



UNIVERSITY *of* WASHINGTON

Design and Optimization of Dielectric Metasurface Optics

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Department of Physics

University of Washington, Seattle

June 12th, 2019







Applications for optical hardware

3

Applications for optical hardware

3



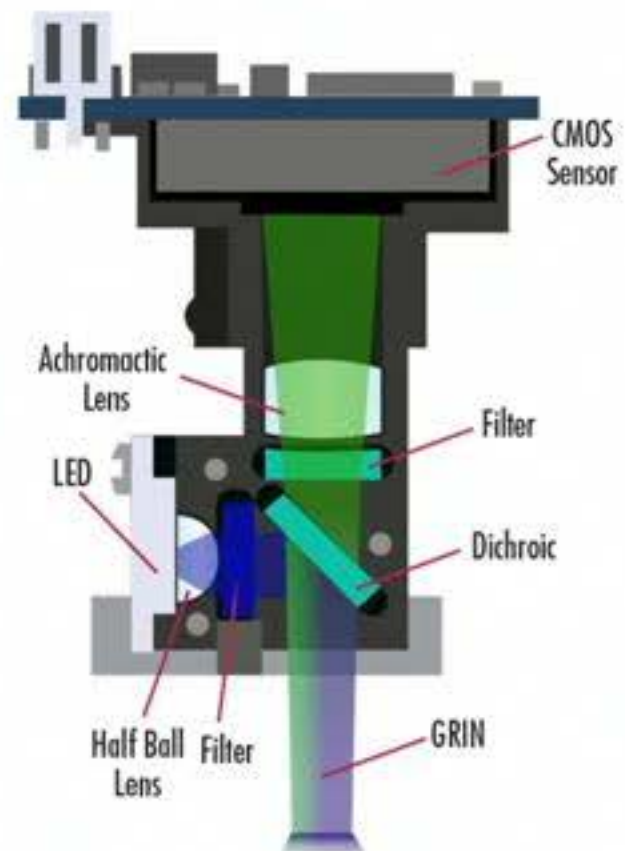
Applications for optical hardware

3



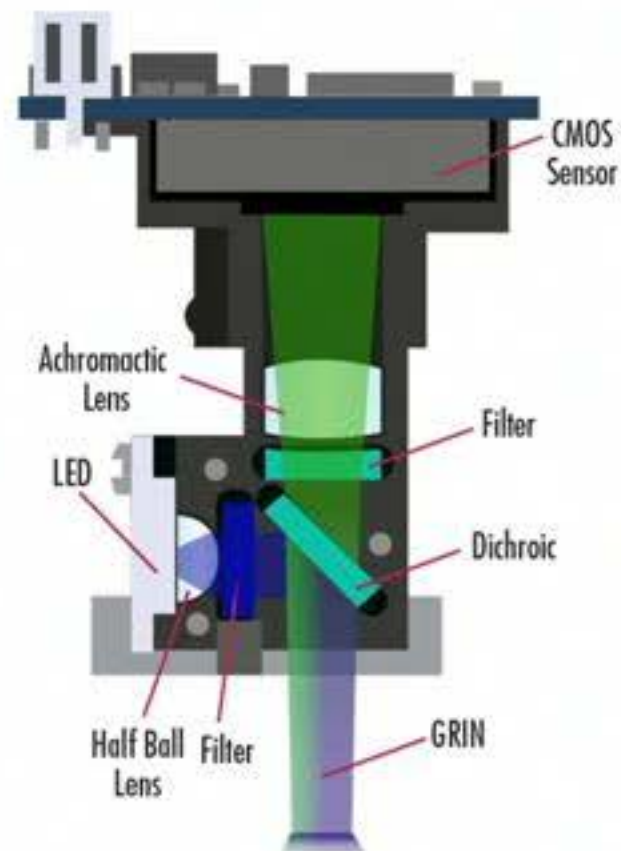
Applications for optical hardware

3



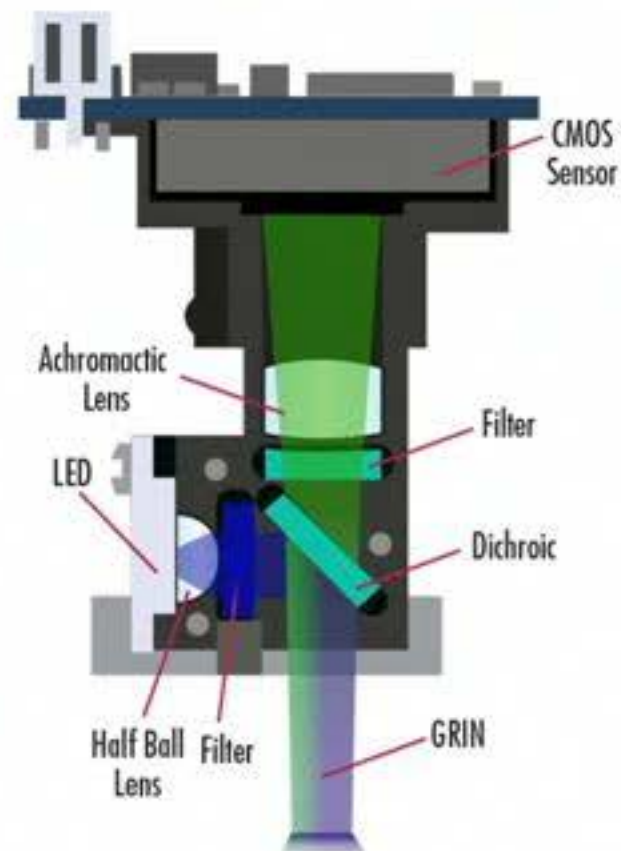
Applications for optical hardware

3



Applications for optical hardware

3



Diffraction optics

4

Amplitude

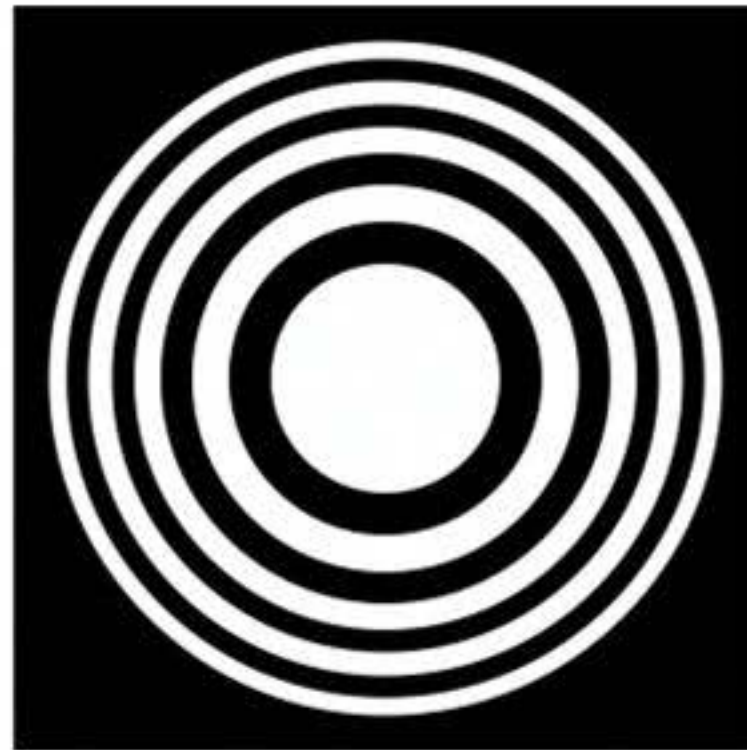
Phase

Amplitude



Phase

Amplitude



Phase



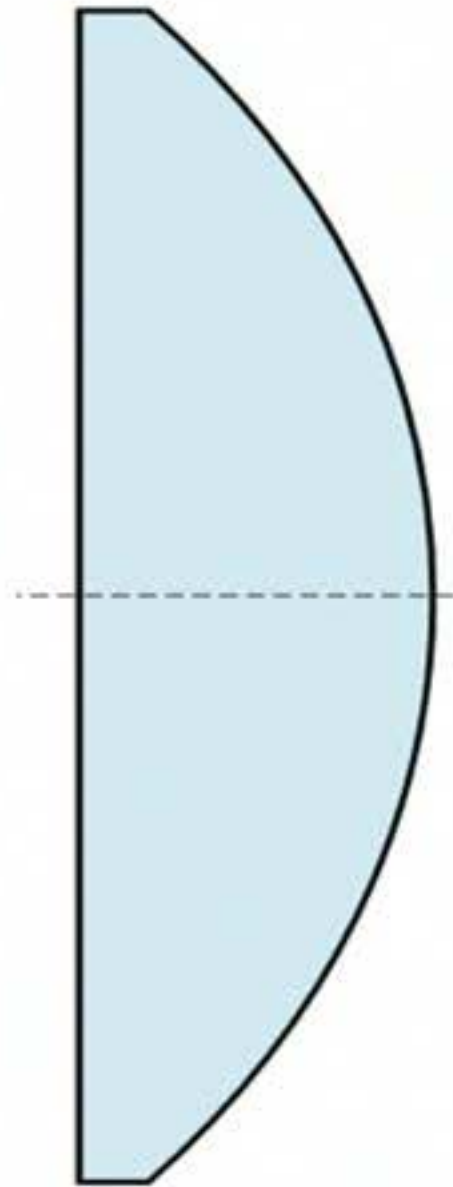
Walsby et al. Opt. Lett. **32**, 9 (2007)

From refractive to diffractive optics

5

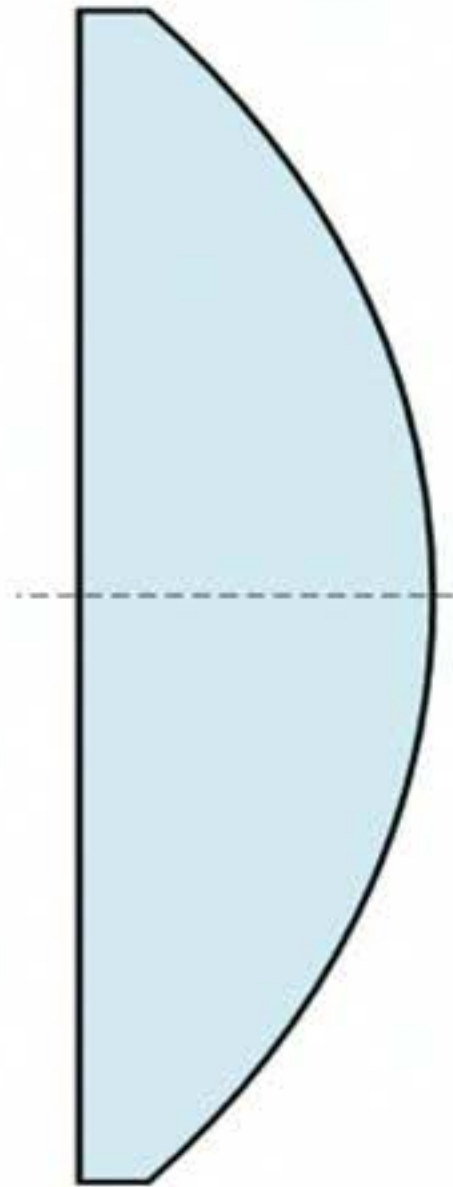
From refractive to diffractive optics

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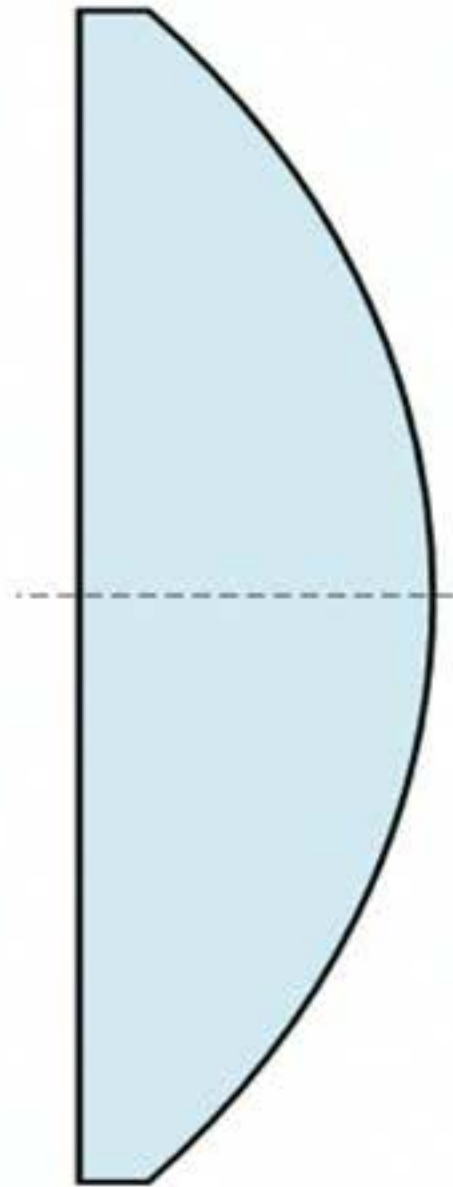


