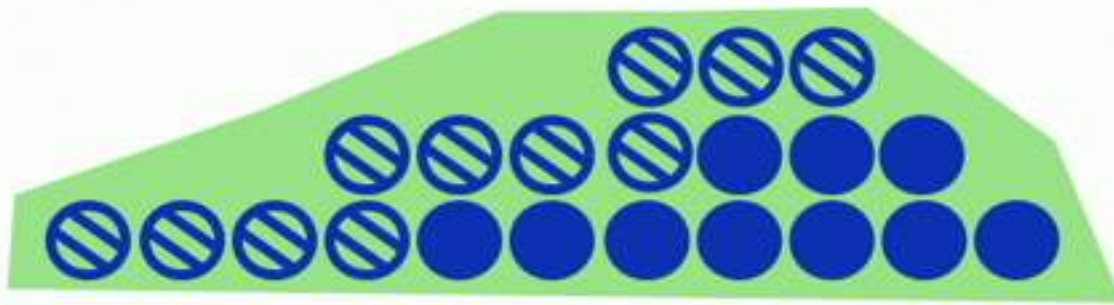
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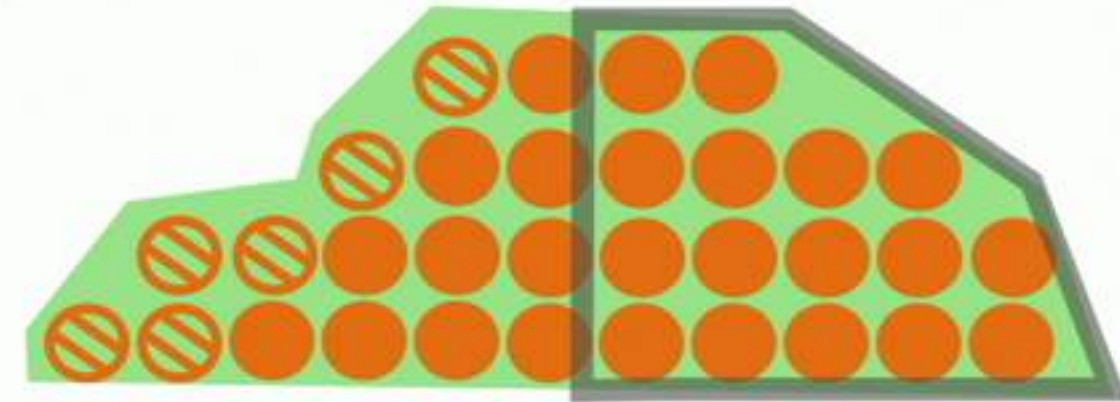
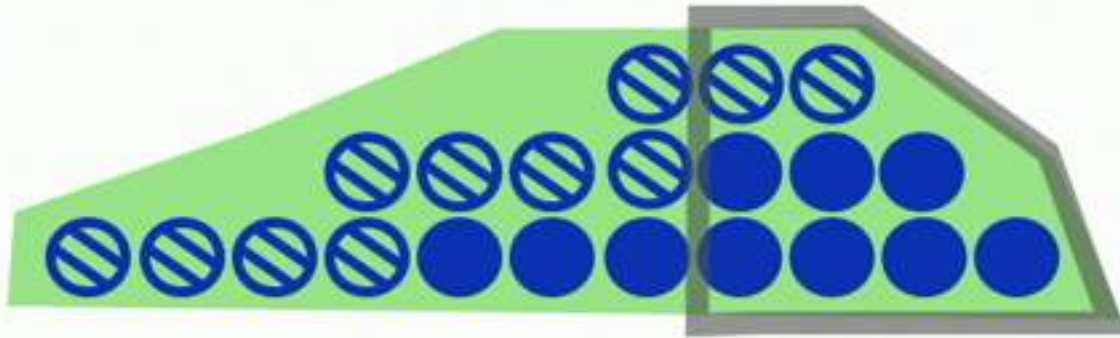
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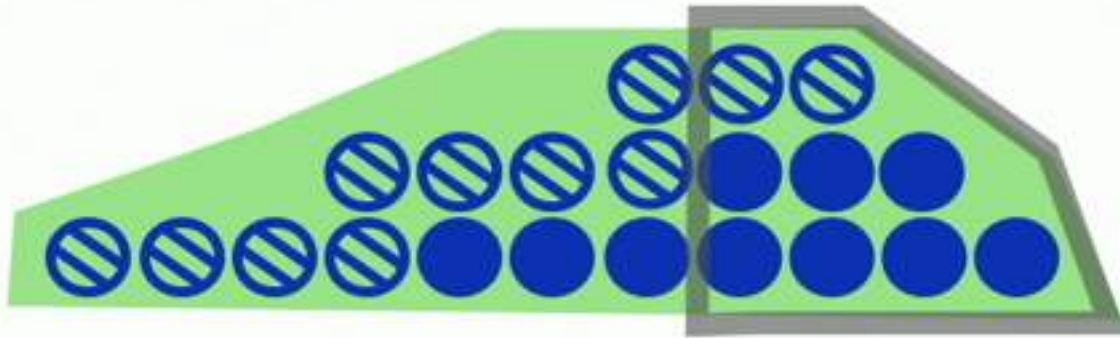
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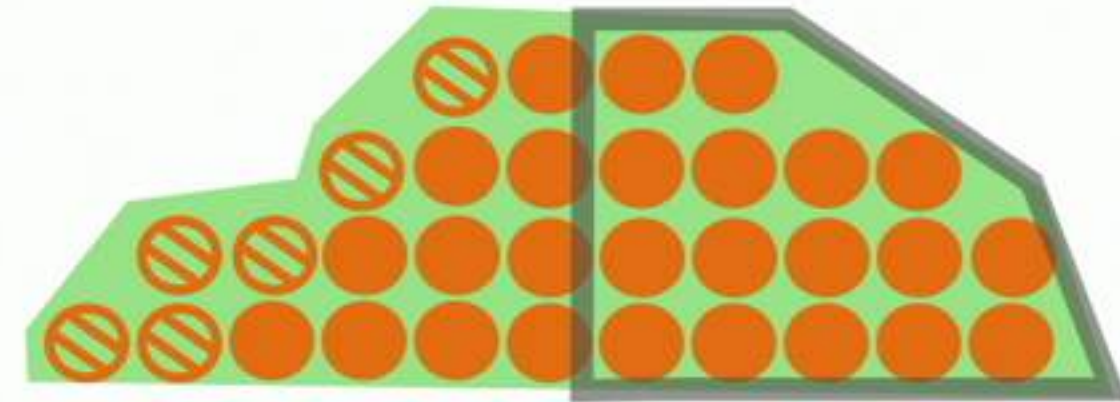


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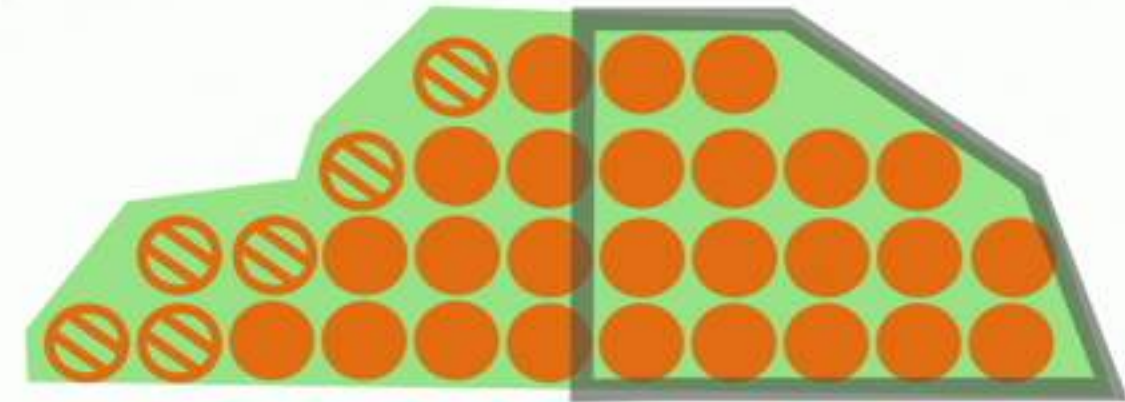
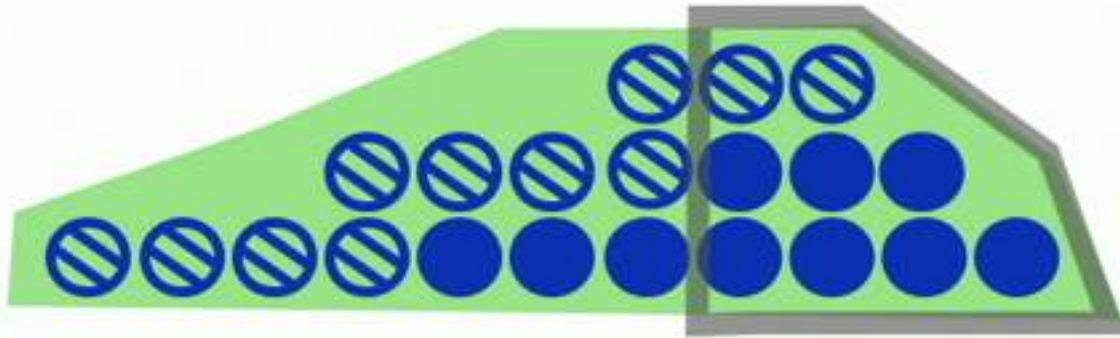