From refractive to diffractive optics

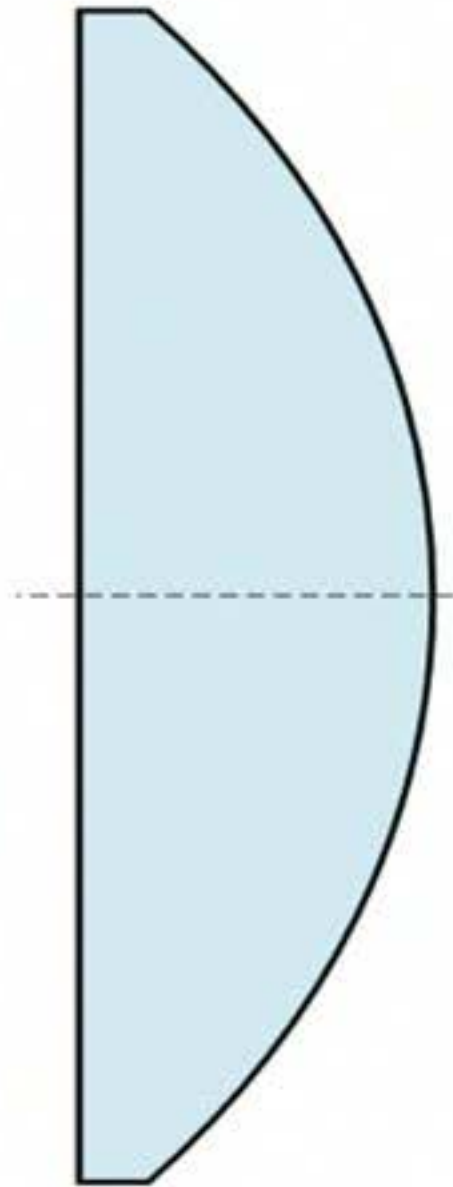
5



$$\varphi(x) = \frac{2\pi n}{\lambda} t(x)$$

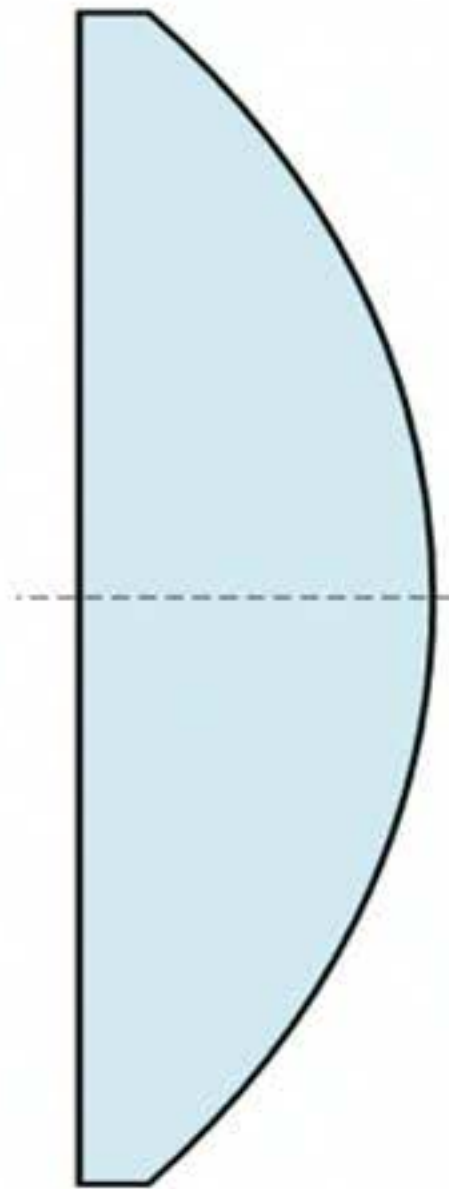


$$\varphi(x) = \frac{2\pi n}{\lambda} t(x)$$

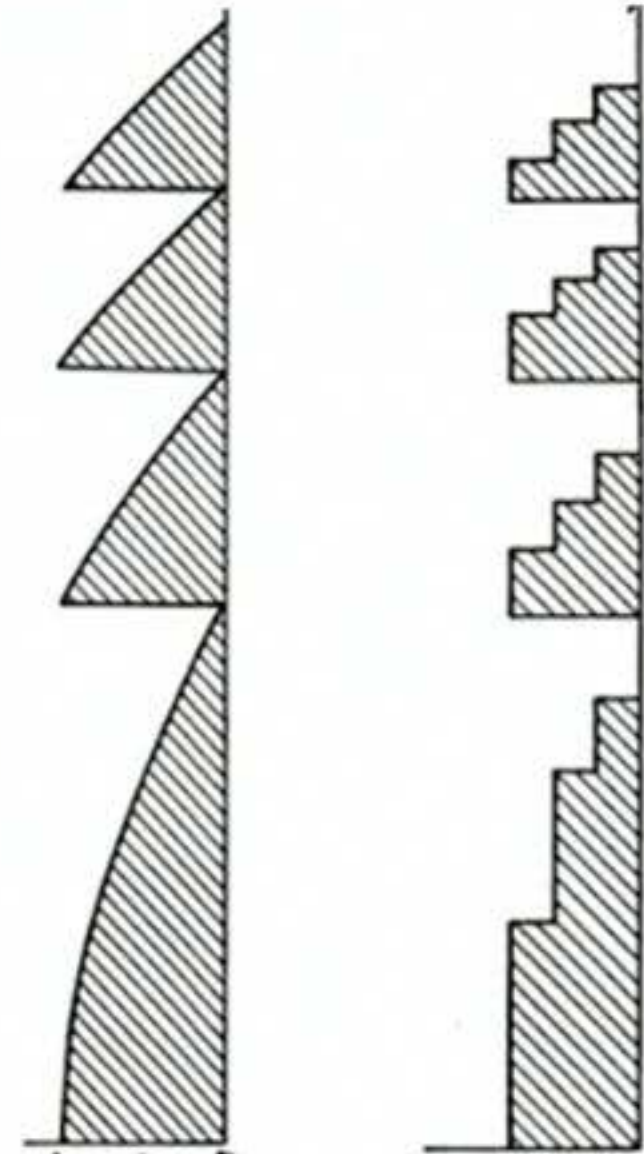


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Diffractive grating optics

7

Diffractive grating optics

7

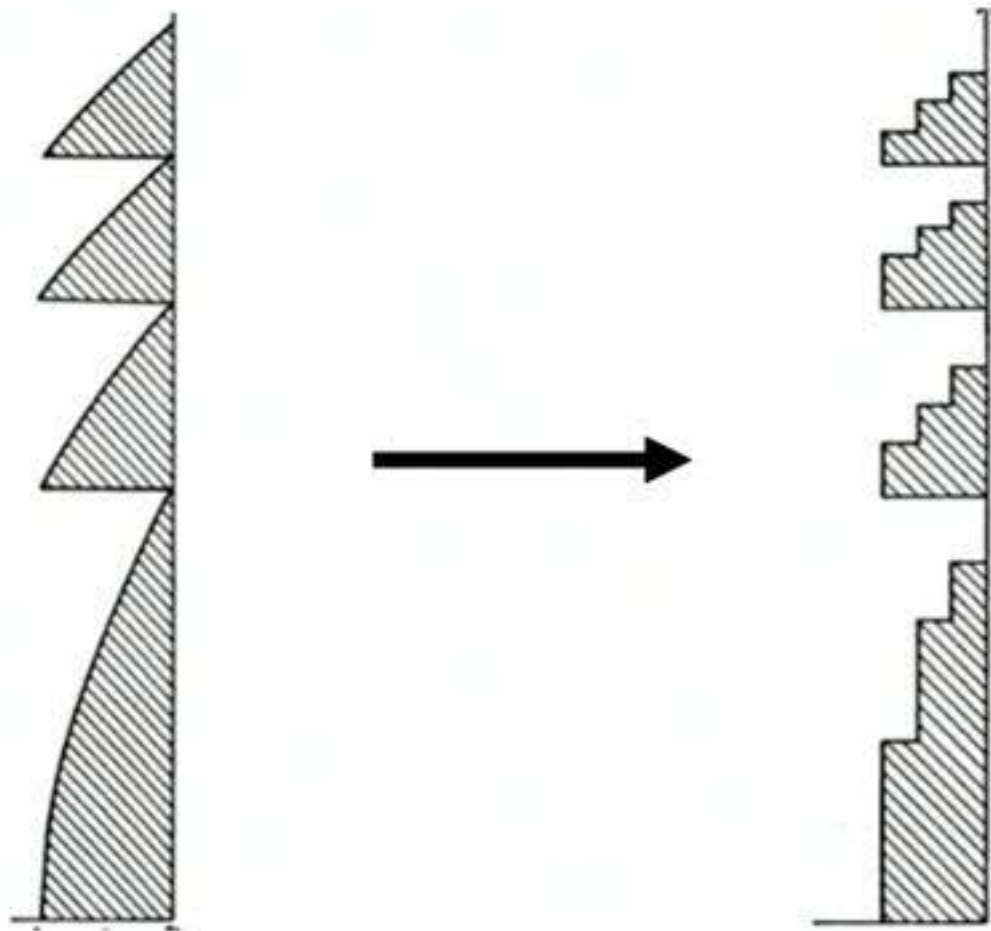
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Diffractive grating optics

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Diffraction grating optics

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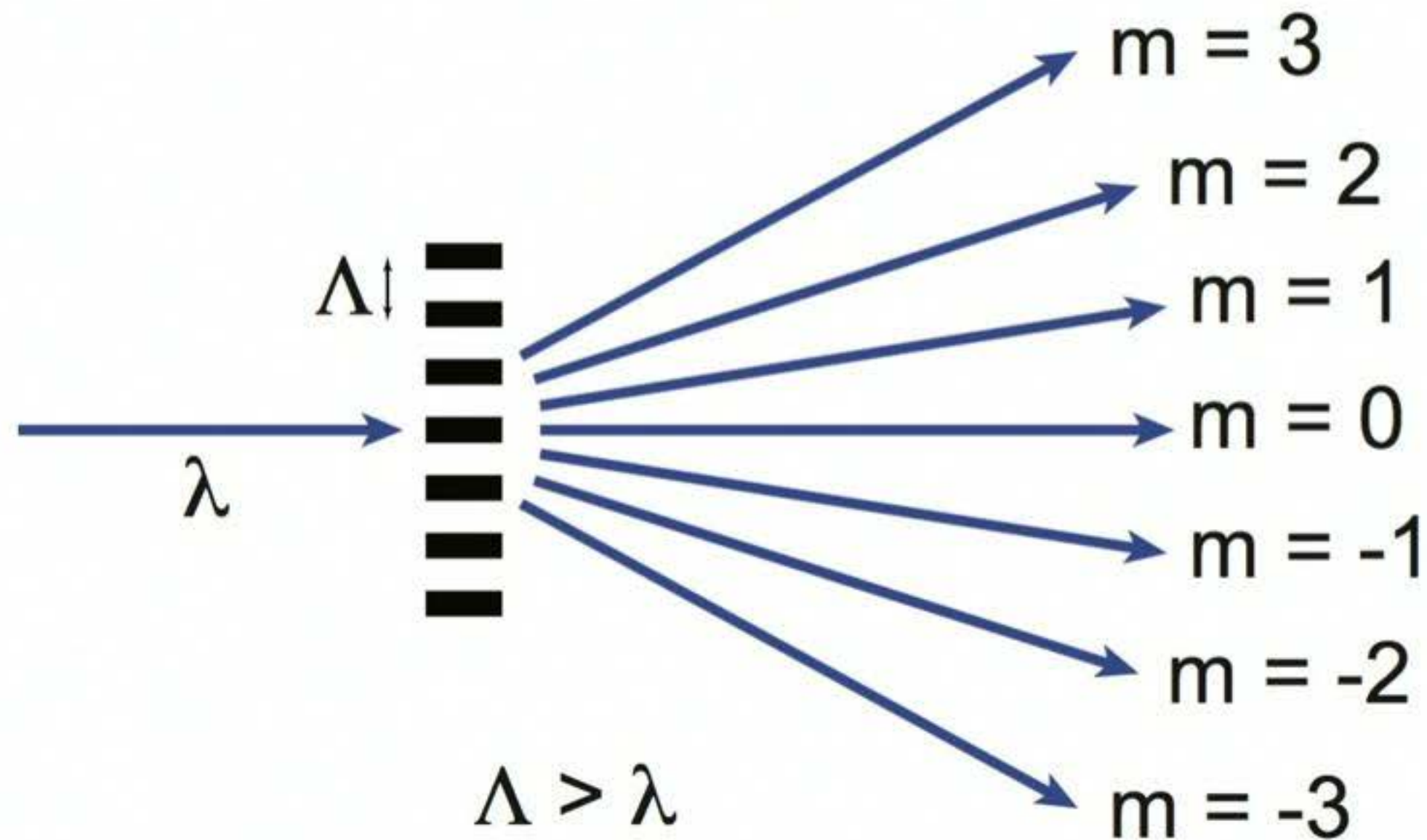
$$\varphi(x) = \frac{2\pi n}{\lambda} t(x)$$

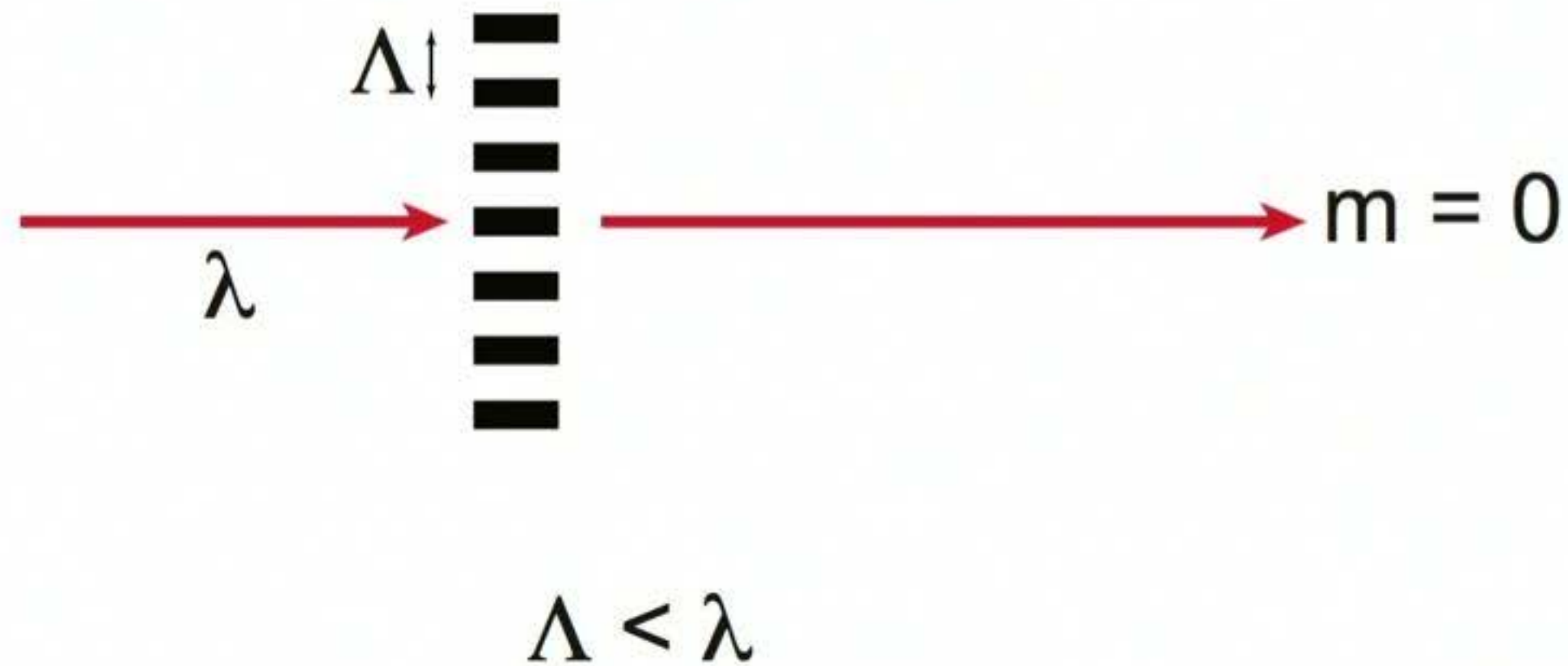


$$\varphi(x) \sim \frac{2\pi n_{eff}(x)}{\lambda} t$$

Grating diffraction

8





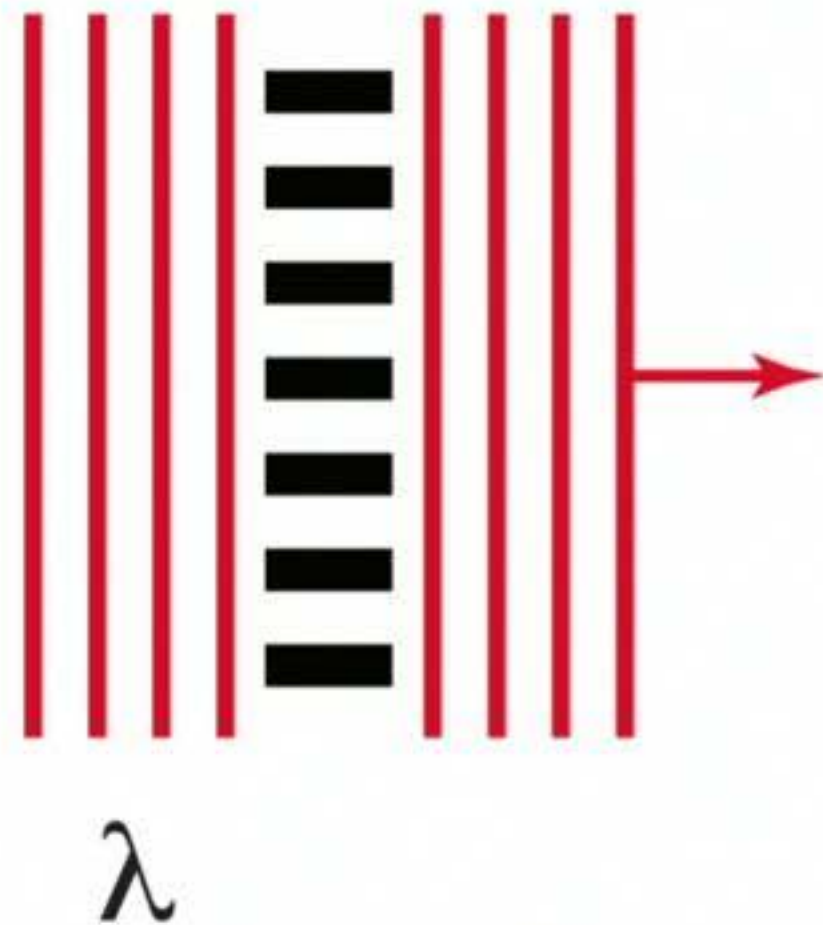
Modulating phase

10

Modulating phase

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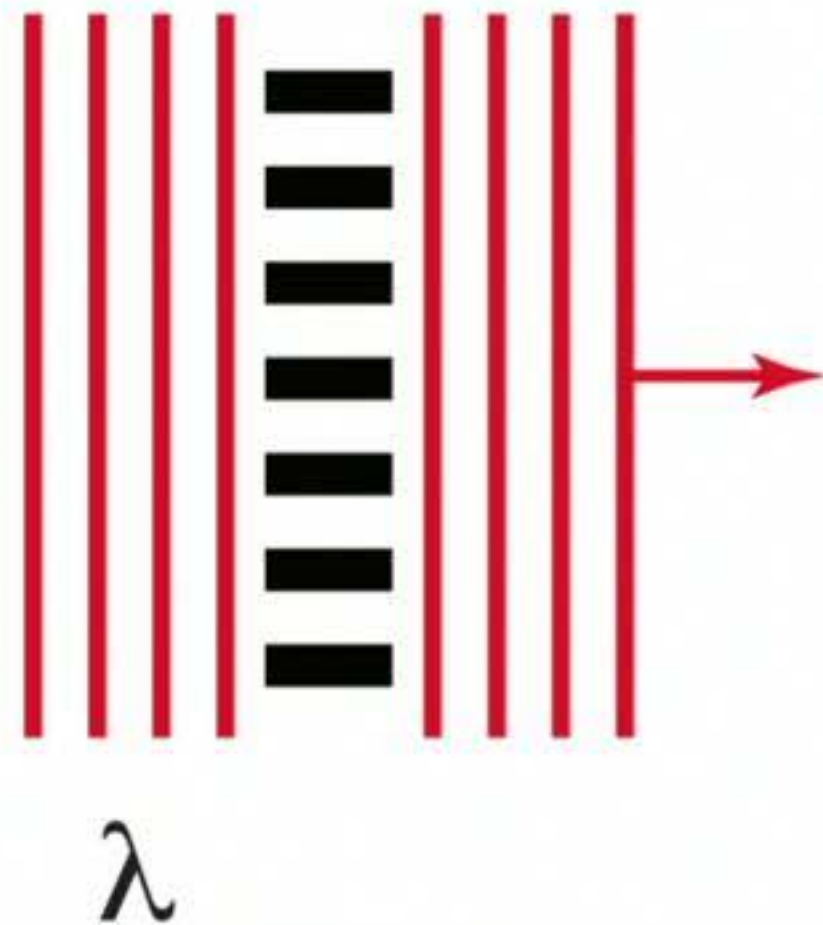
Uniform phase shift



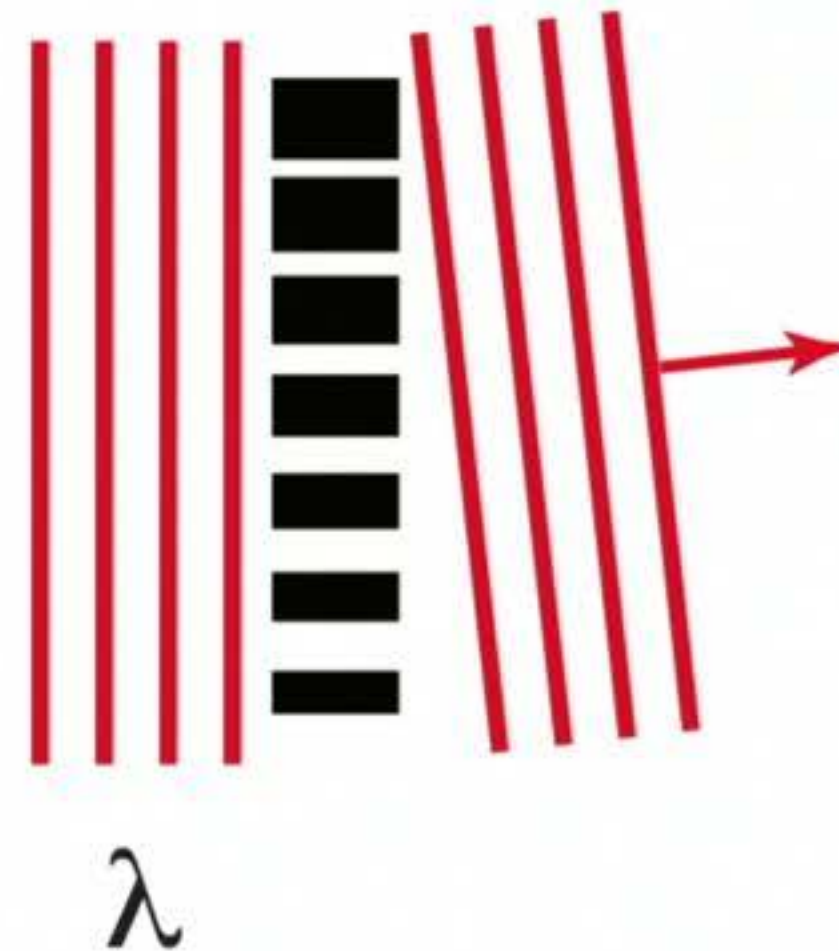
Modulating phase

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Uniform phase shift



Spatially varying phase shift

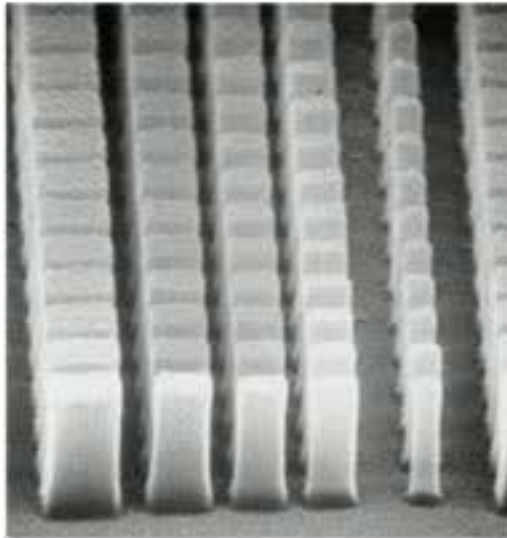


Dielectric metasurface optics

11

Dielectric metasurface optics

11



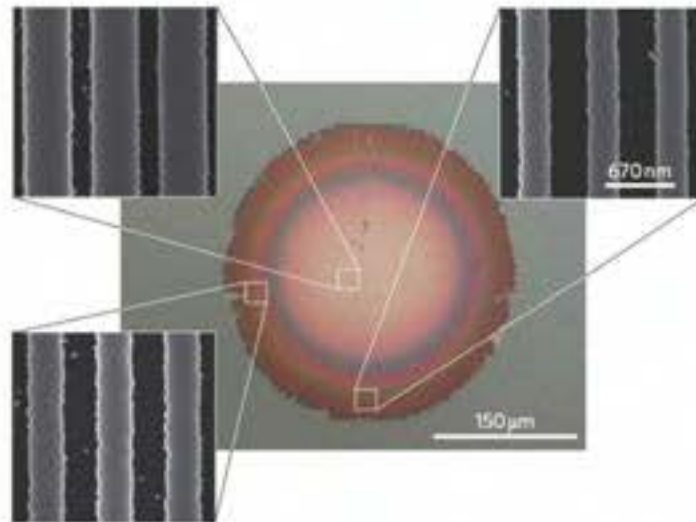
Lalanne et al. Opt. Lett. **23**,
14 (1998)

Dielectric metasurface optics

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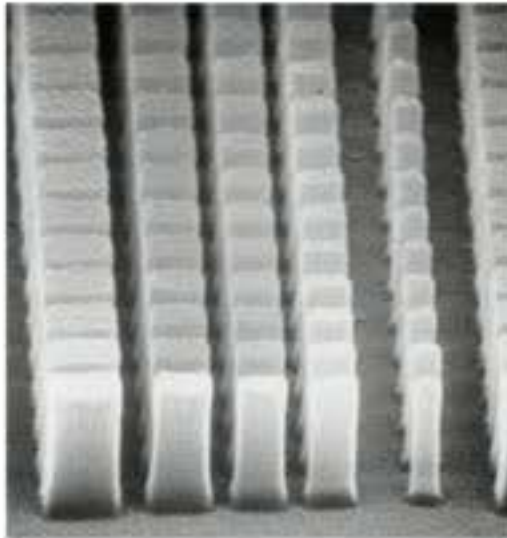
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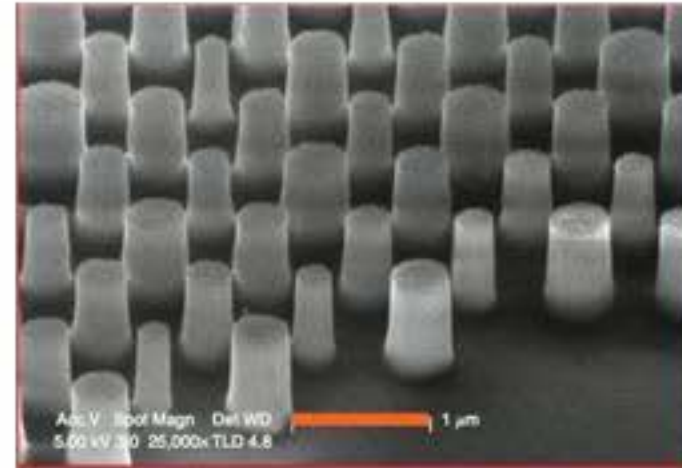
Fattal et al. Nat. Photon. **4**, 466
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Dielectric metasurface optics