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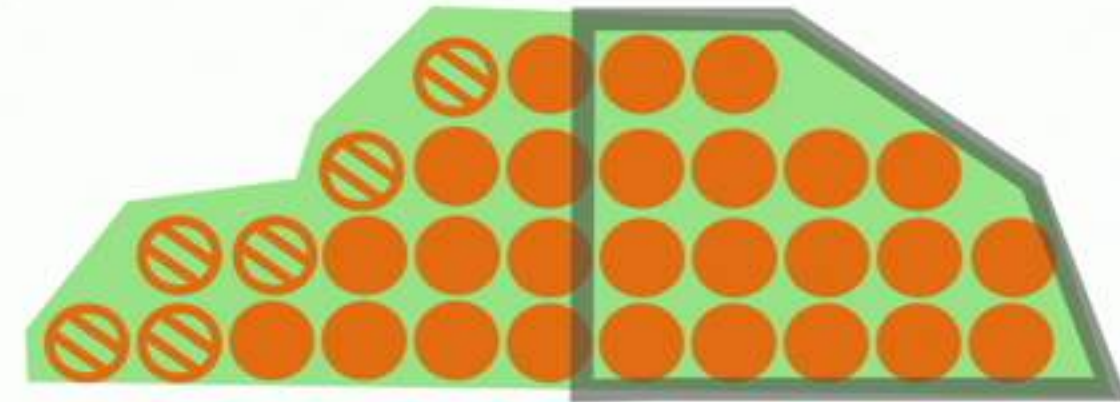
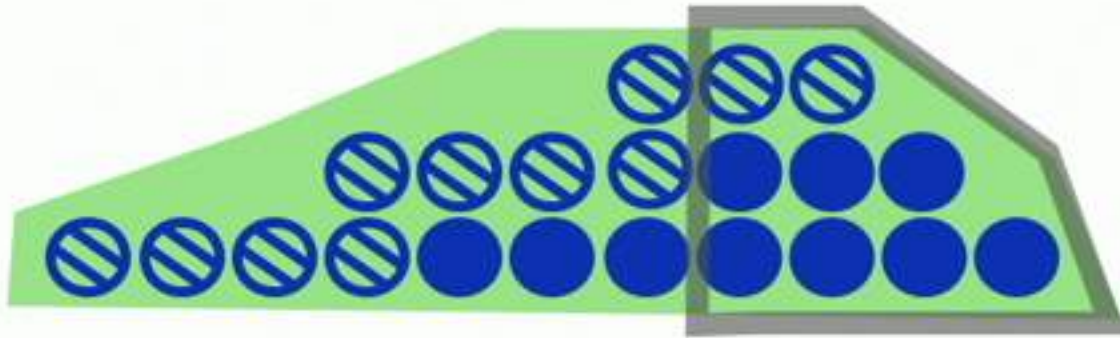
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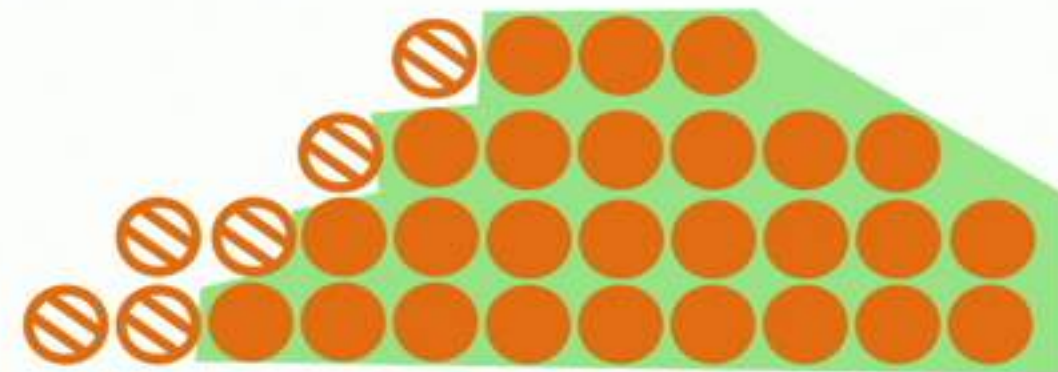
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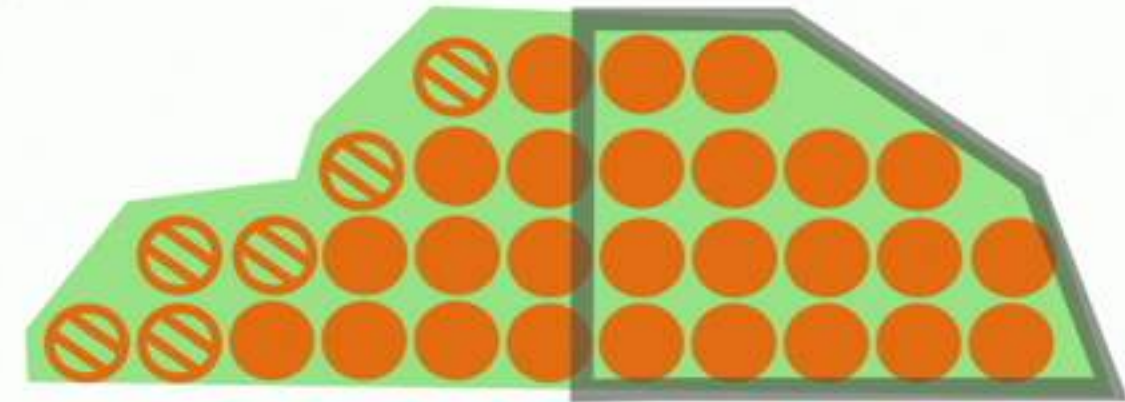
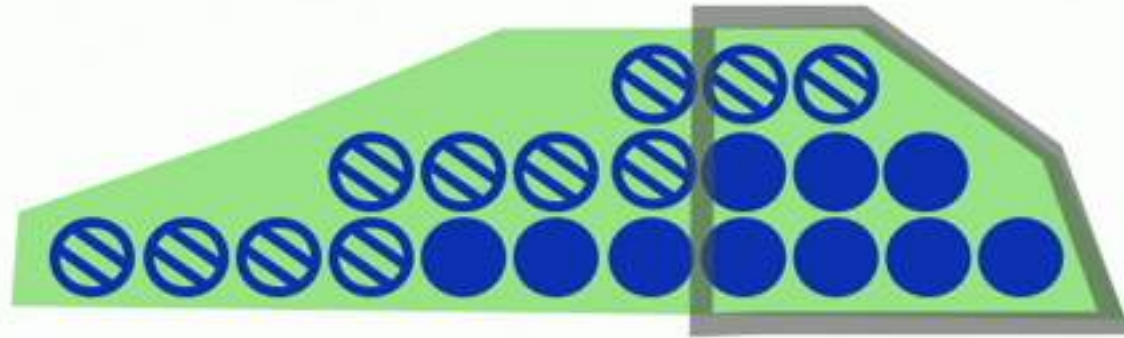
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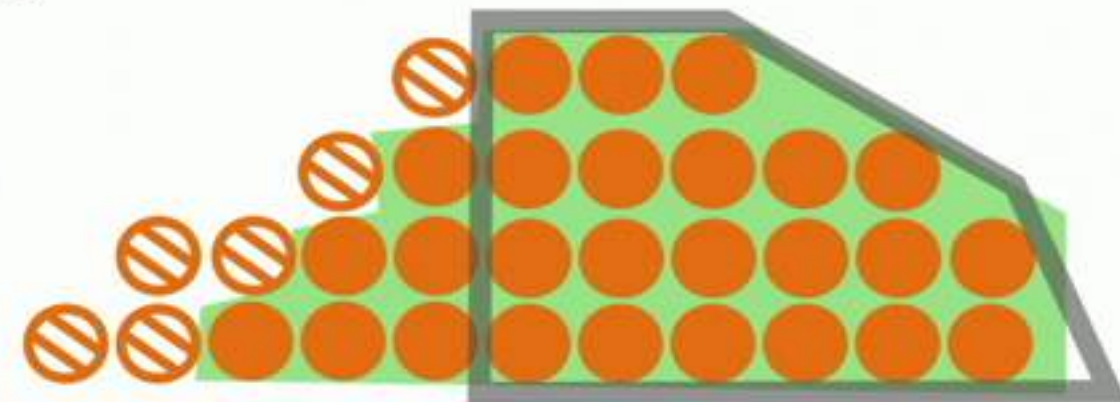
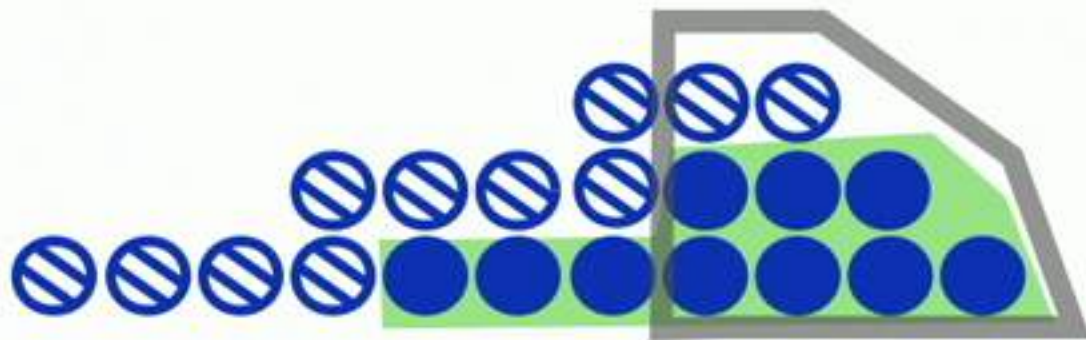
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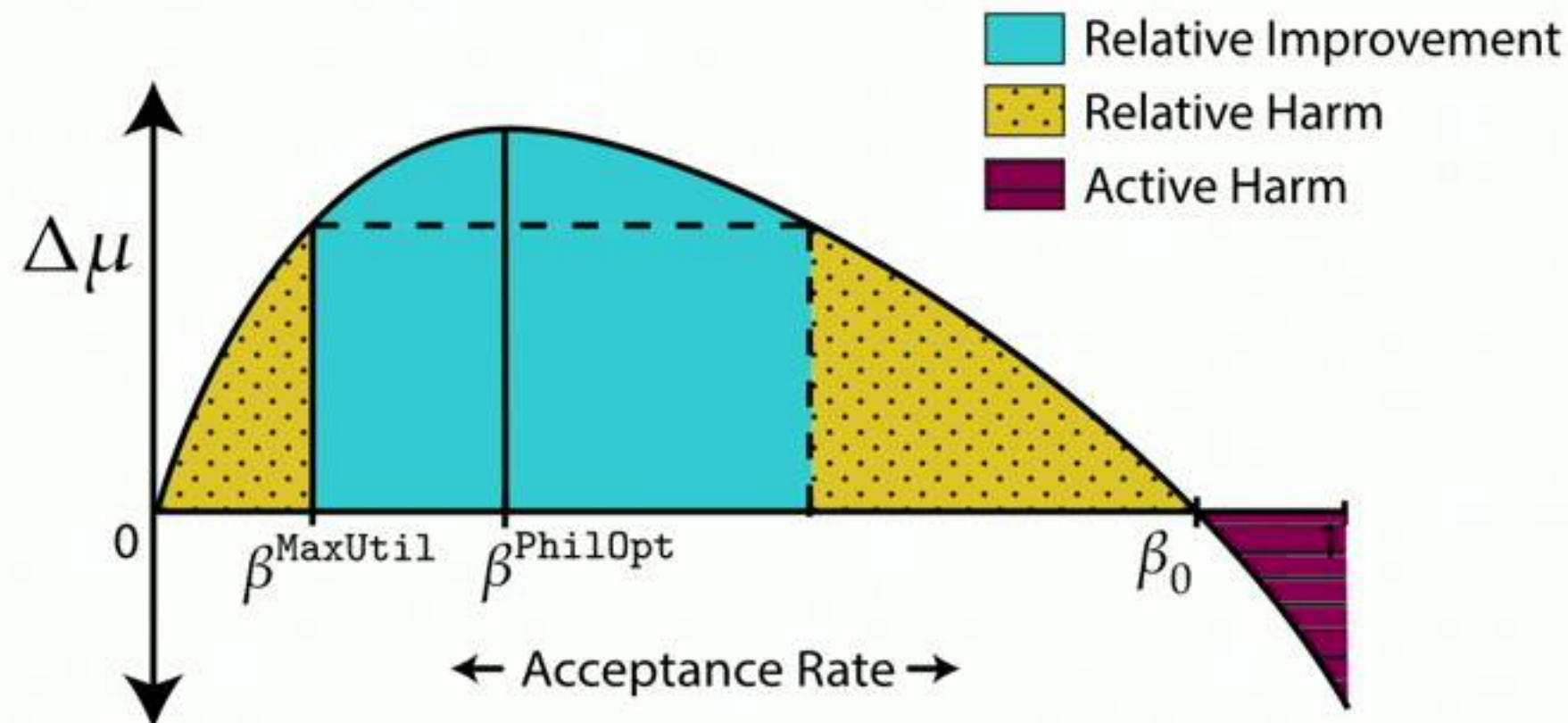
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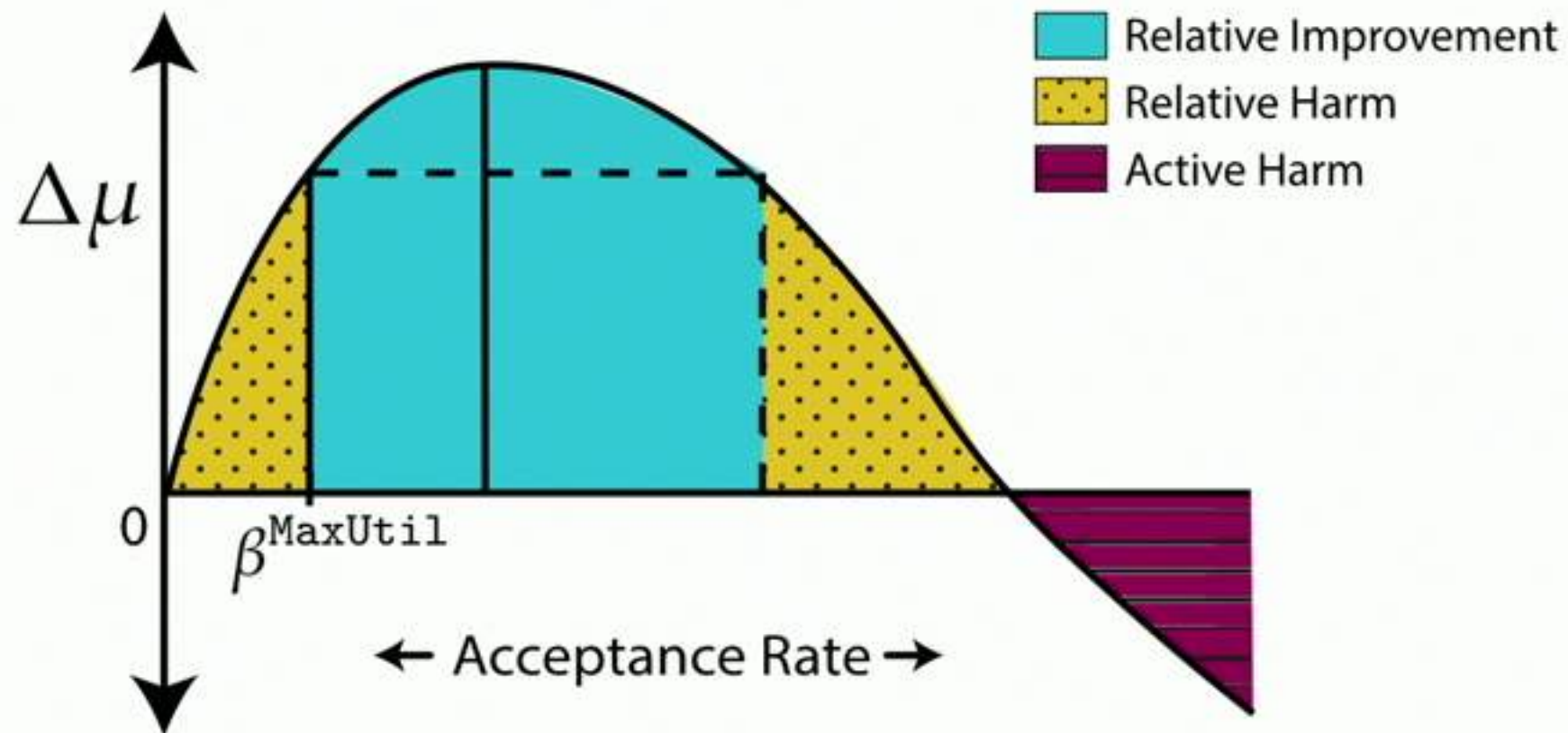
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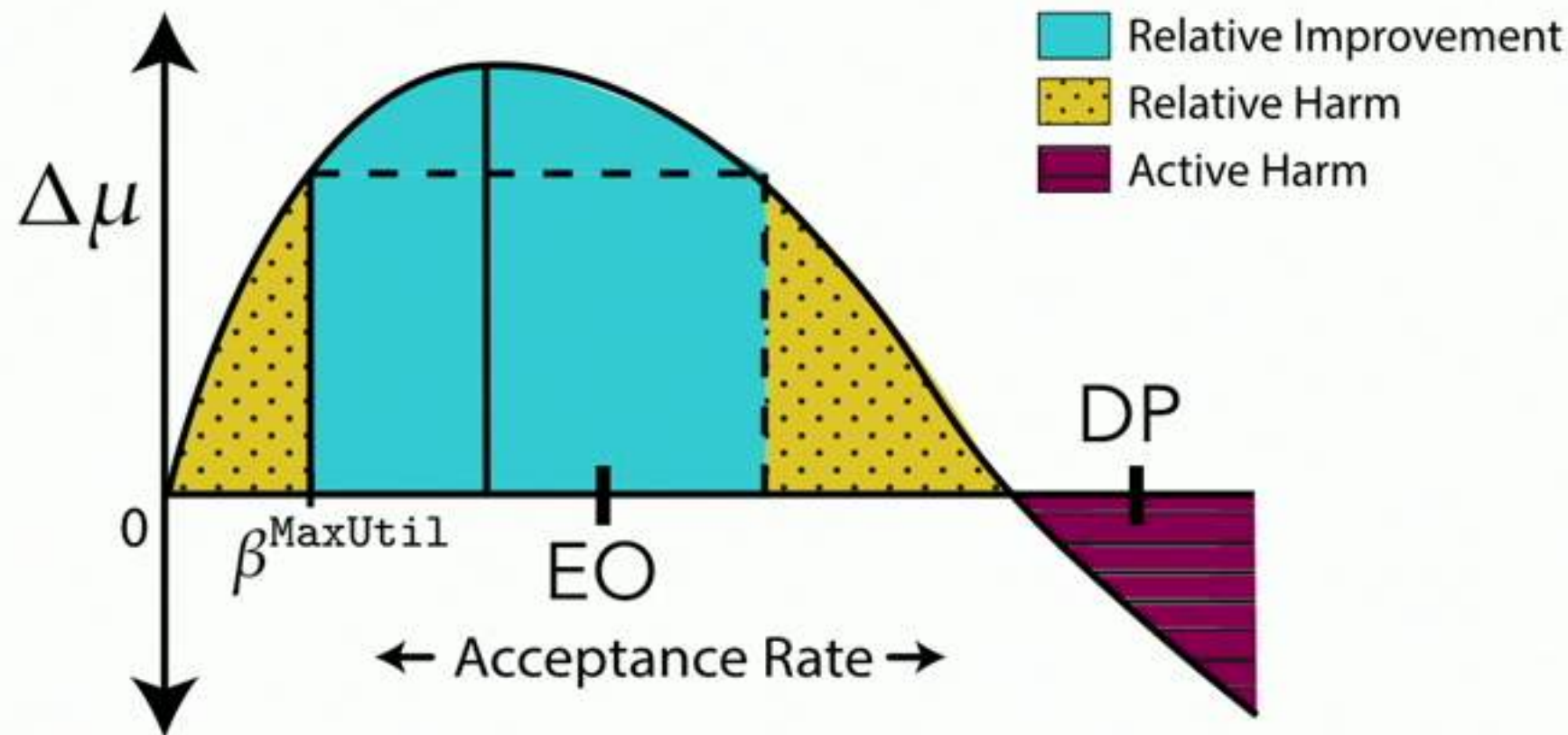
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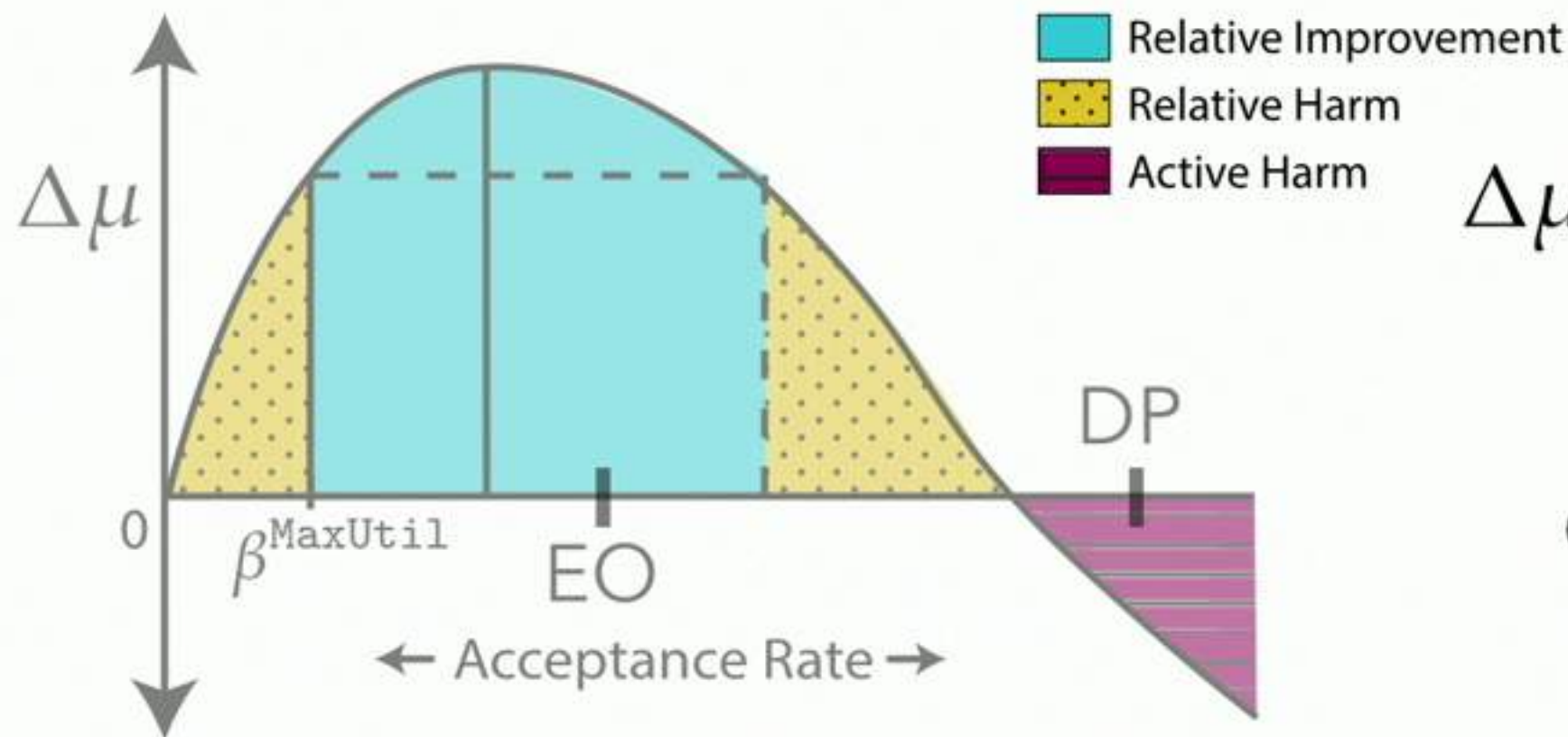