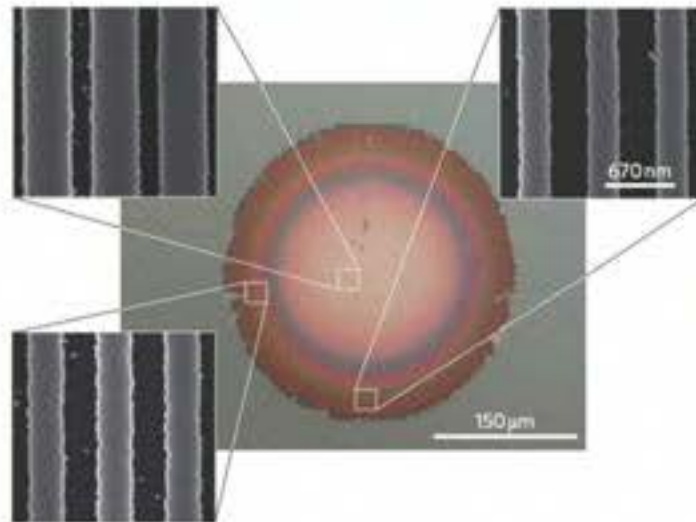
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Lalanne et al. Opt. Lett. **23**,
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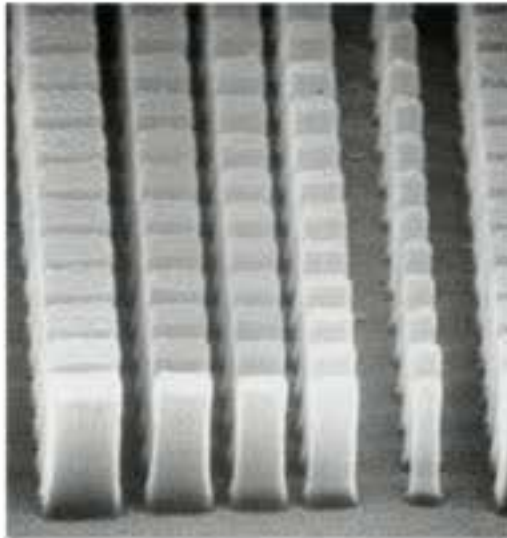
Arbabi et al. Nat. Comm. **6**, 7069
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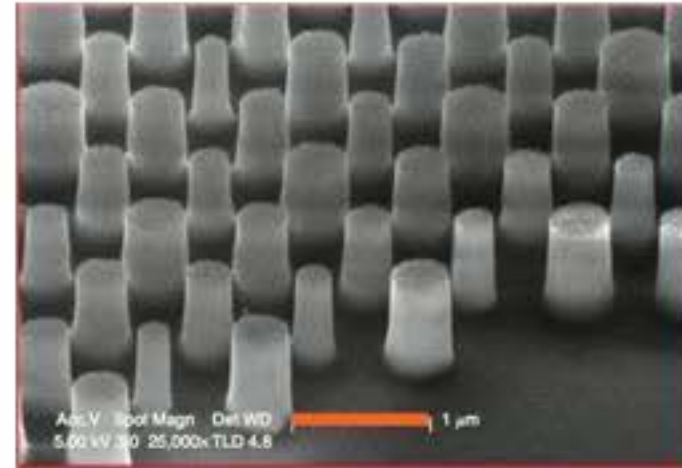
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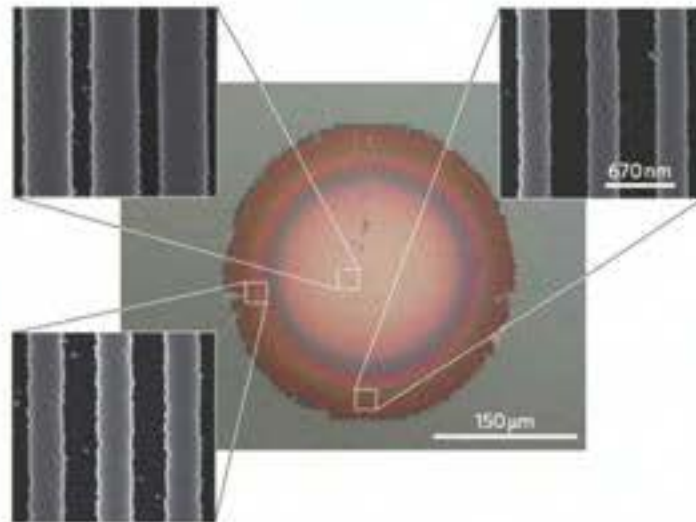
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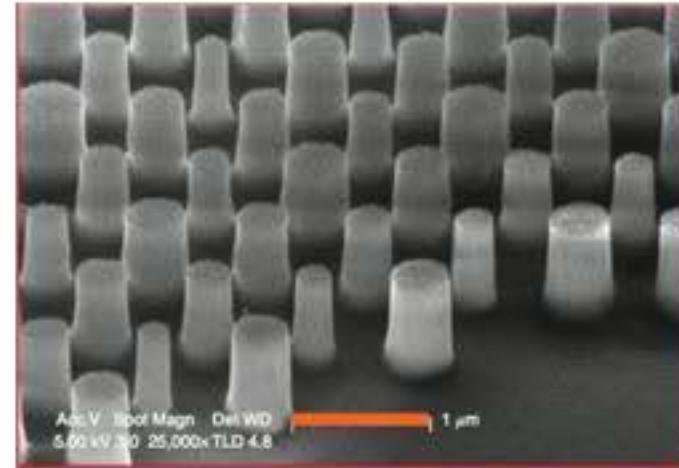
Khorasaninejad et al. Science. **352**,
6290 (2016)

Dielectric metasurface optics

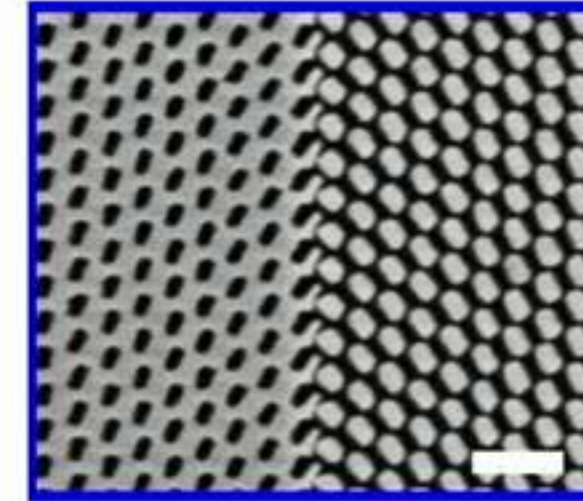
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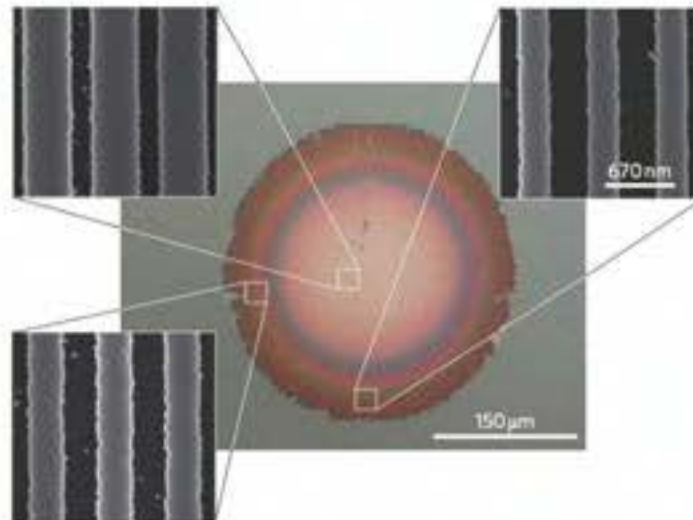
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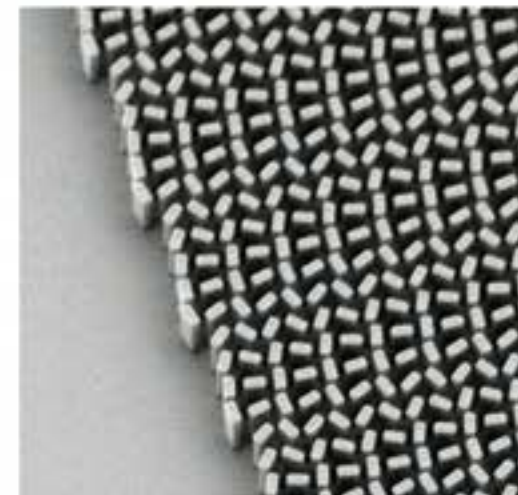
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Wang et al. Nat. Nano. **13**,
227 (2018)



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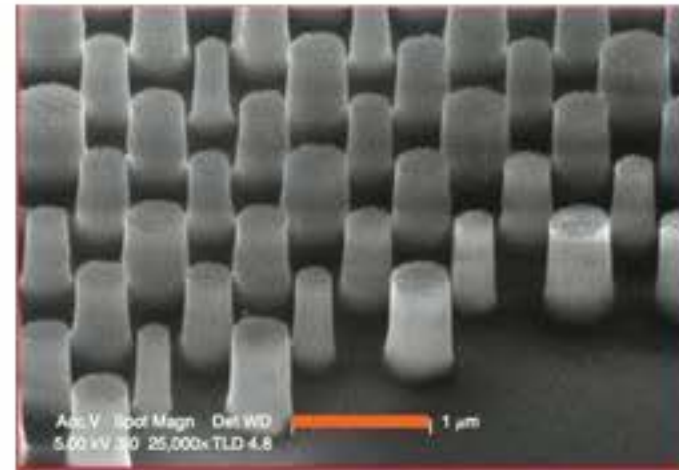
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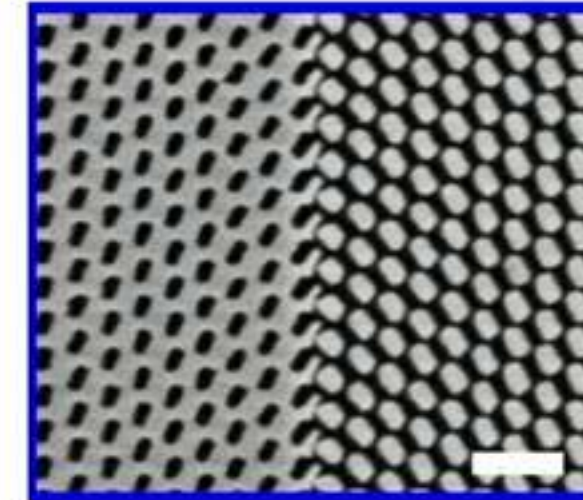
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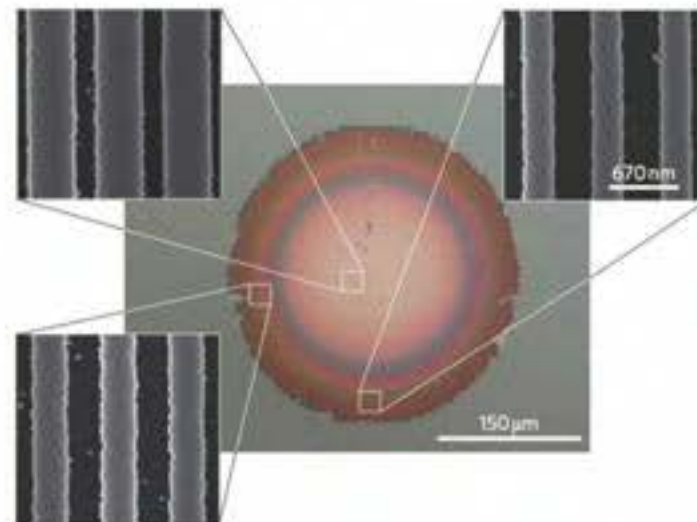
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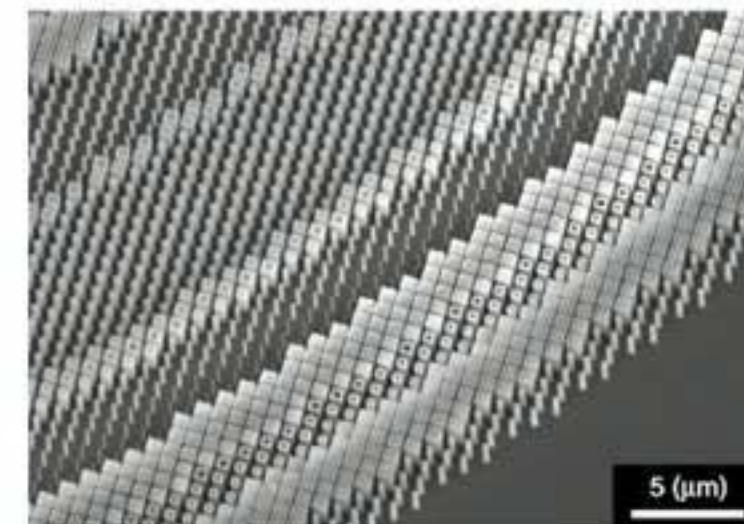
Wang et al. Nat. Nano. **13**, 227 (2018)



Fattal et al. Nat. Photon. **4**, 466 (2010)



Khorasaninejad et al. Science. **352**, 6290 (2016)



Shrestha et al. Light: Sci. and Appl. **7**, 95 (2018)

How do I best implement a given optical function on a metasurface?

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Comes down to:

How do I best take advantage of the large numbers of degrees of freedom?

How do I best implement a given optical function on a metasurface?

Comes down to:

How do I best take advantage of the large numbers of degrees of freedom?

A relatively small $100 \times 100 \mu m^2$ metasurface with periodicity 500 nm has at least 4×10^4 degrees of freedom

Solving the design problem

13

Forward design

Intuition based

Forward design

Intuition based

Scatterers



Functionality

Solving the design problem

13

Forward design

Intuition based

Scatterers



Functionality

Inverse design

Computation based

Solving the design problem

13

Forward design

Intuition based

Scatterers



Functionality

Inverse design

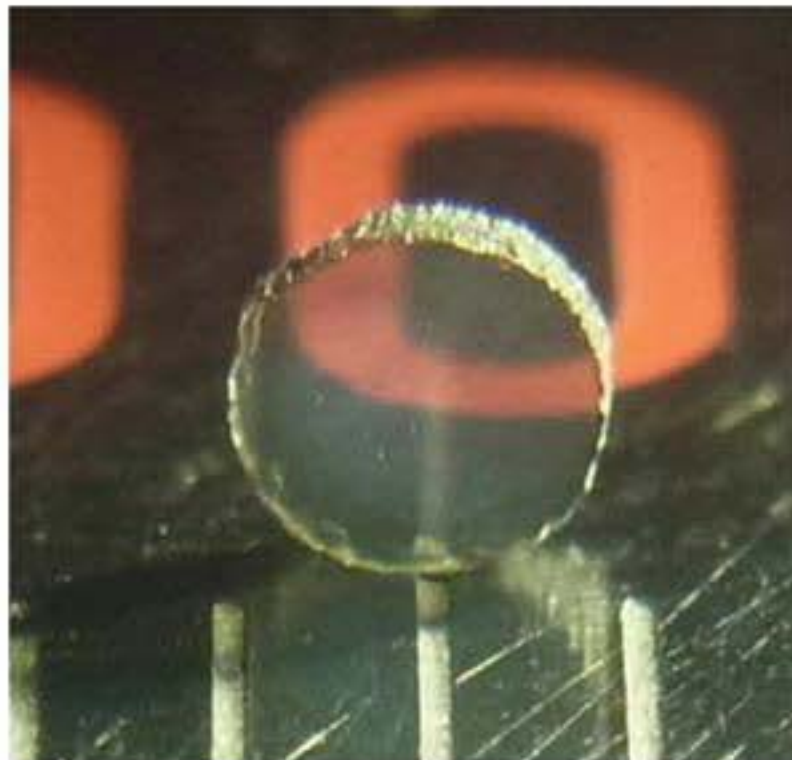
Computation based

Functionality



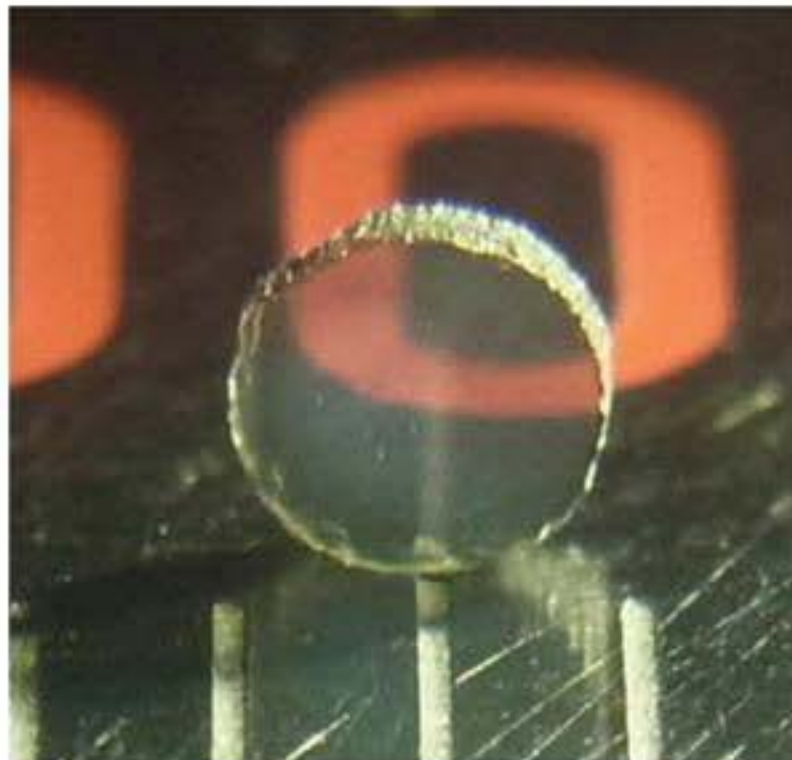
Scatterers

1. **Single element metasurface optics**
2. **Towards metasurface optical systems**
3. **Inverse design and optimization of metasurfaces**
4. **Future work and outlook**



Nishiyama et al. Sci. Reports. **7**,
44755 (2017)

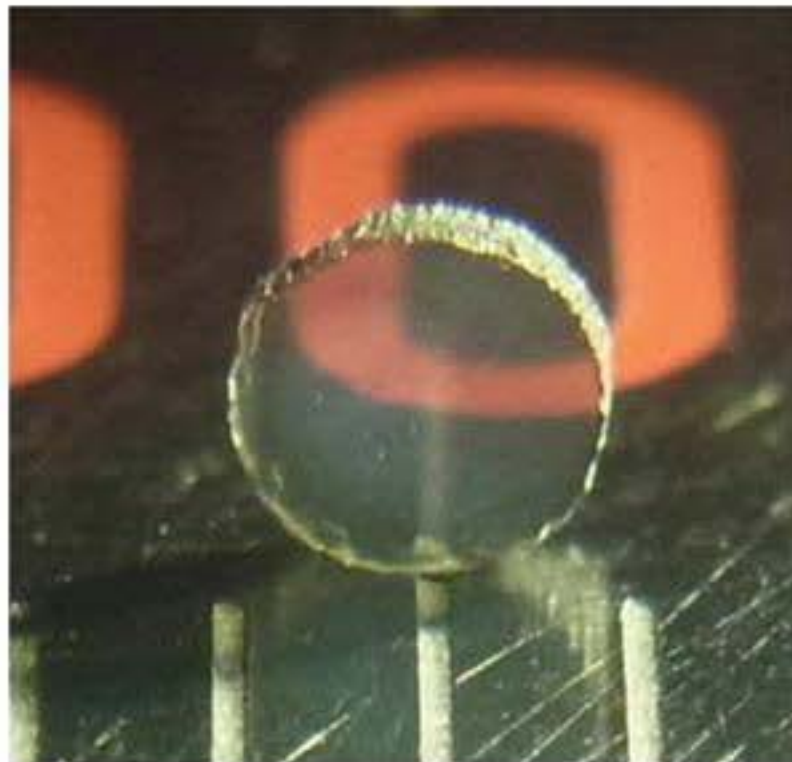
Refractive index ~ 2



Nishiyama et al. Sci. Reports. **7**,
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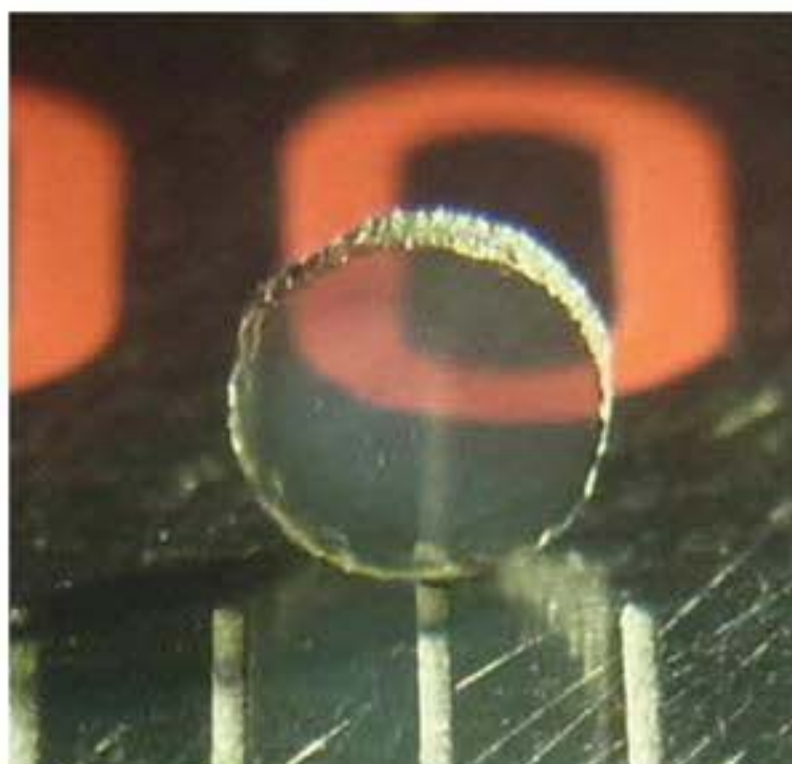
Band gap $\sim 4\text{-}5\text{ eV}$



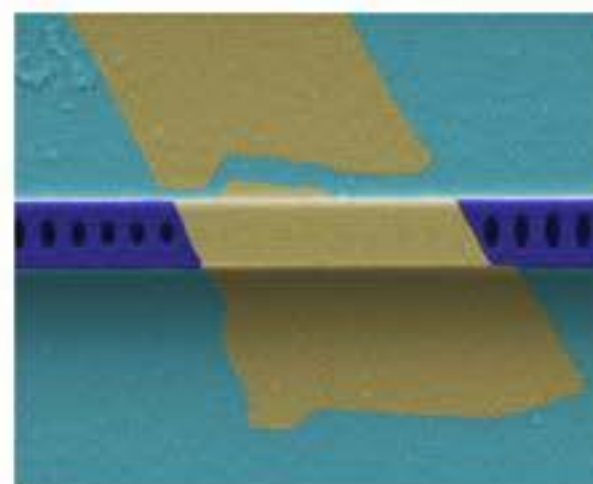
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Refractive index ~ 2

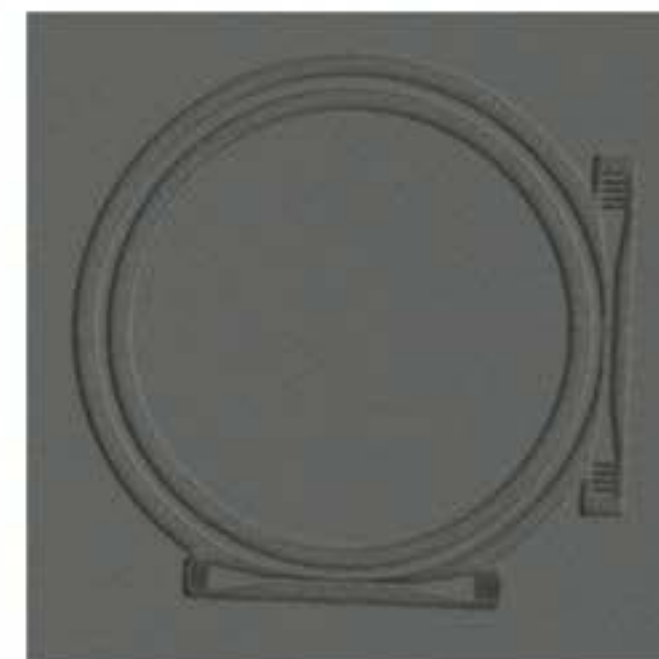
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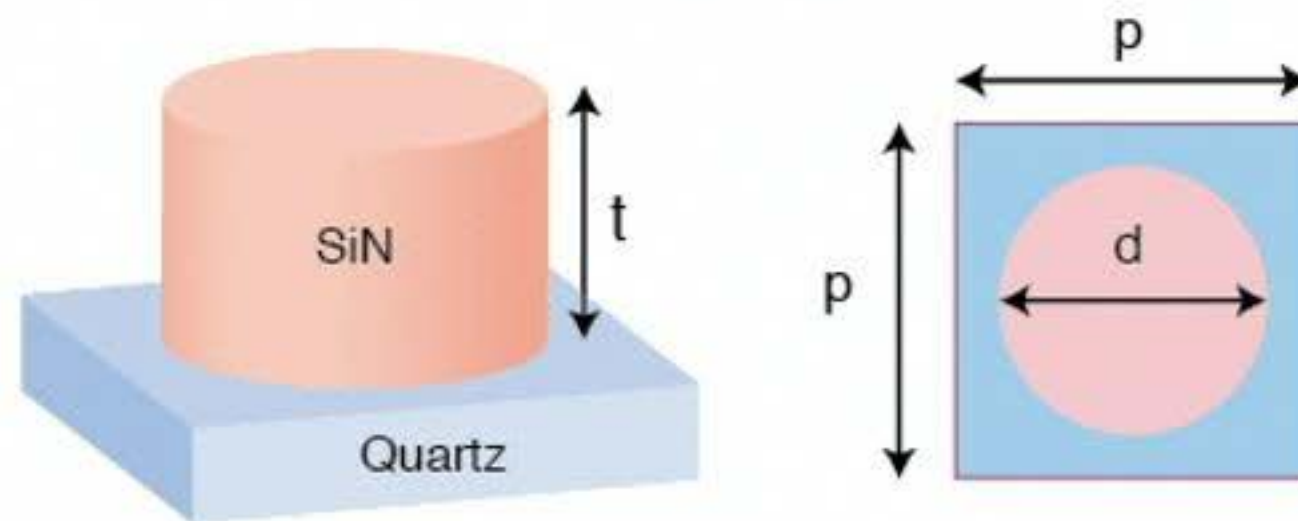
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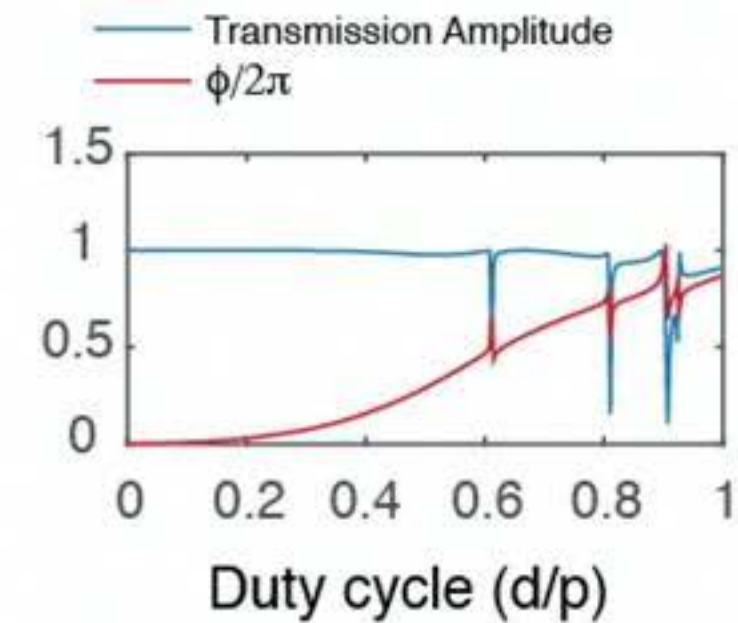
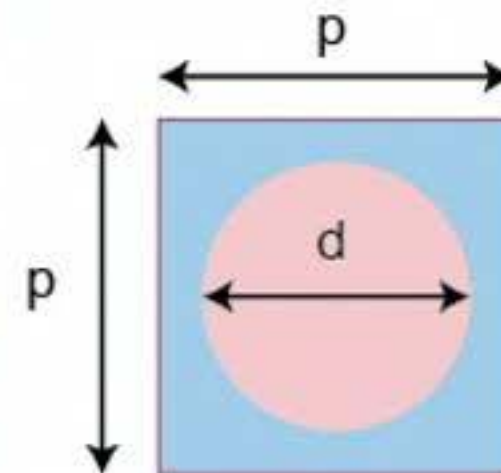
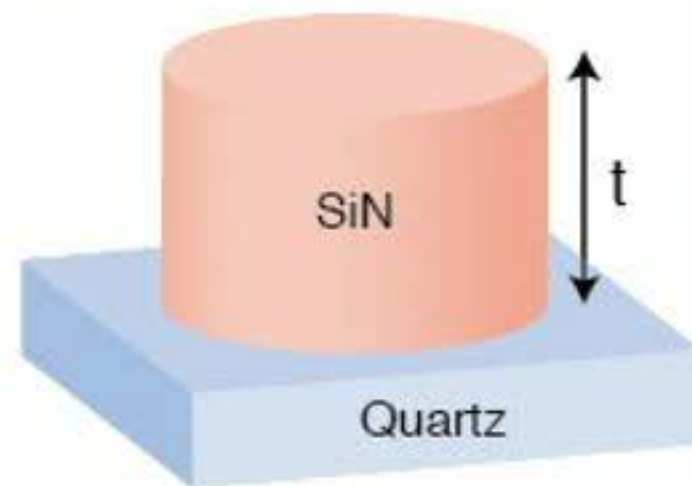
Fryett et al. ACS Photonics
(2018)