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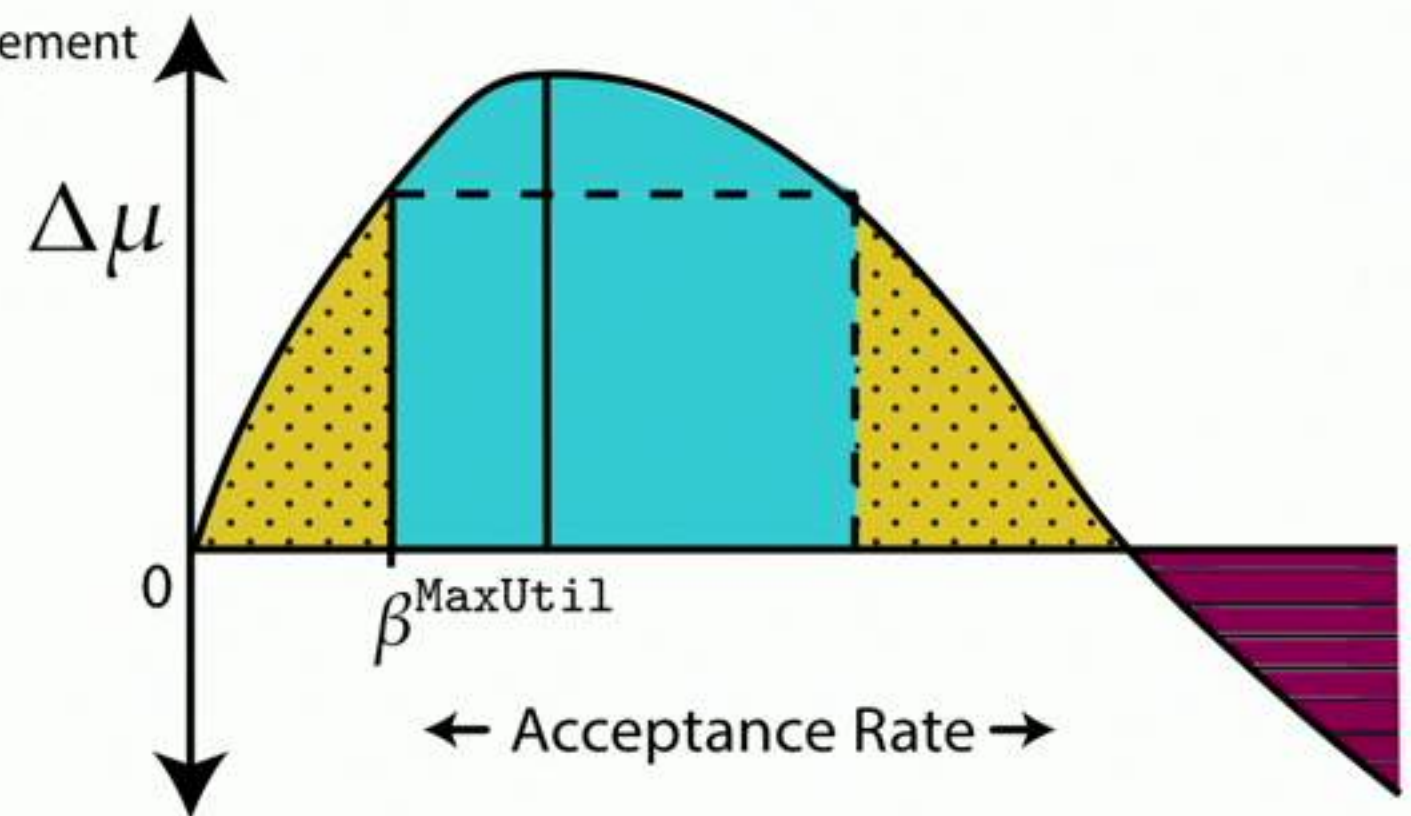
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- blue group
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- **0.8** probability of repaying loan
- assigned credit score of **700**



- blue group
- **0.8** probability of repaying loan
- but assigned credit score of **600** (*underestimated*)

“MEASUREMENT ERROR”

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- *Theorem:* **Acceptance rate for blue group is lower** if their scores are systematically underestimated than when their scores reflect true probability of repayment.

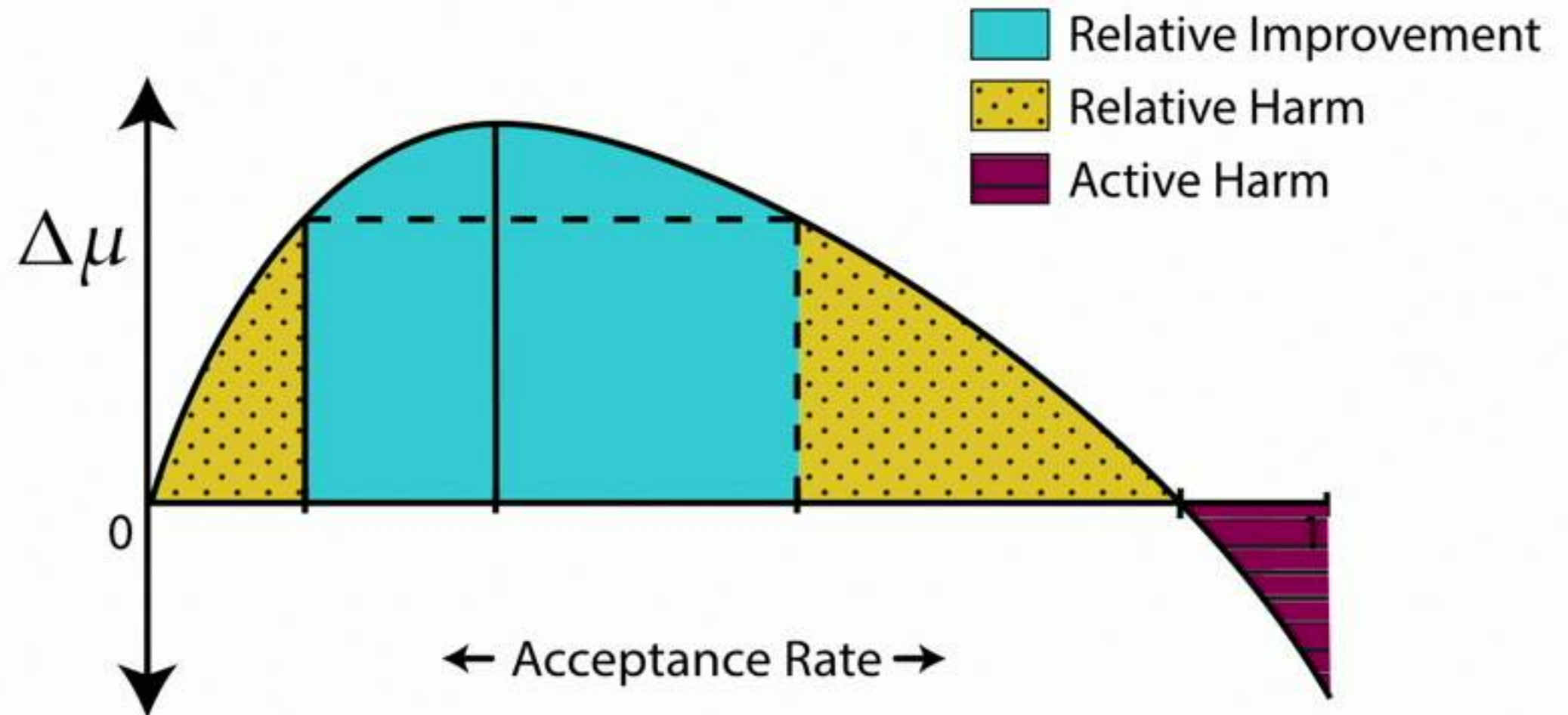
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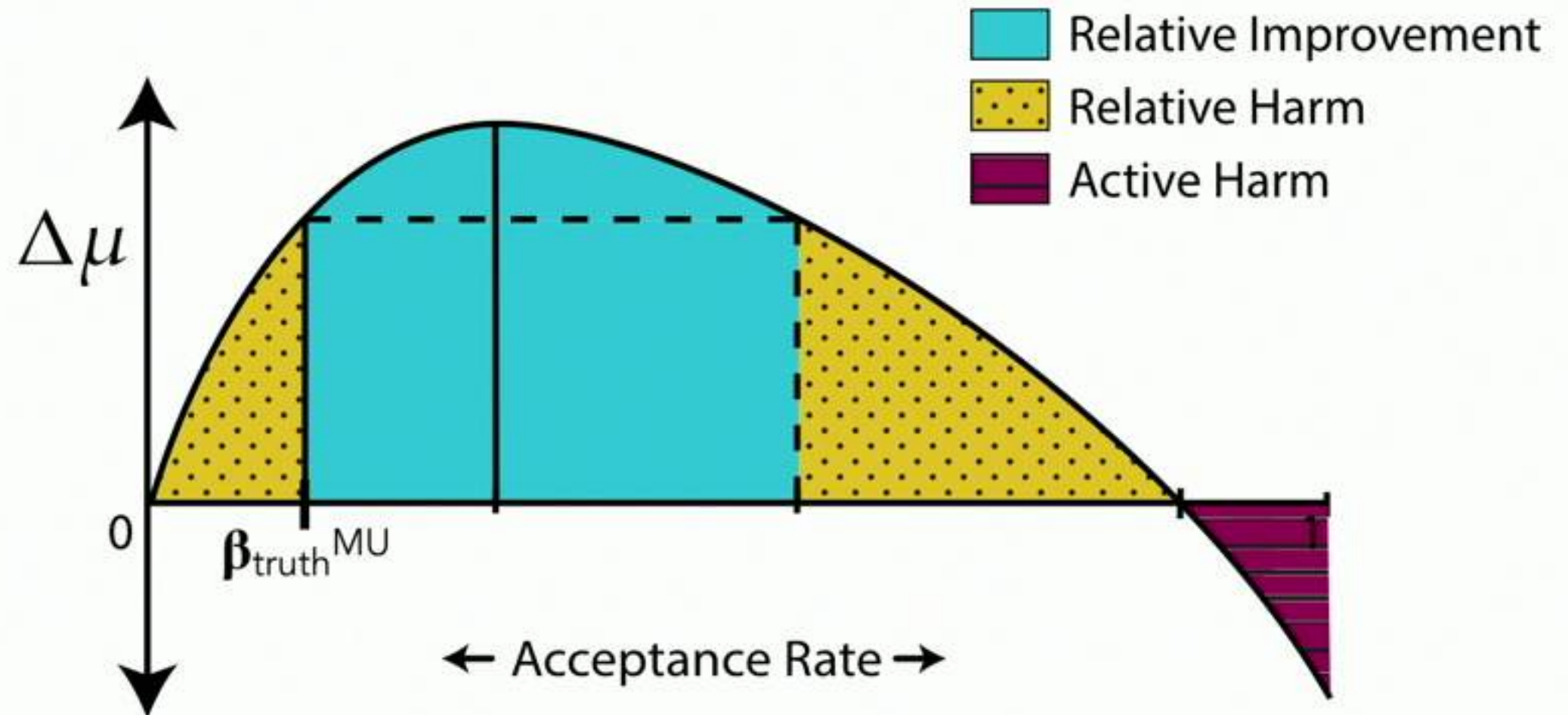
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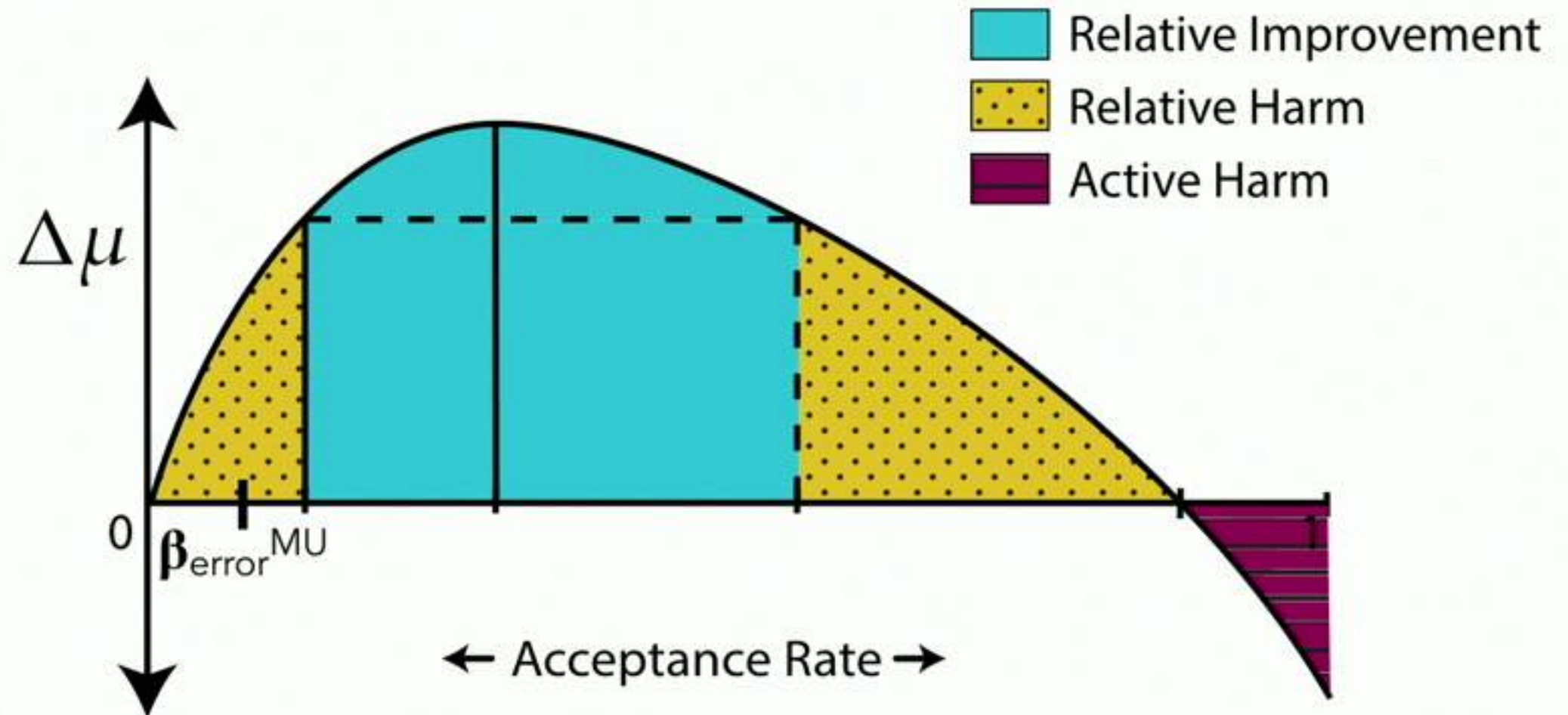
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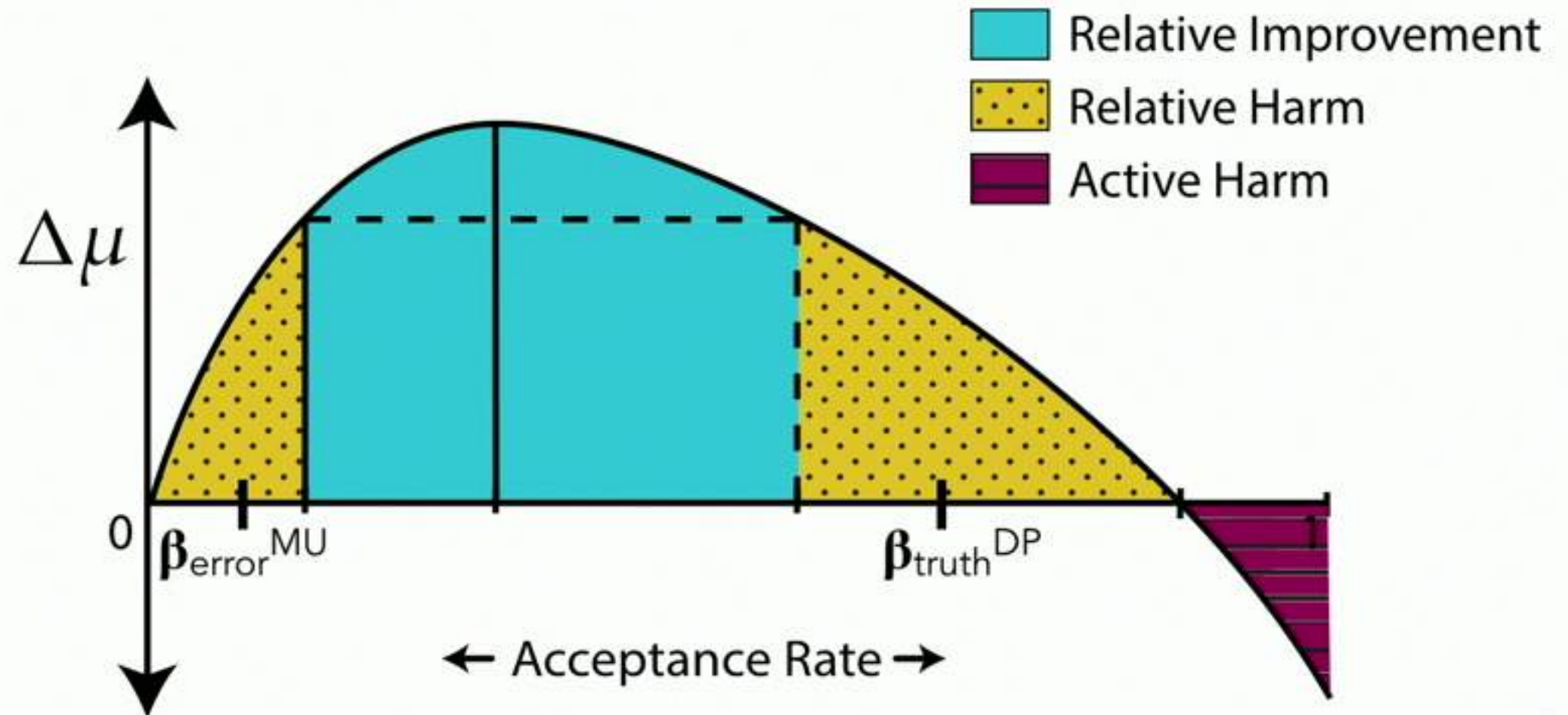
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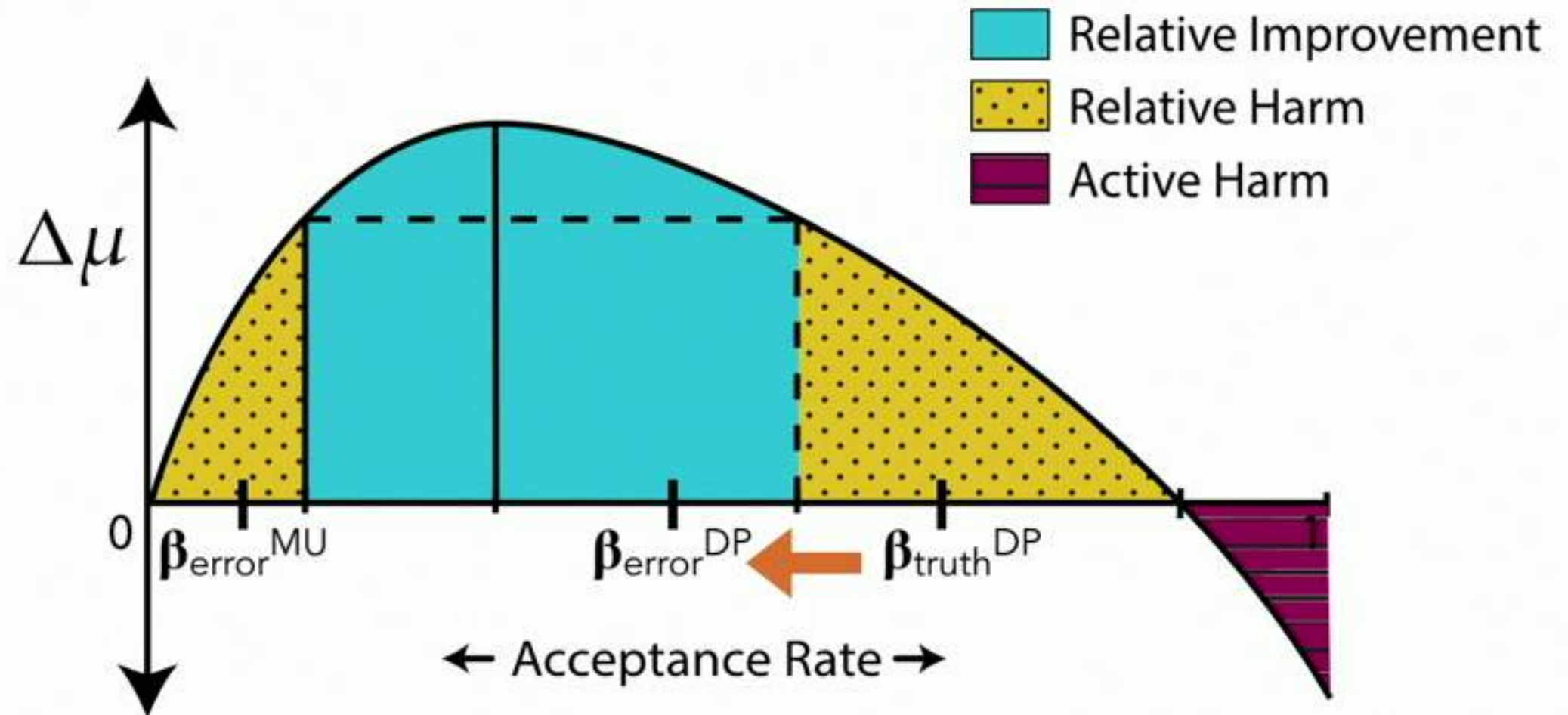
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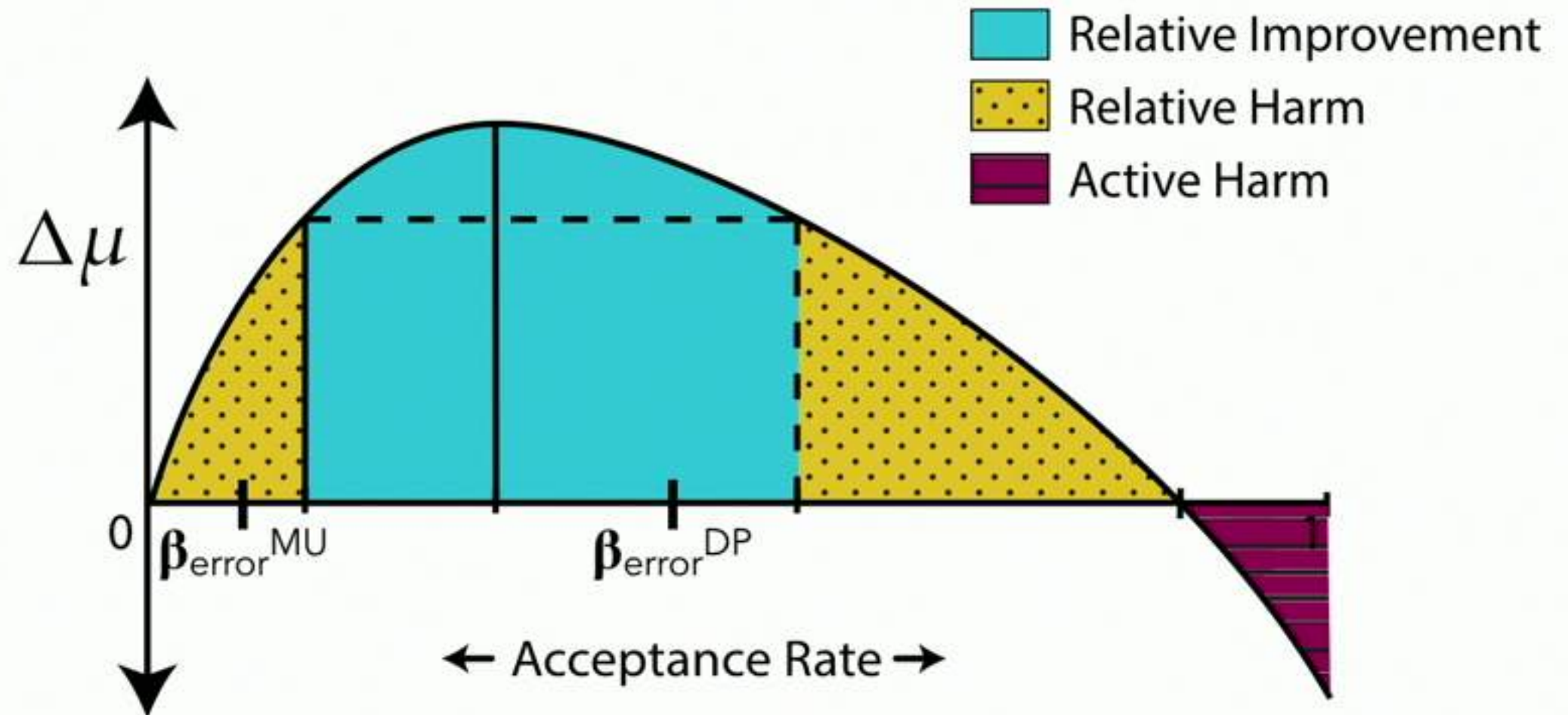
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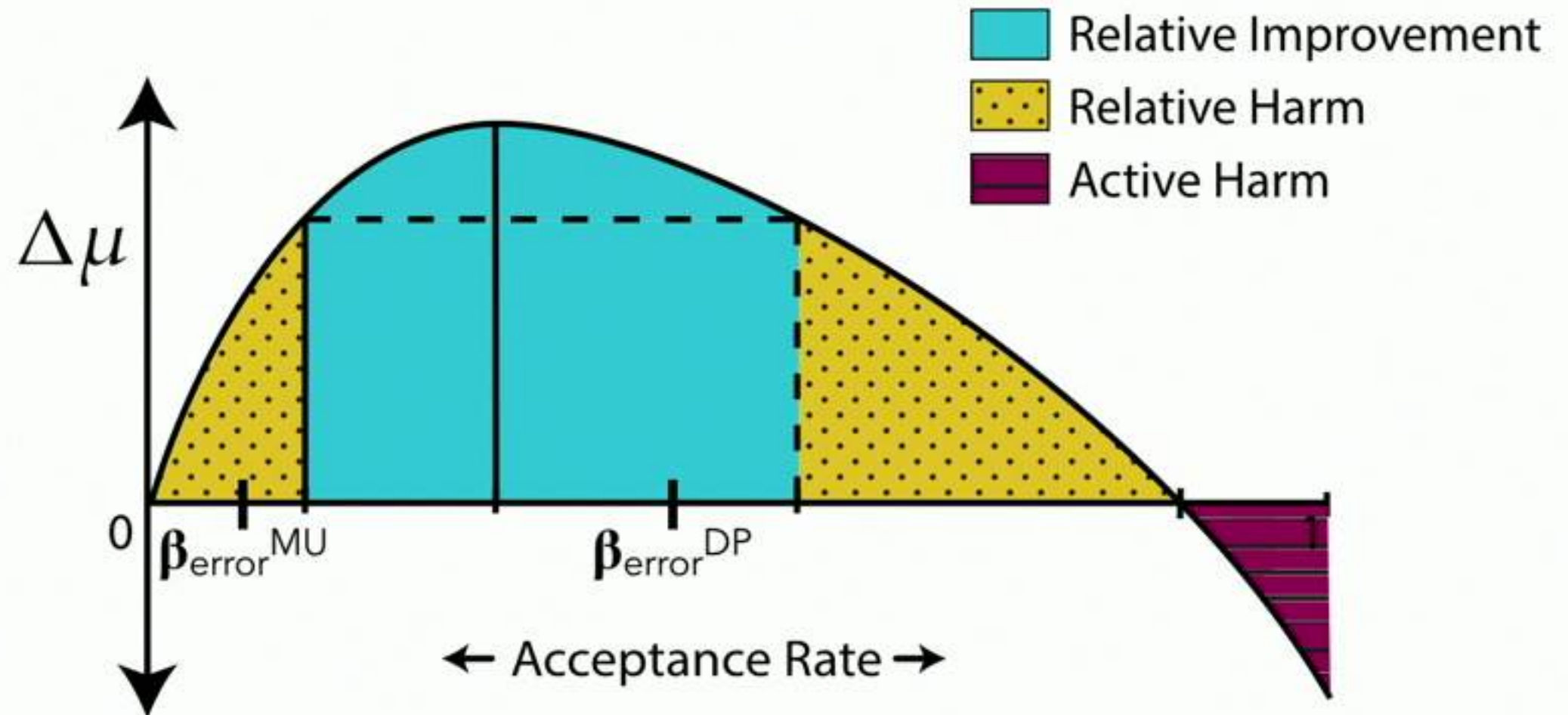
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- Example:
If there's measurement error, **demographic parity** yields more favorable delayed impact by promoting higher acceptance rate.