Rigorous Coupled Wave Analysis (RCWA)



Rigorous Coupled Wave Analysis (RCWA)



Implementing the phase profile

17

Implementing the phase profile

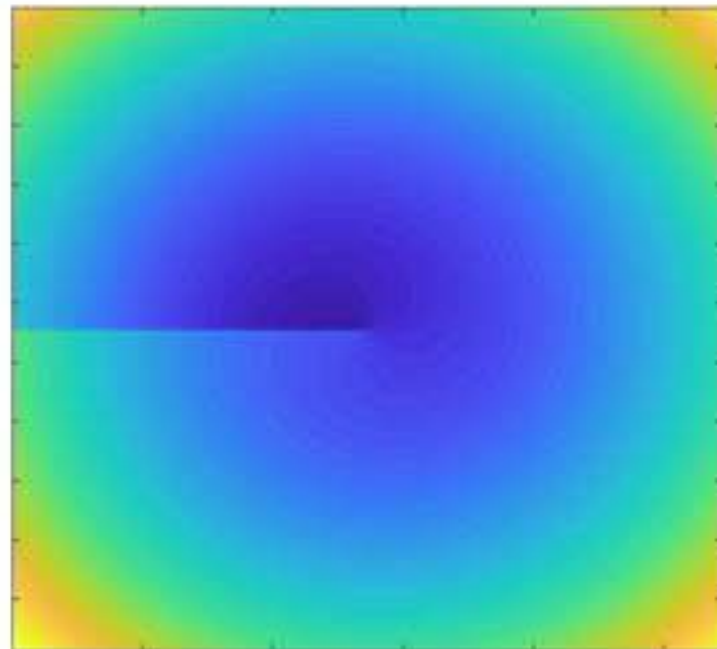
17

$$\varphi(r, \theta) = \frac{2\pi}{\lambda} \left(\sqrt{r^2 + f^2} - f \right) + l\theta$$

Implementing the phase profile

17

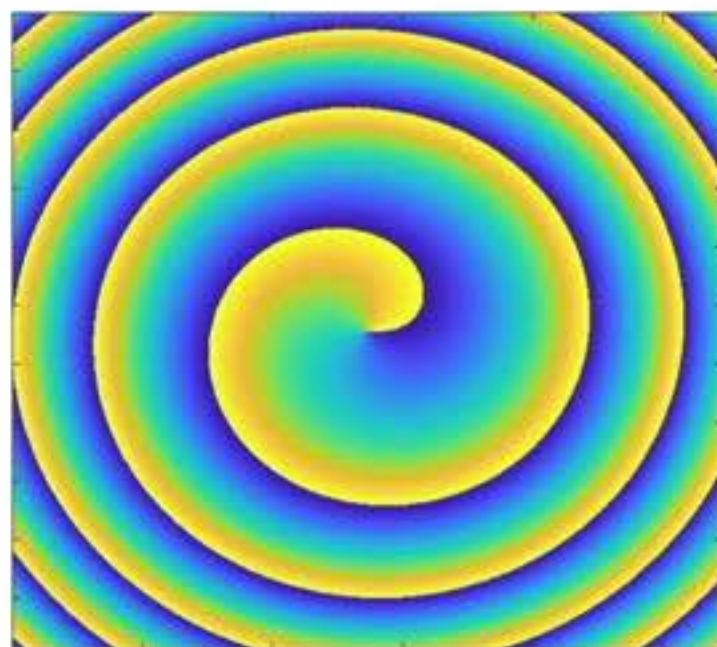
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Implementing the phase profile

18

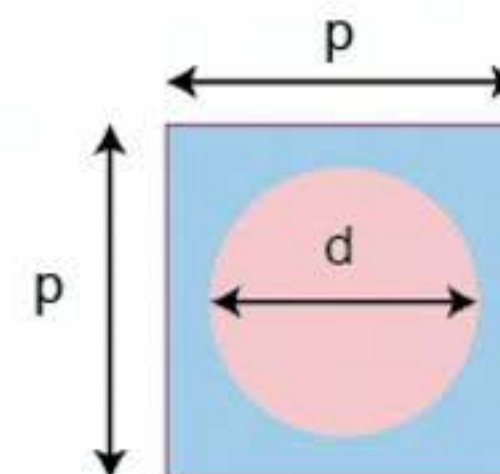
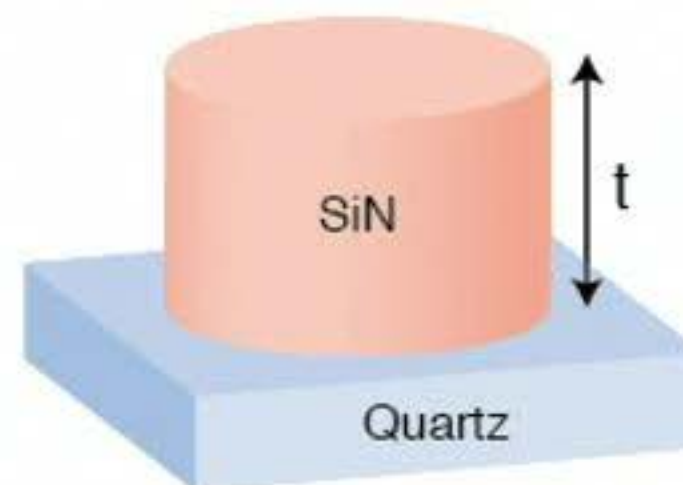
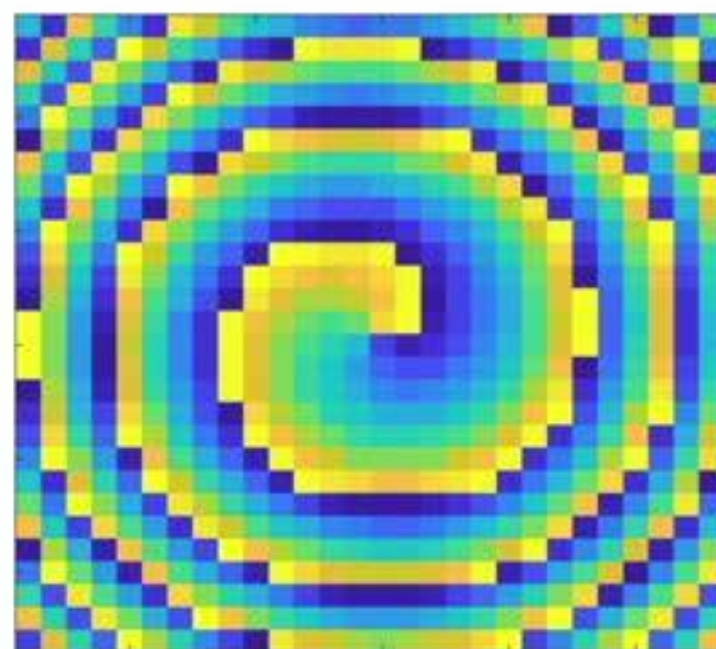
$$\varphi(r, \theta) = \text{mod} \left(\frac{2\pi}{\lambda} \left(\sqrt{r^2 + f^2} - f \right) + l\theta, 2\pi \right)$$



Implementing the phase profile

19

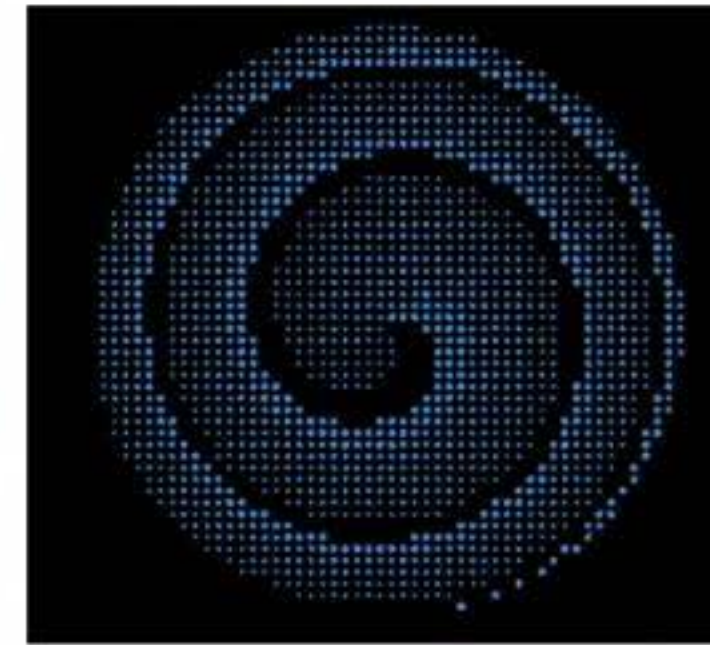
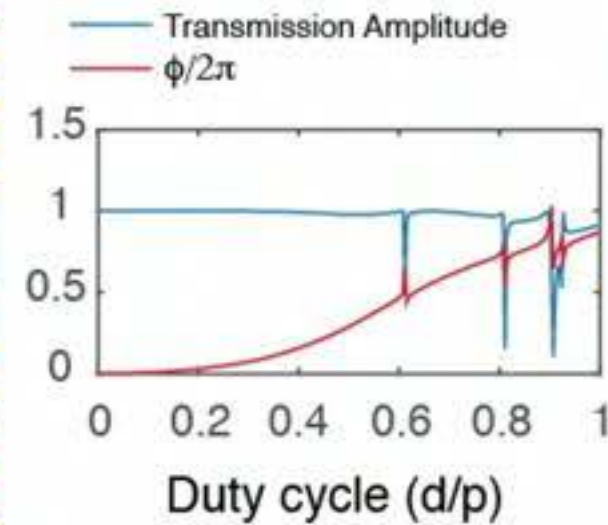
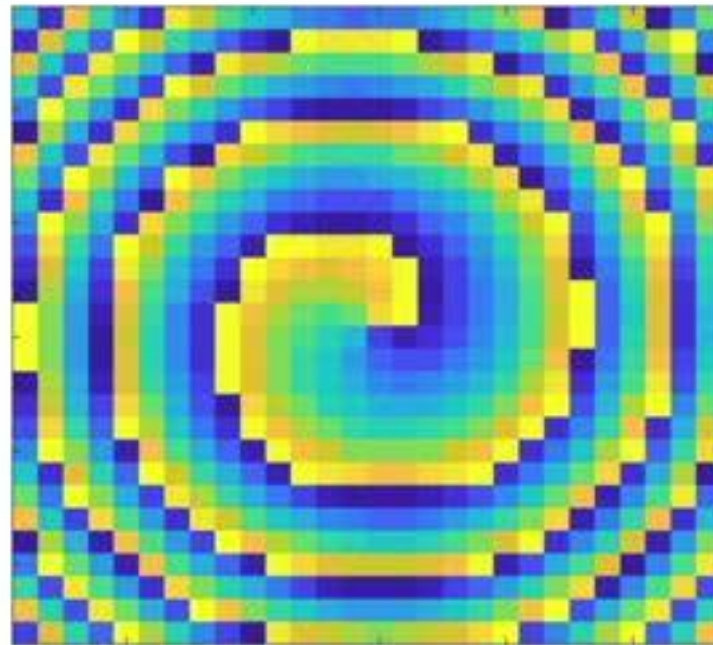
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Implementing the phase profile