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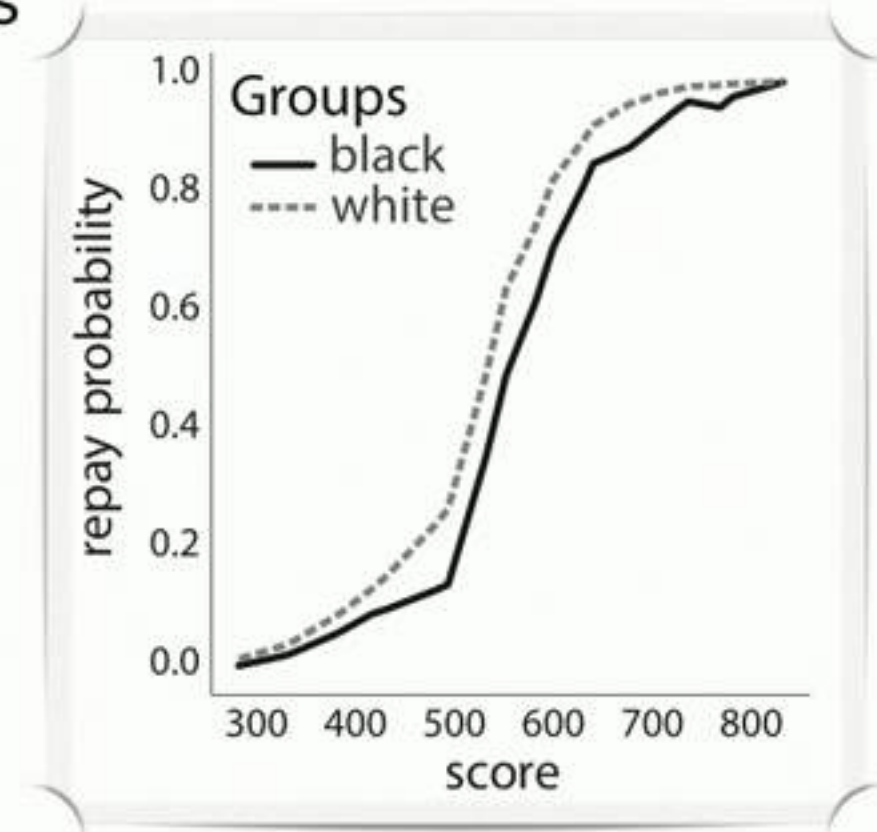
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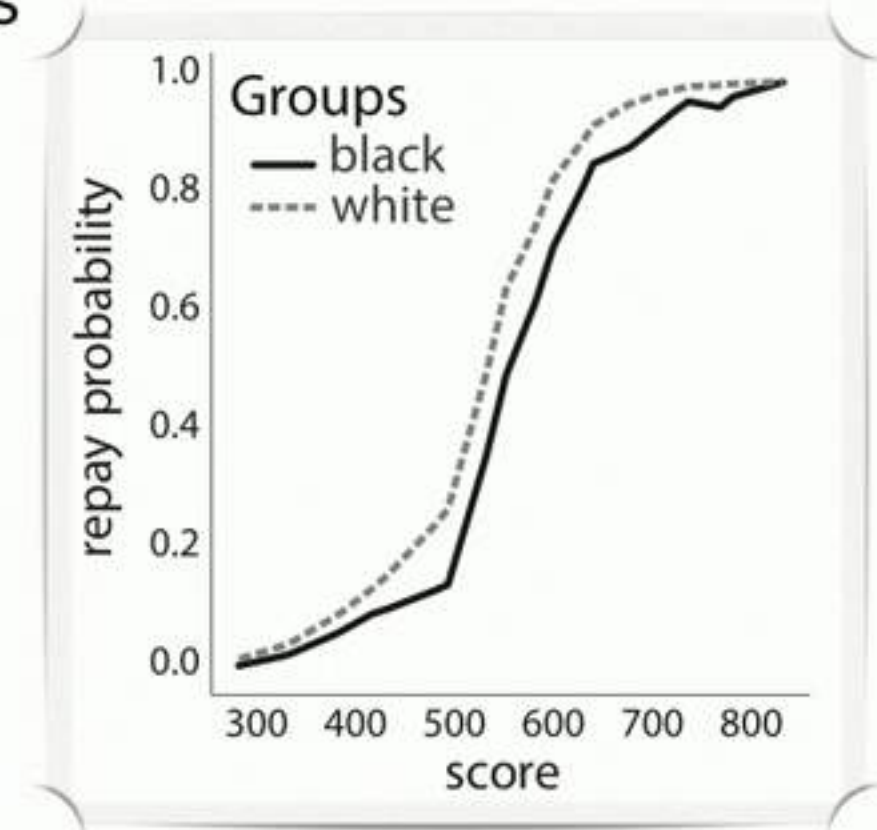


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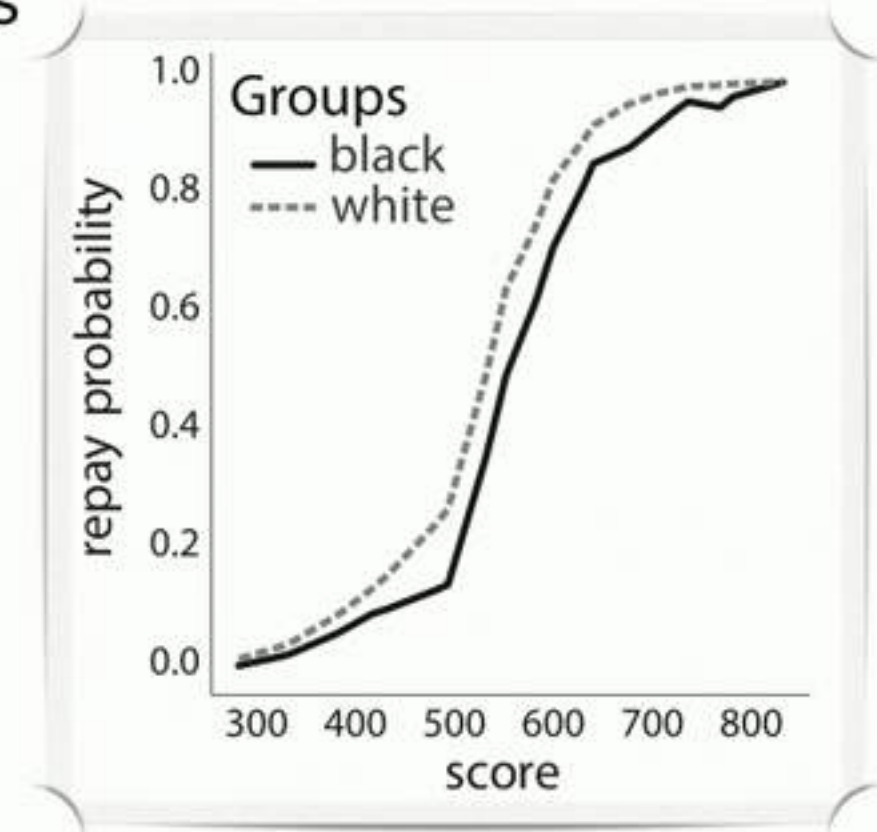


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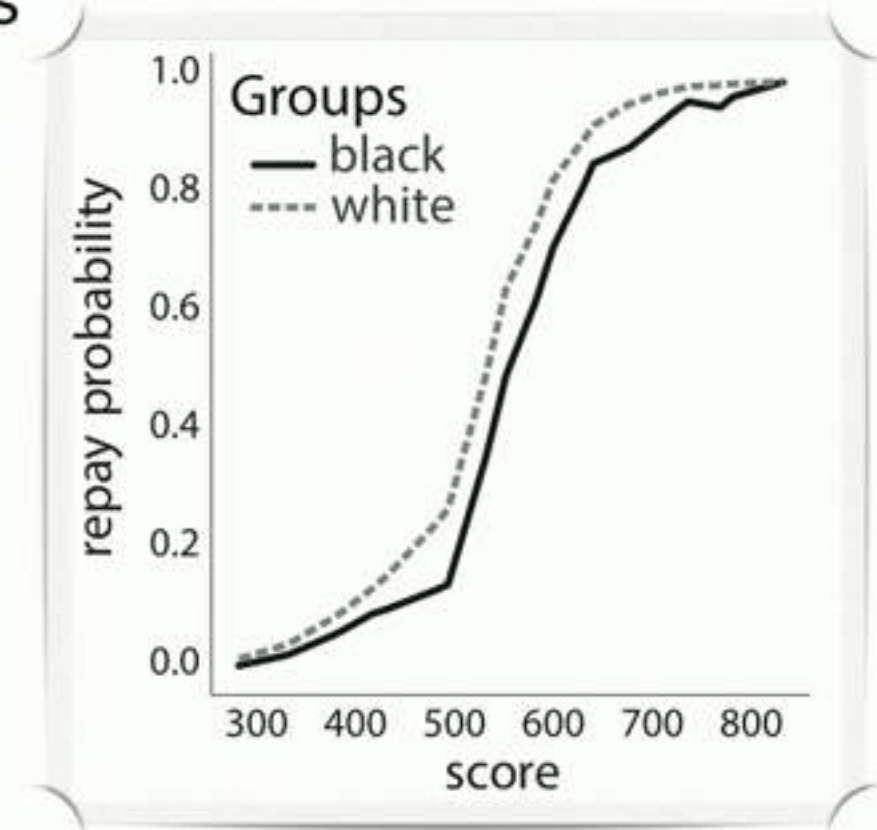


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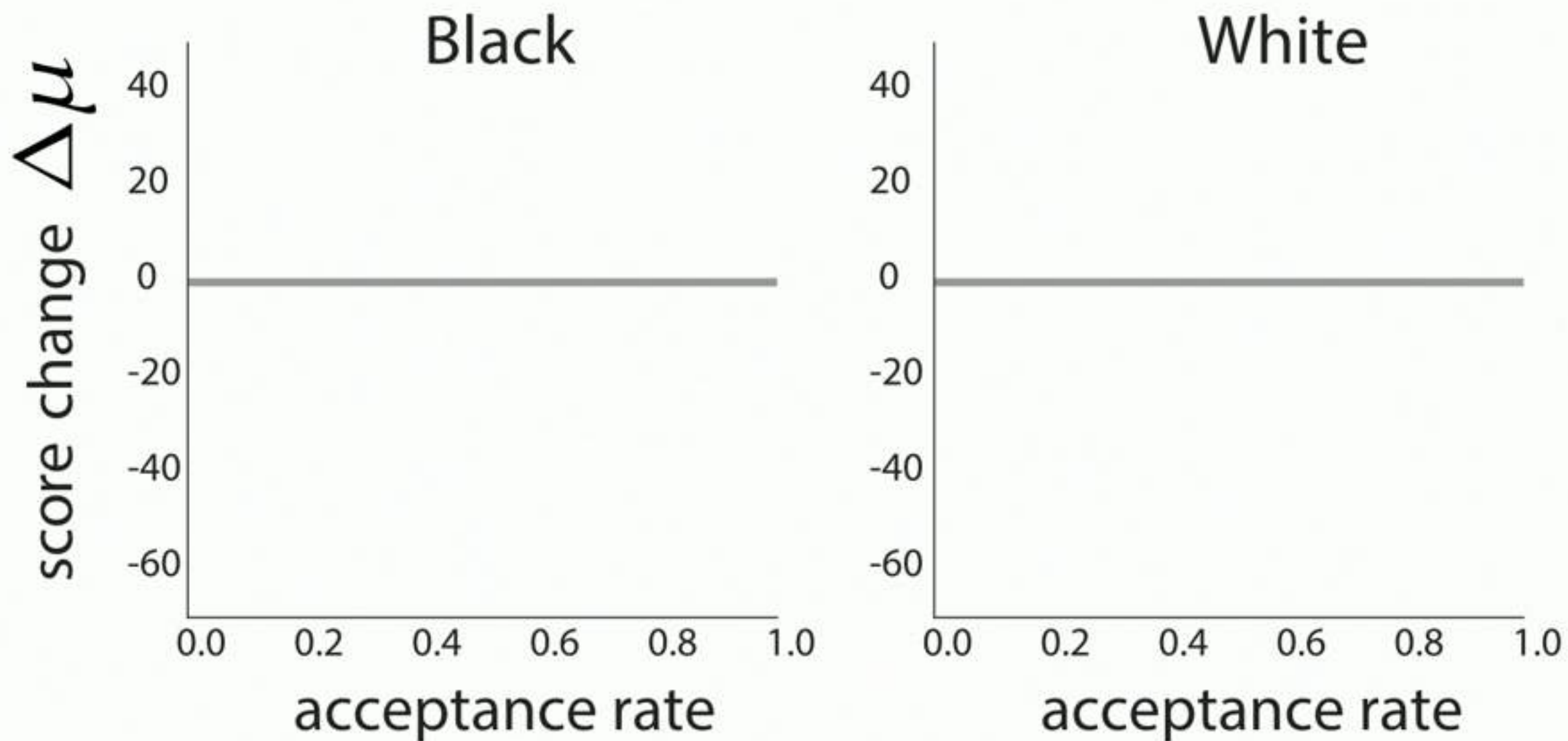
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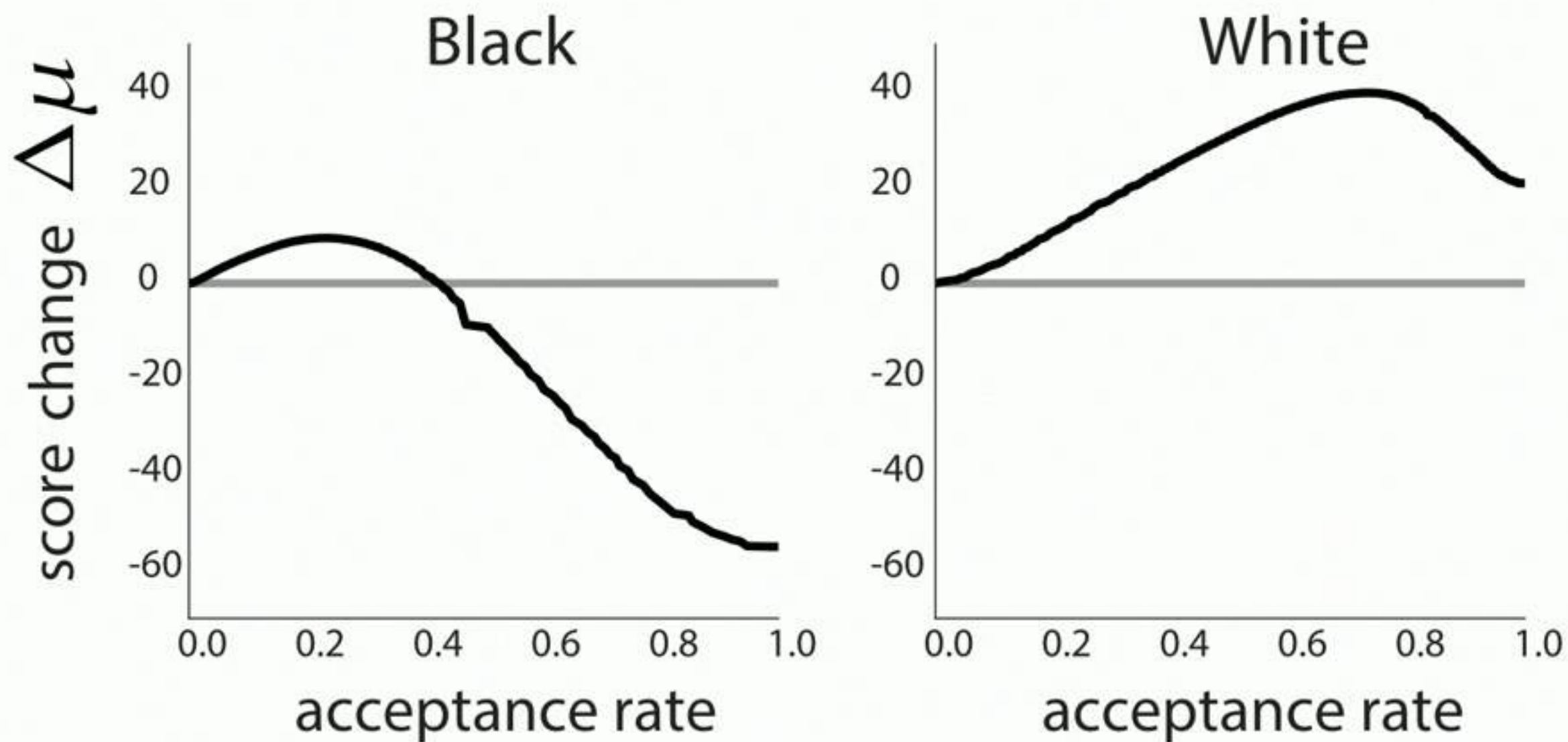
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- Compute "outcome curves" and delayed impact under different fairness criteria



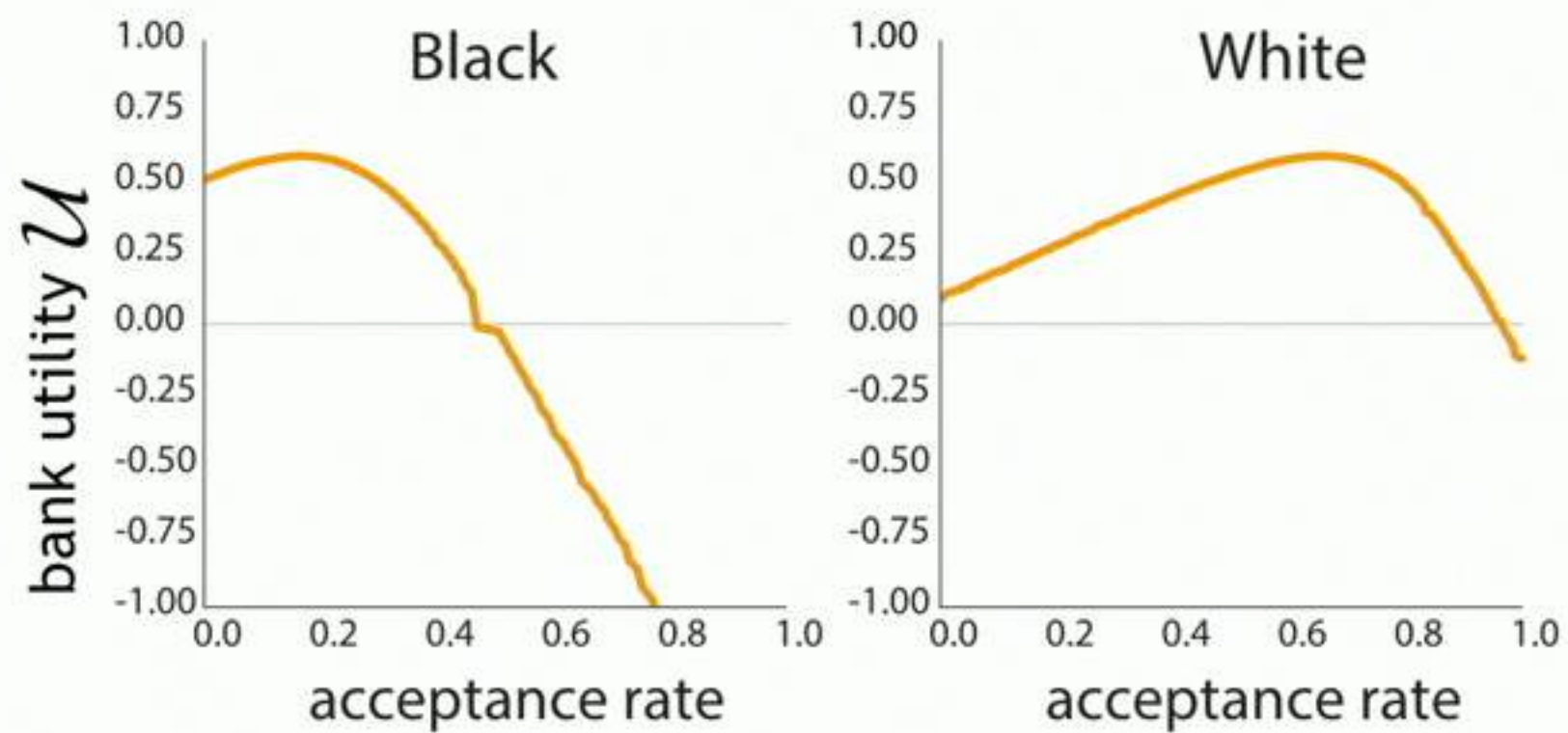
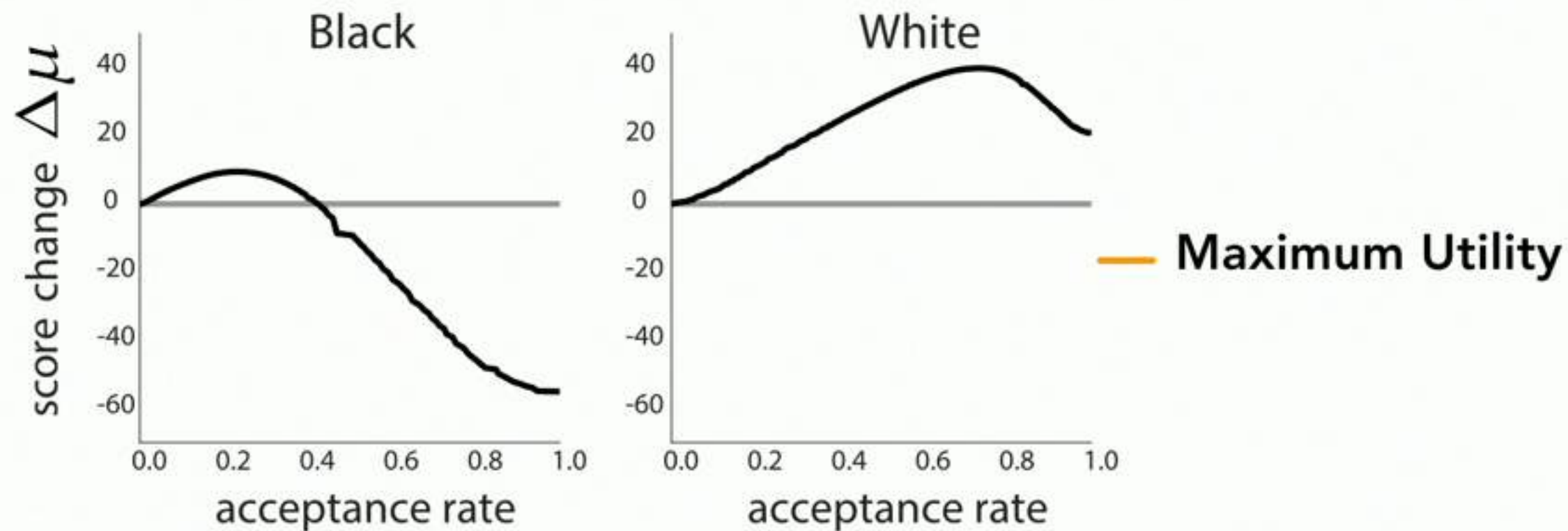
Outcome Curves