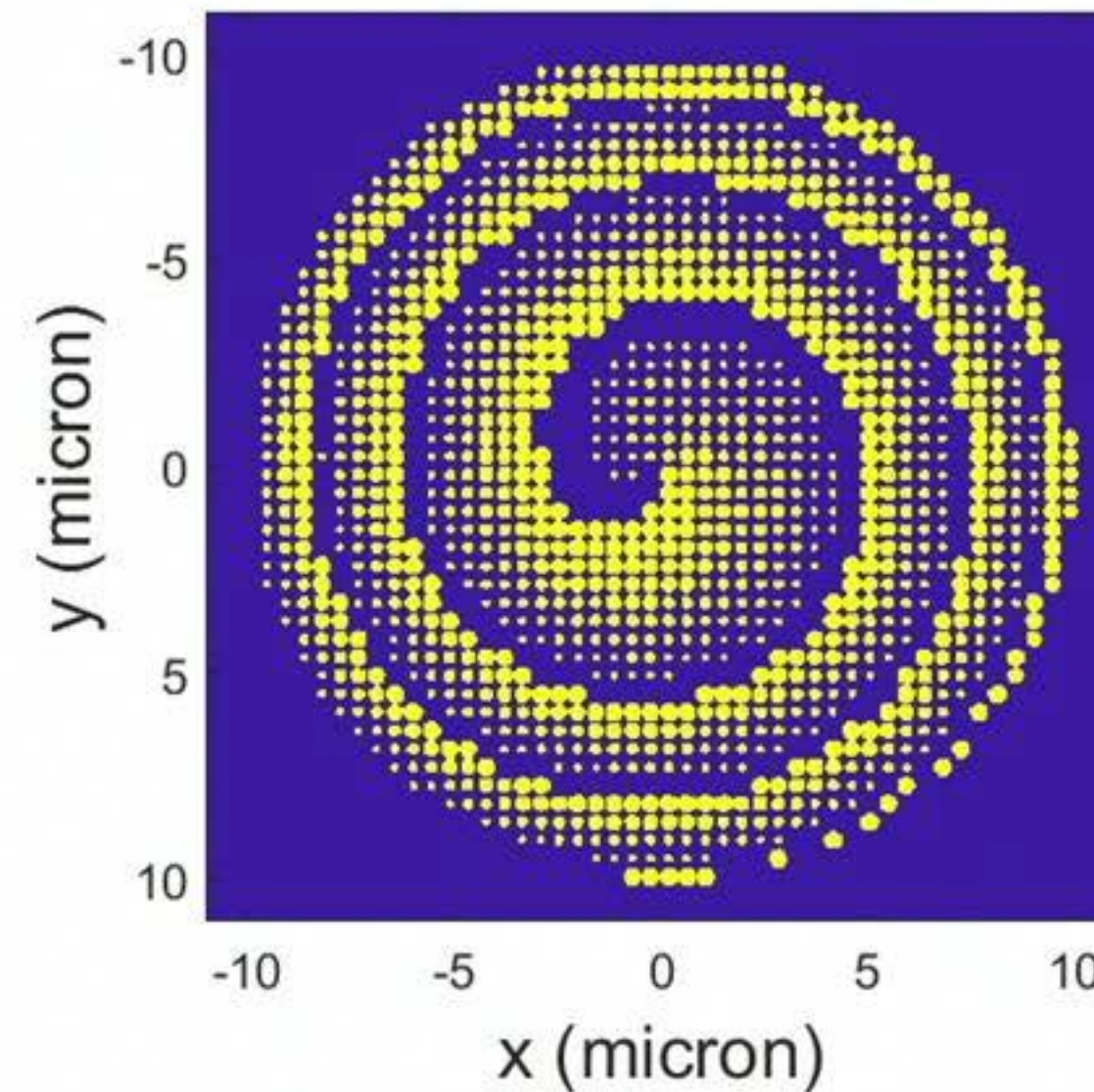
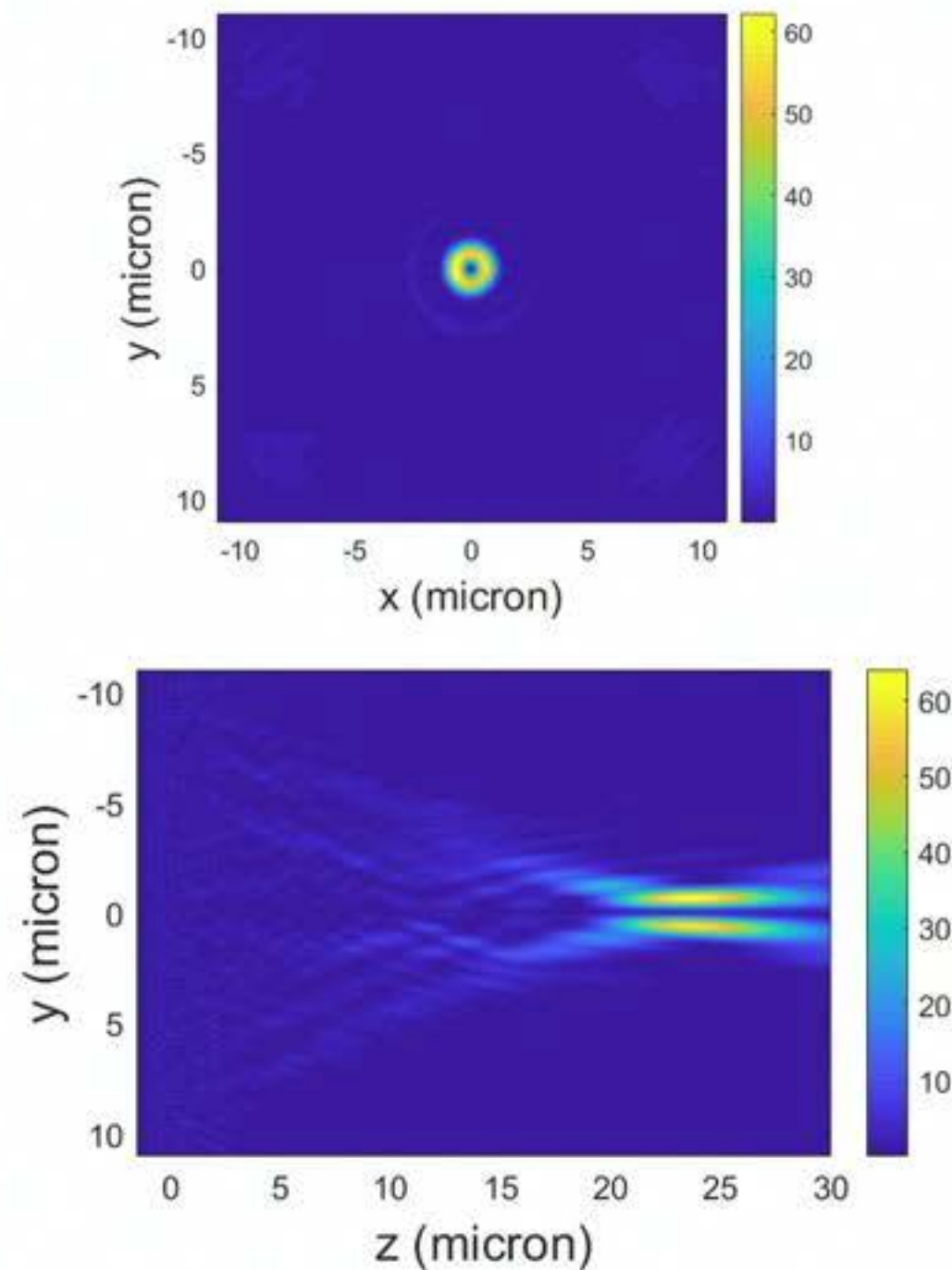
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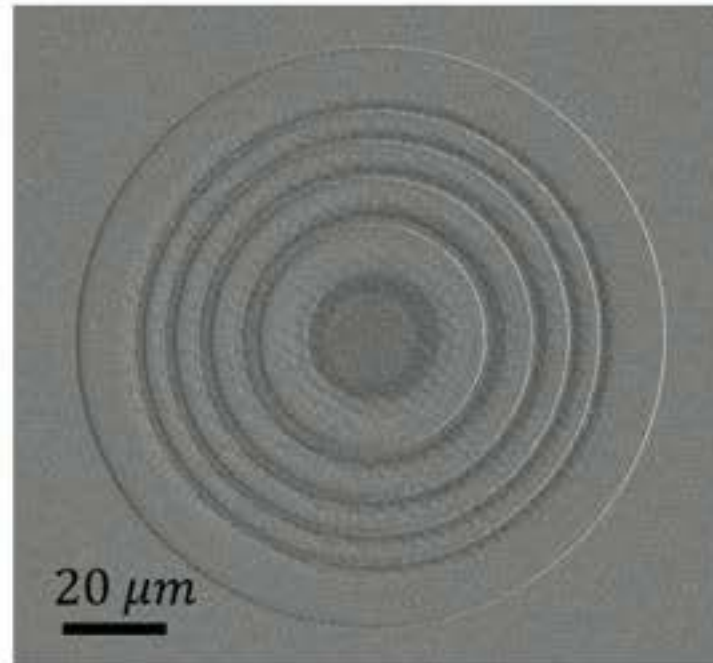
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Finite difference time domain simulation

21

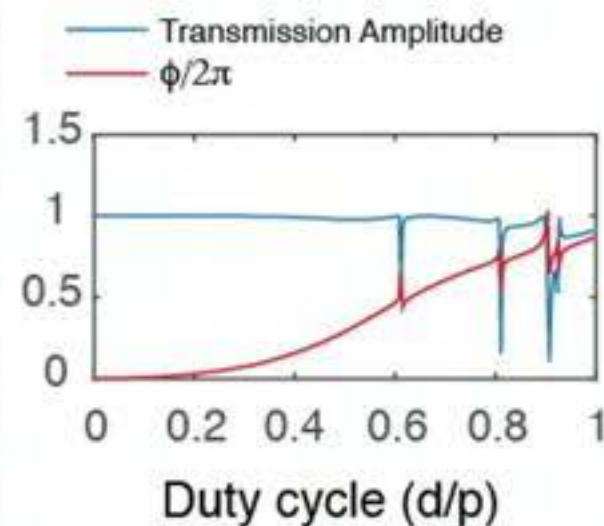
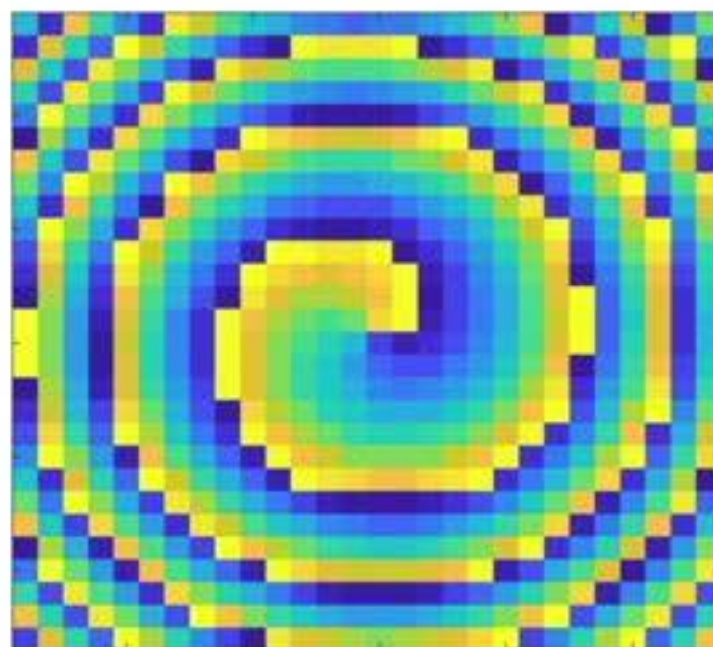