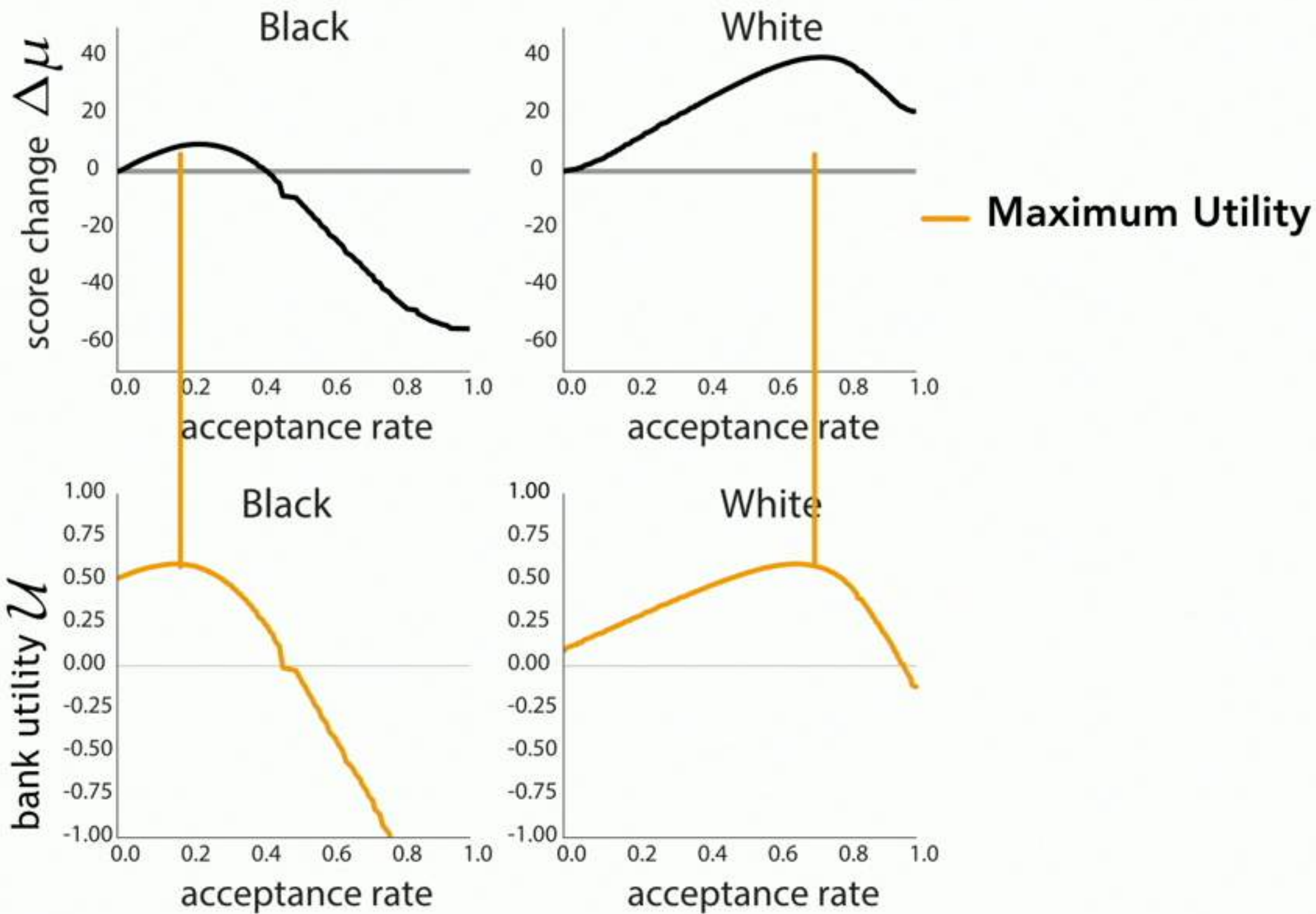
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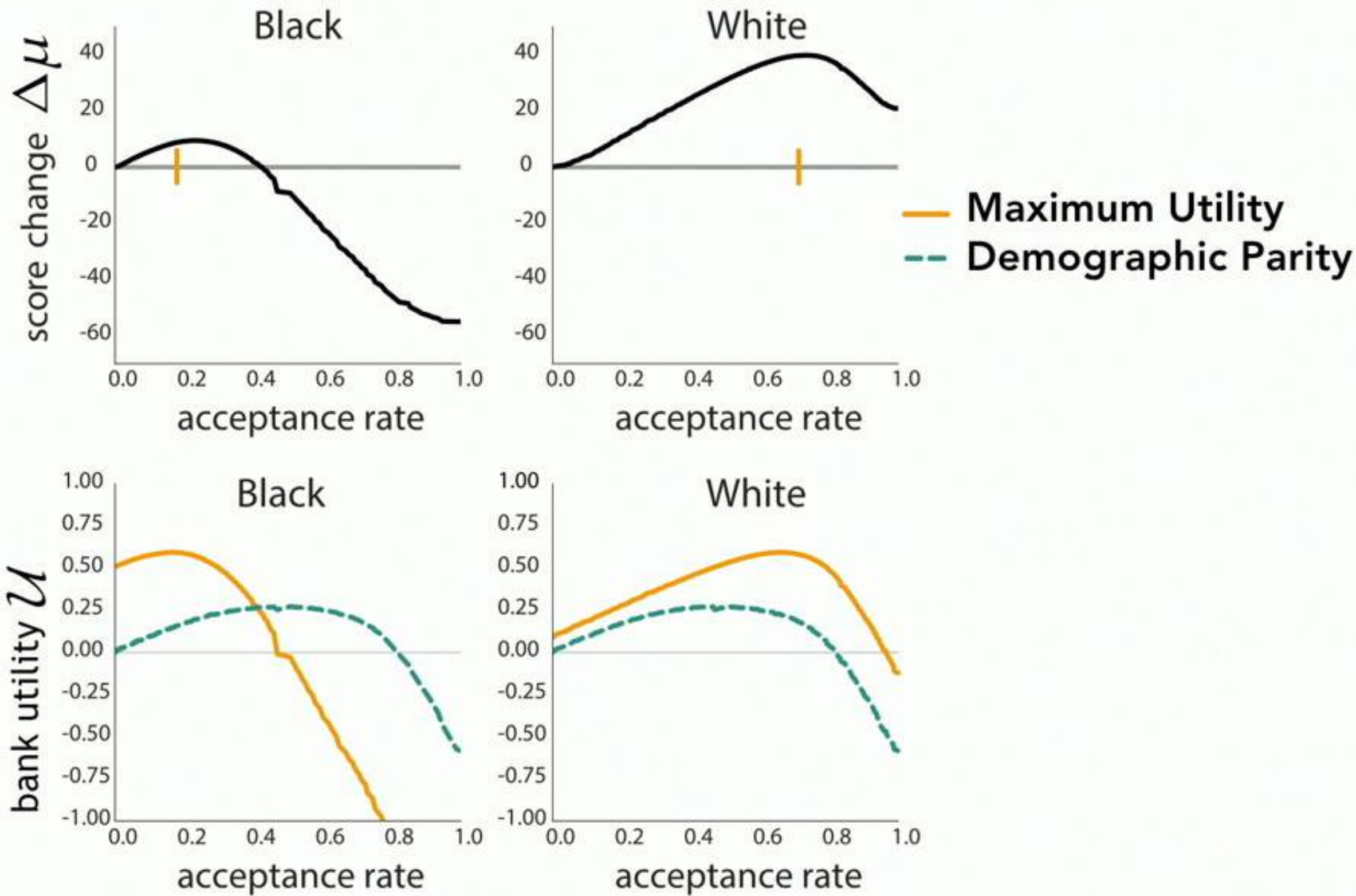
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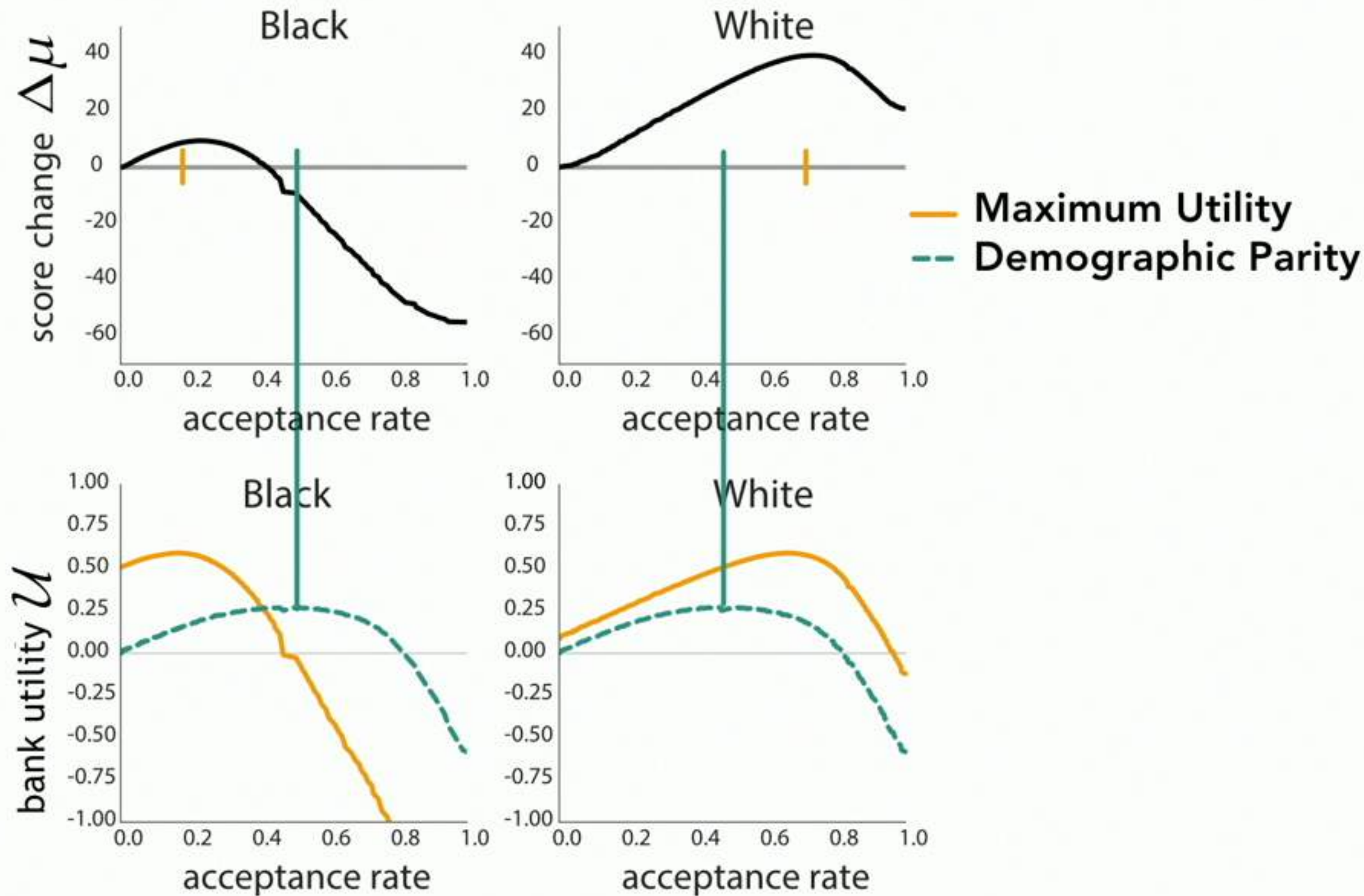
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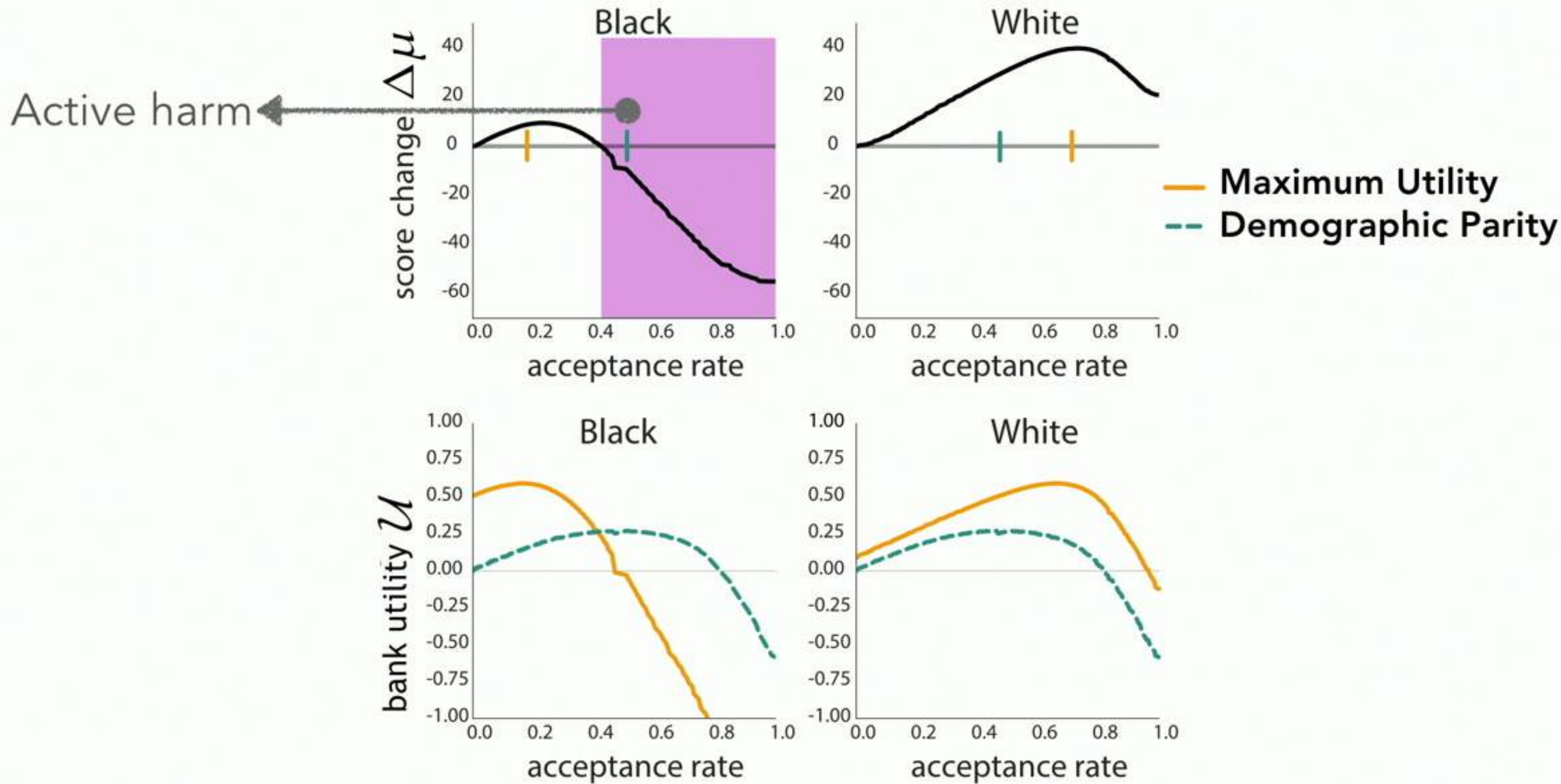
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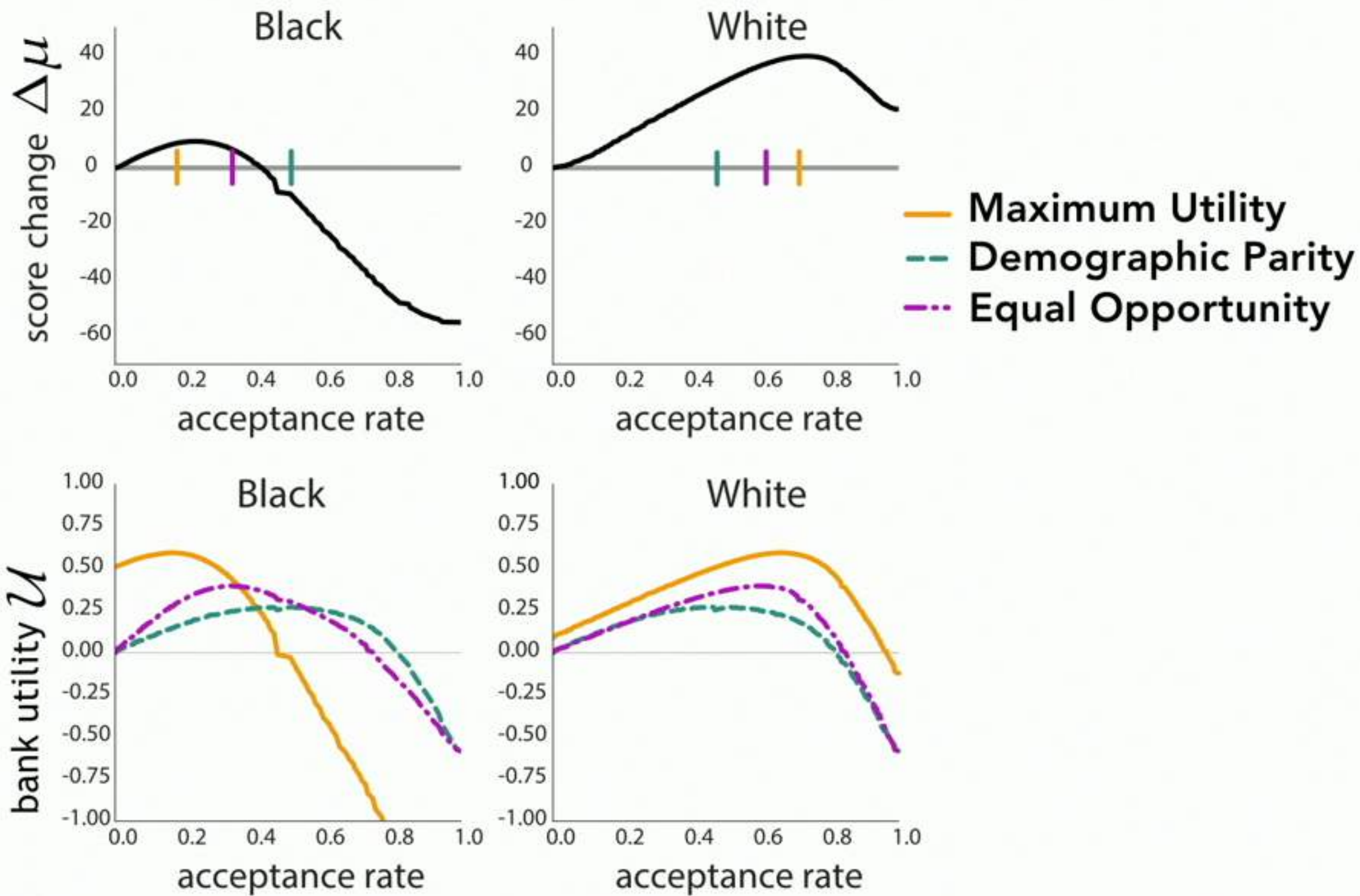
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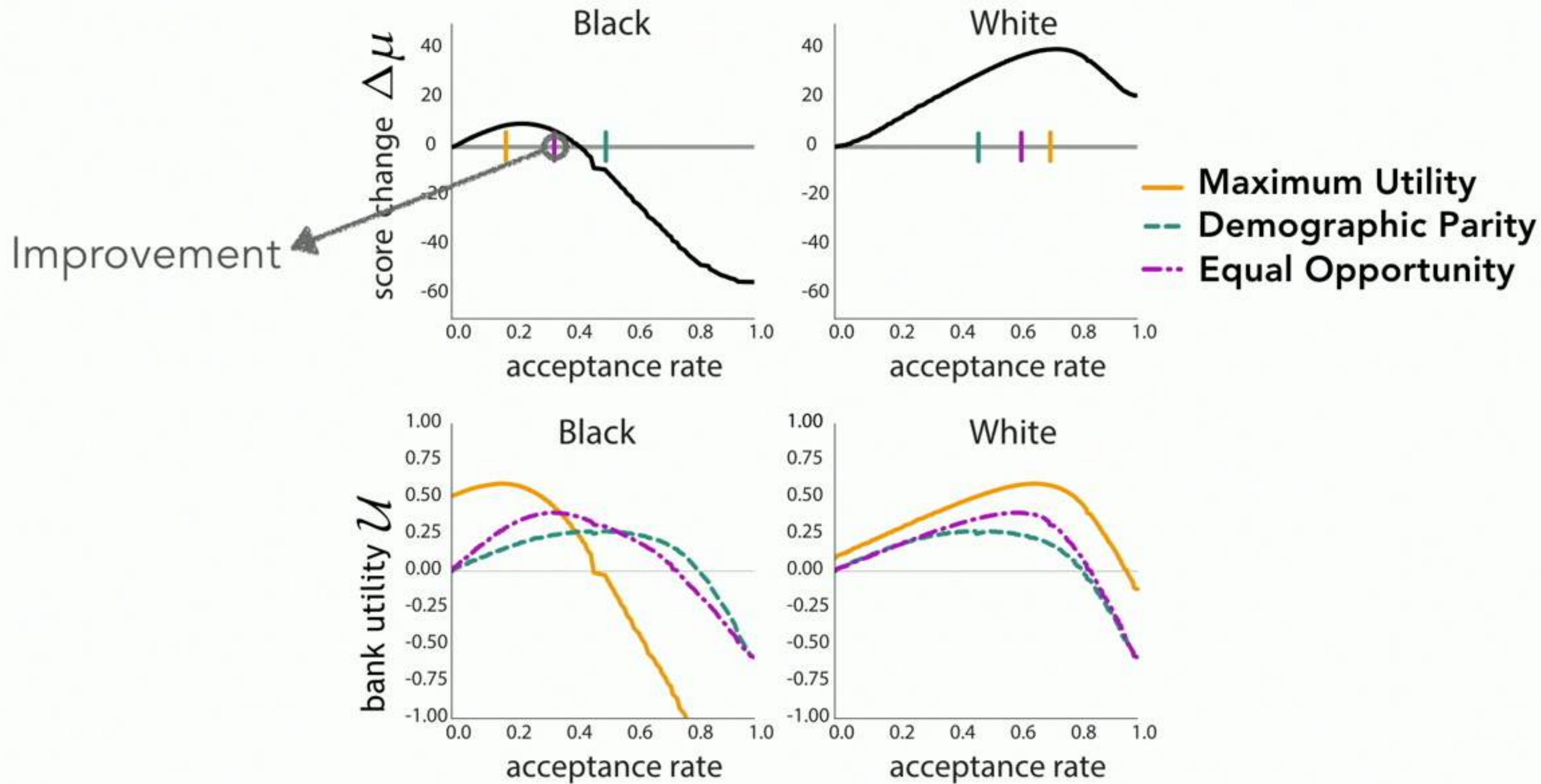
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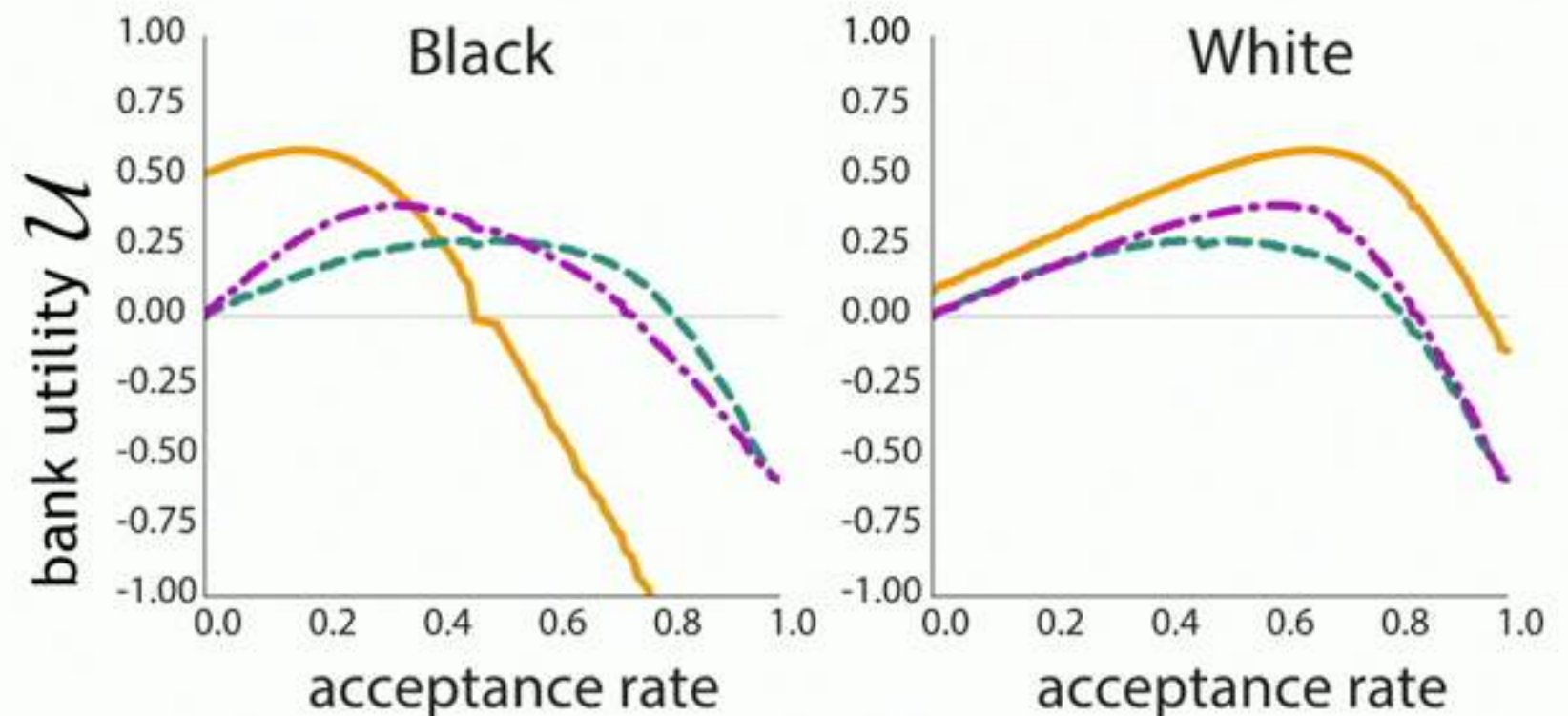
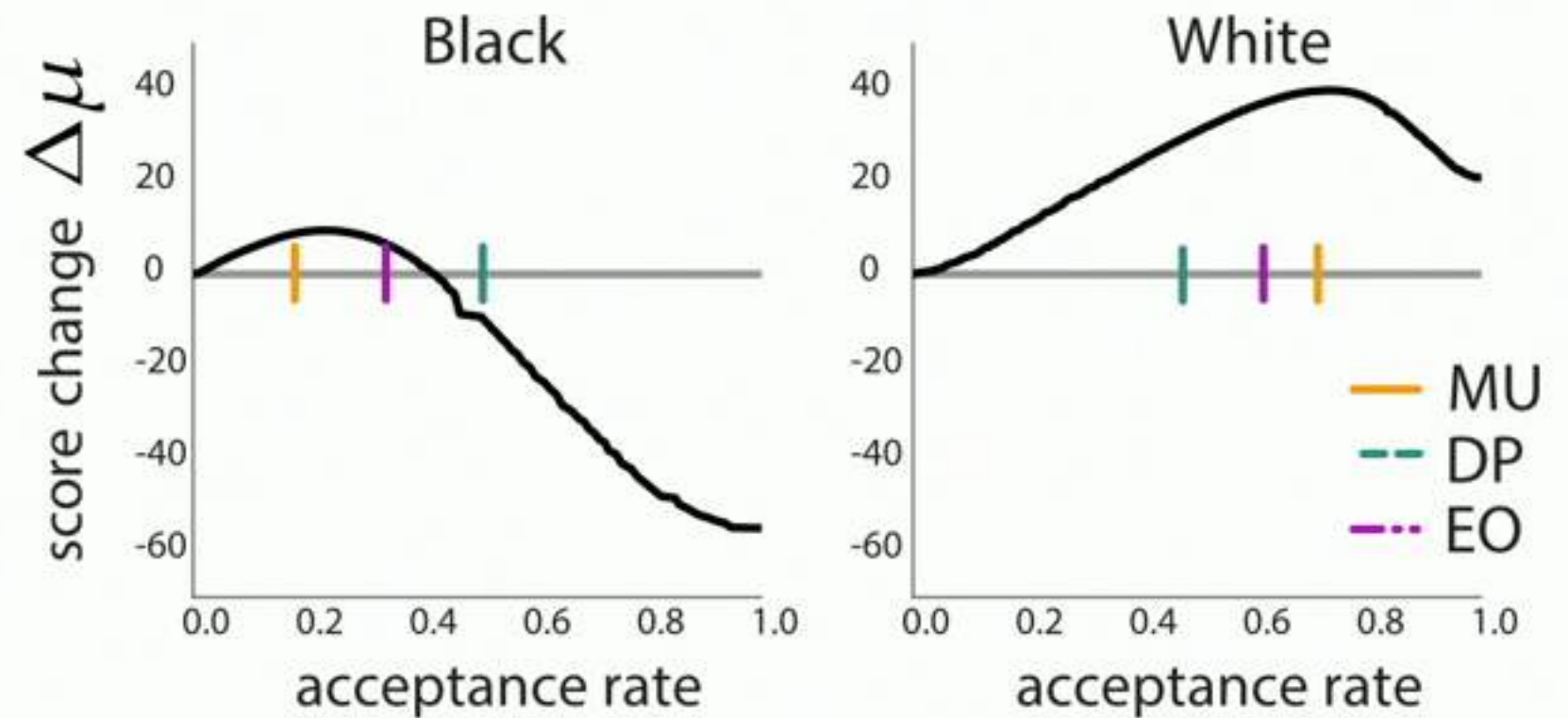


Outcome Curves



*Why the large difference
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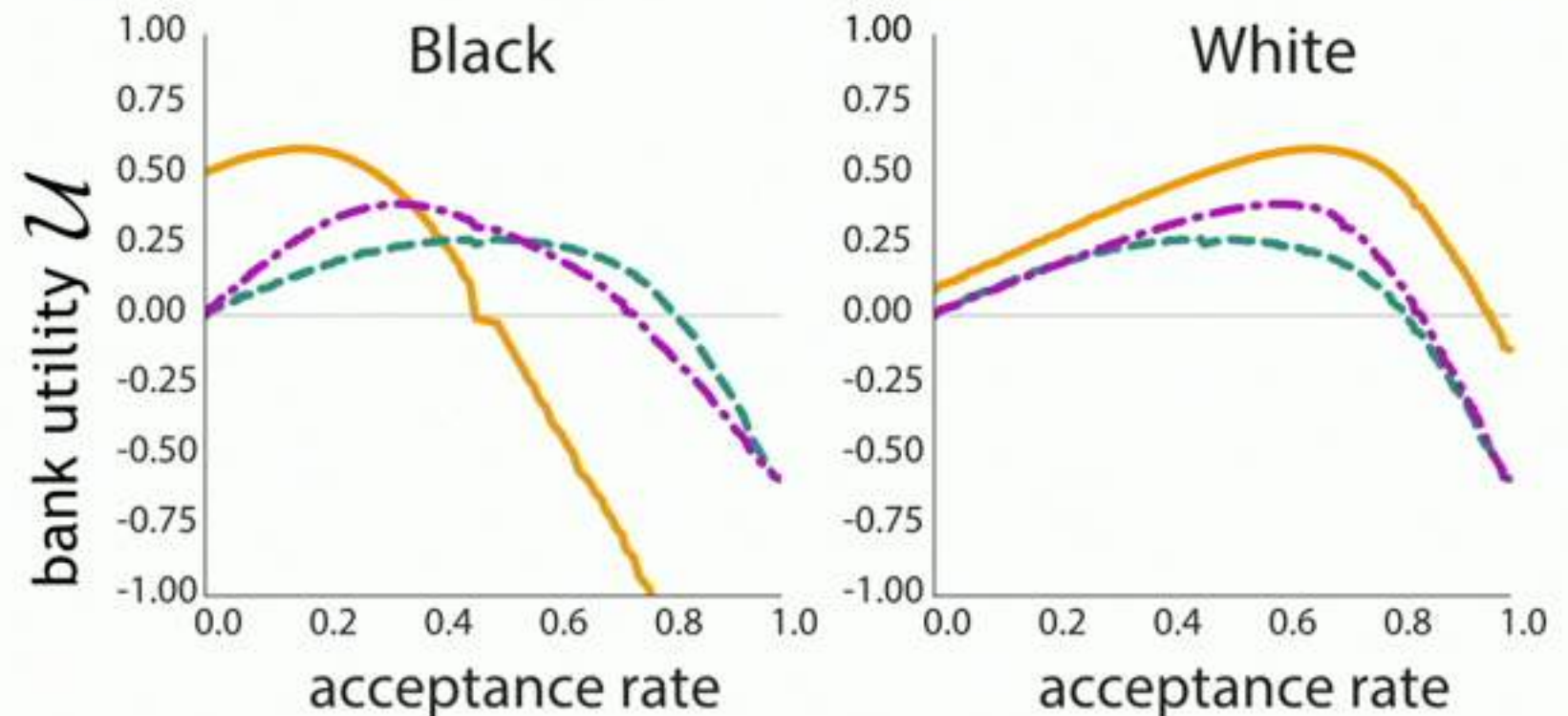
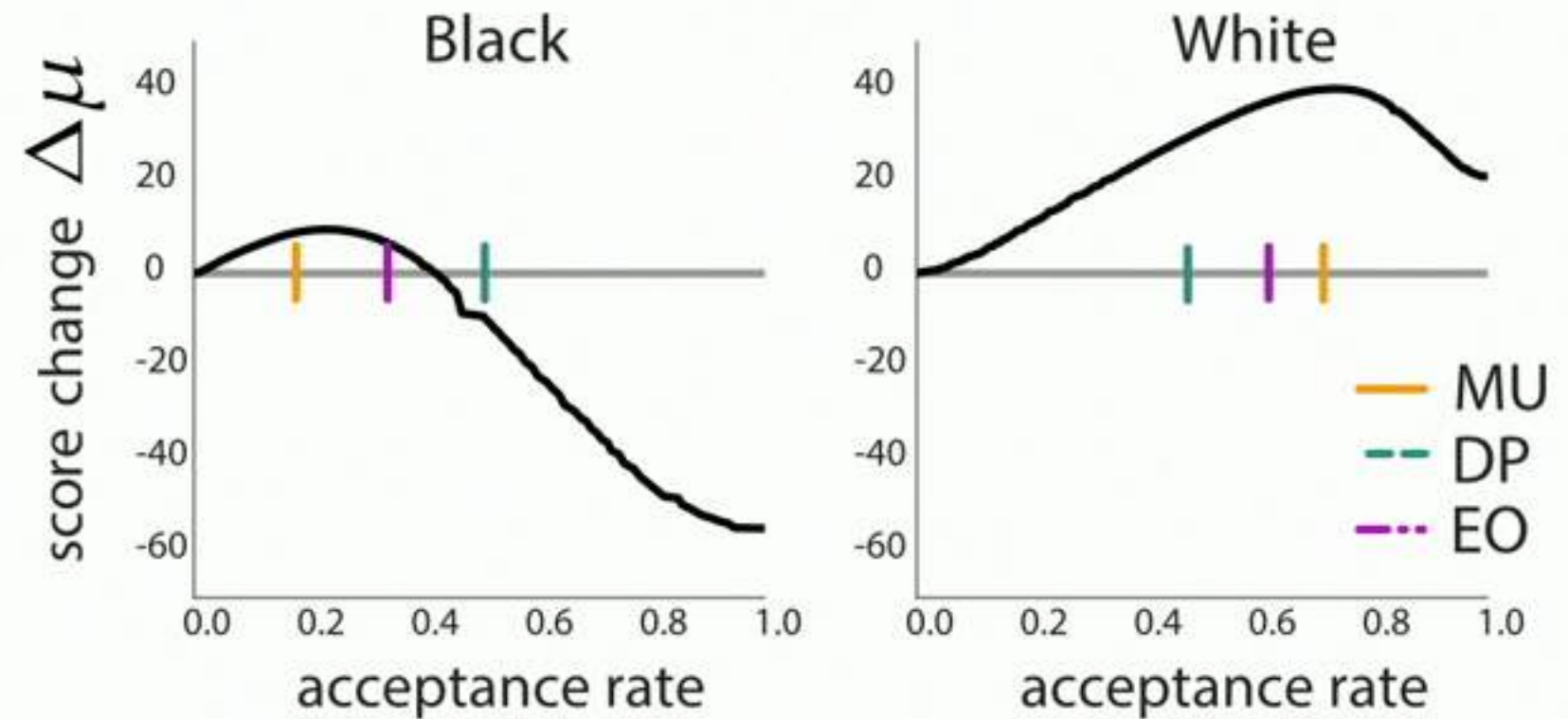
Outcome Curves



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Maxima of outcome and
utility curves under
fairness criteria are **more
misaligned** in the
minority "black" group

Outcome Curves



DISCUSSION

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FUTURE WORK

- Moving beyond **binary** decisions
- Moving beyond the **mean** score as measure of impact
- **Dynamics** of the **distributional impact** of machine learning algorithms
[Ensign et al. 2017; Hu and Chen 2017]

THANK YOU

Details in full version:
<https://arxiv.org/abs/1803.04383>