Implementing the phase profile

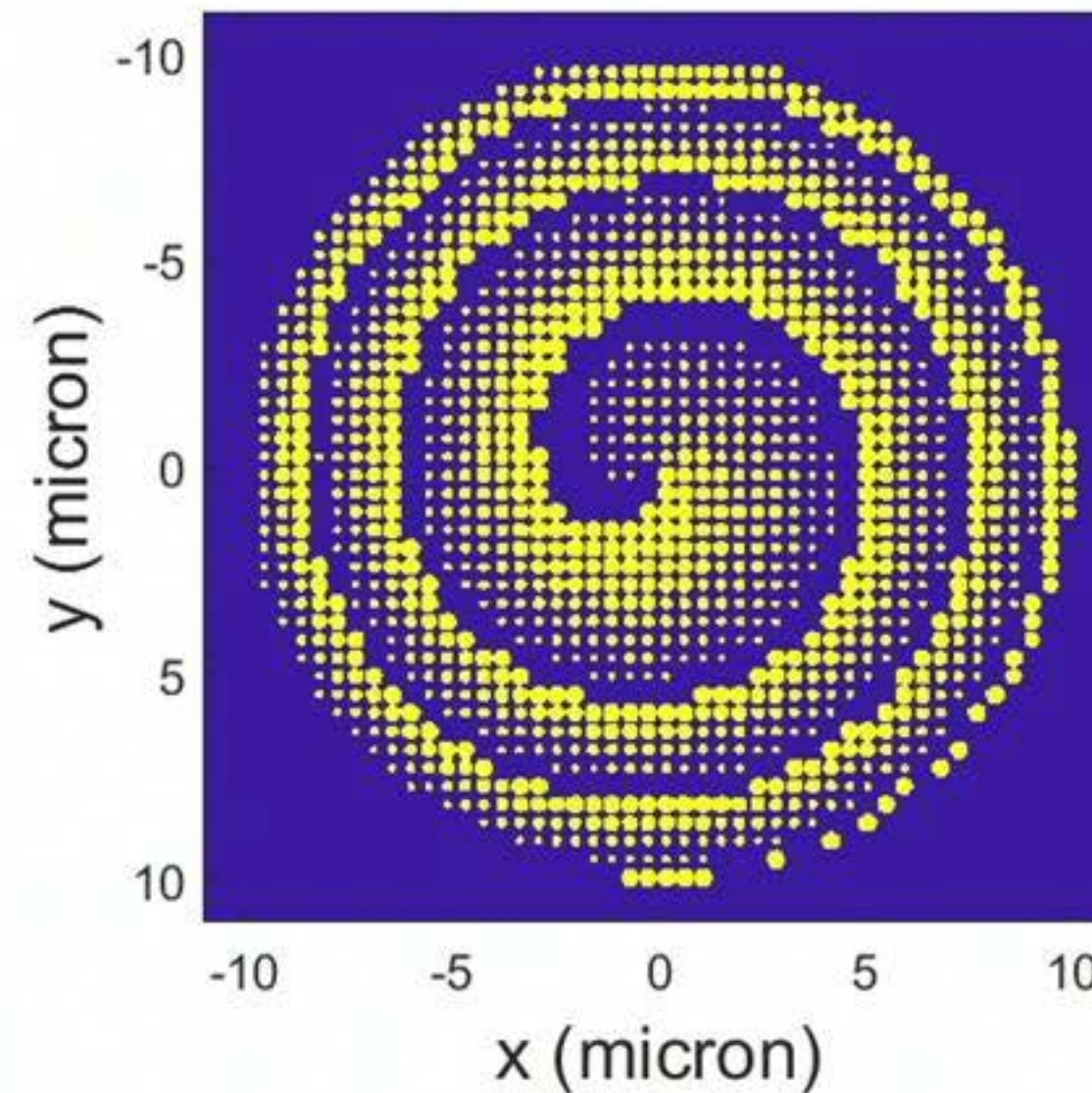
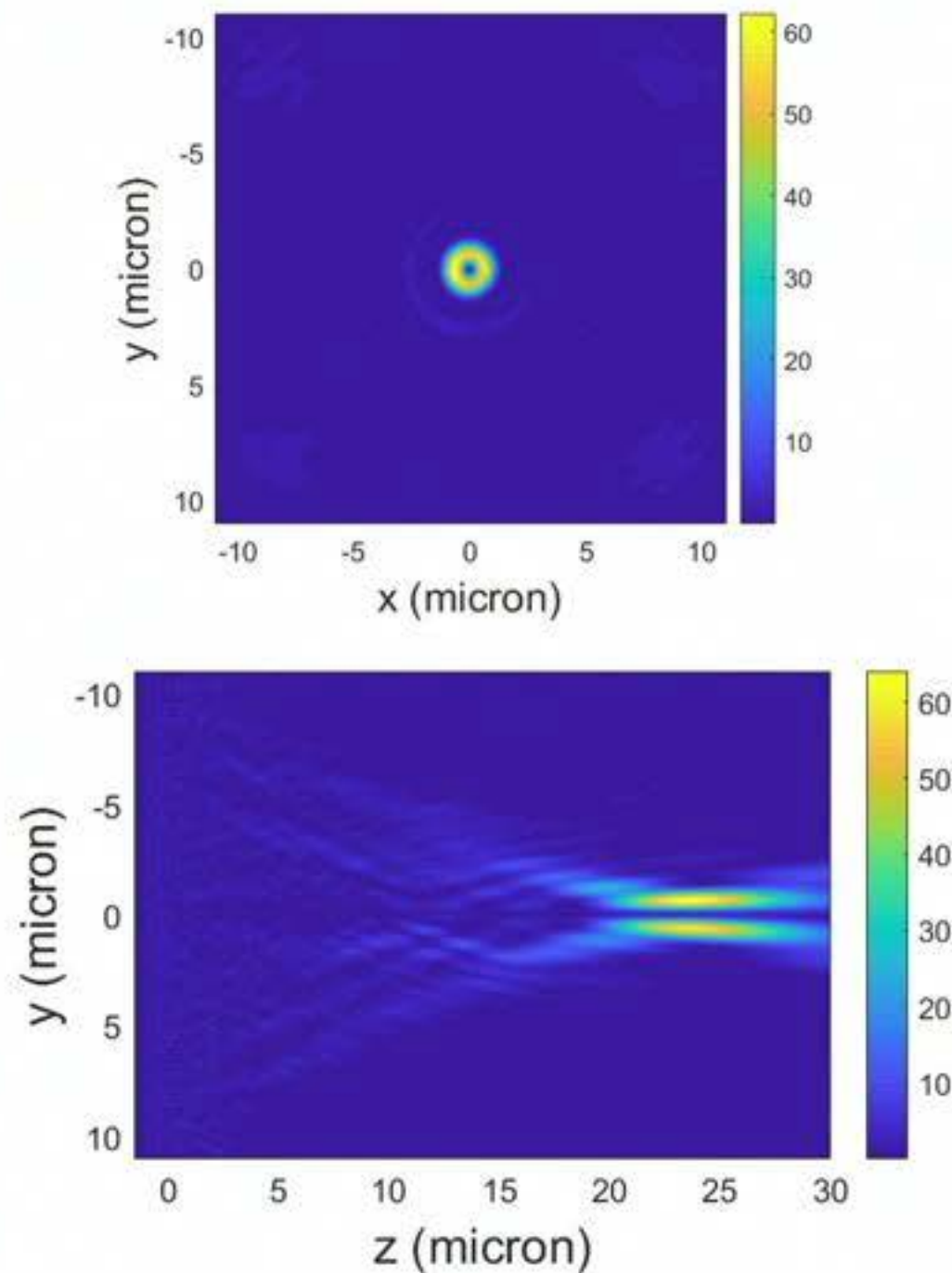
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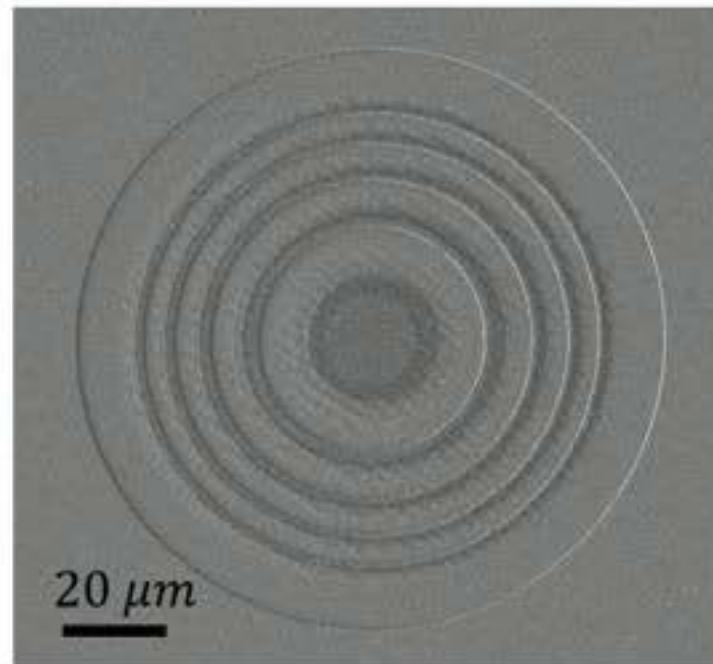
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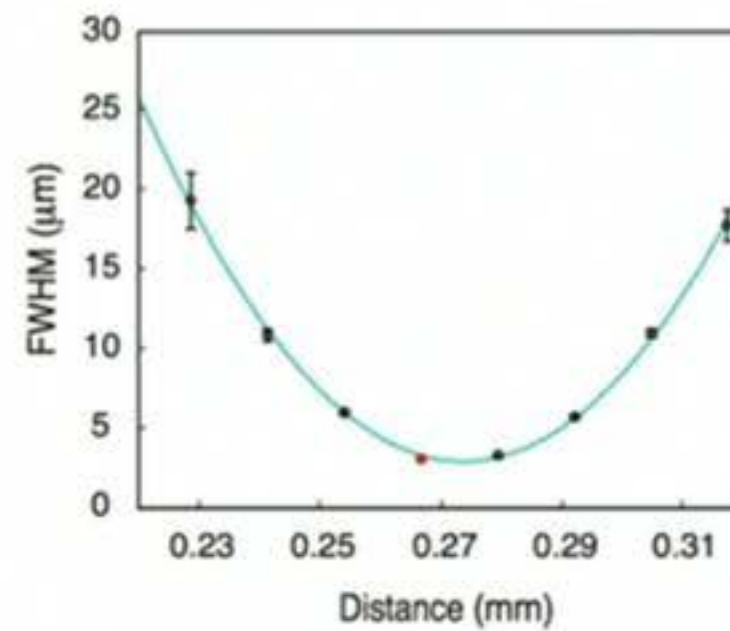
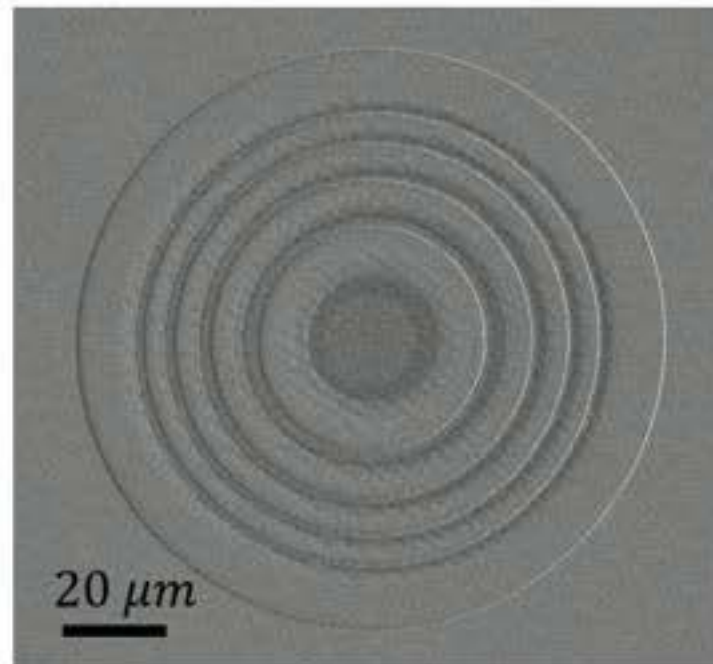


Finite difference time domain simulation

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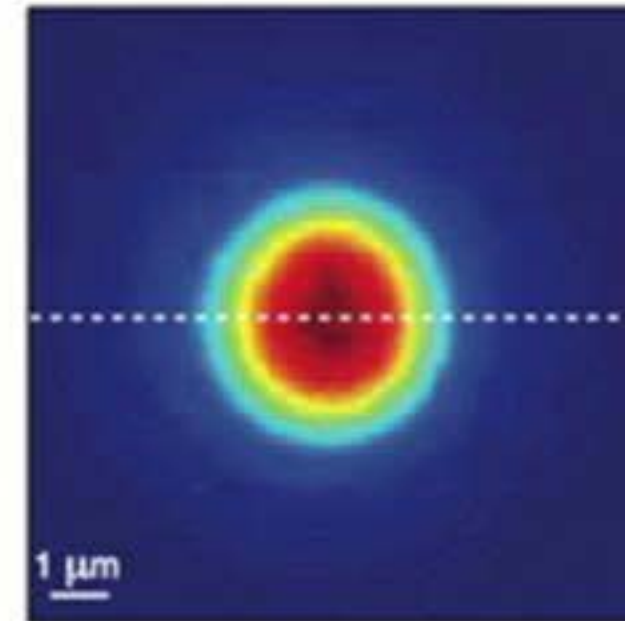
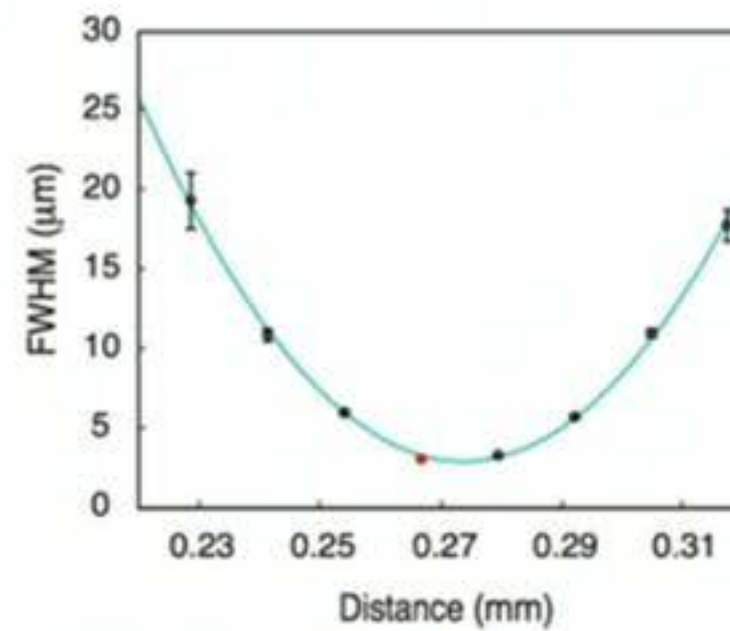
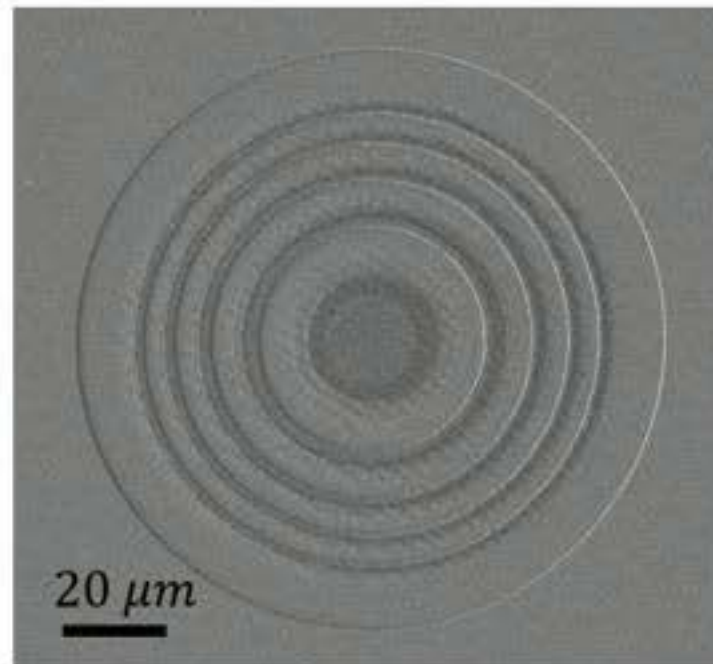






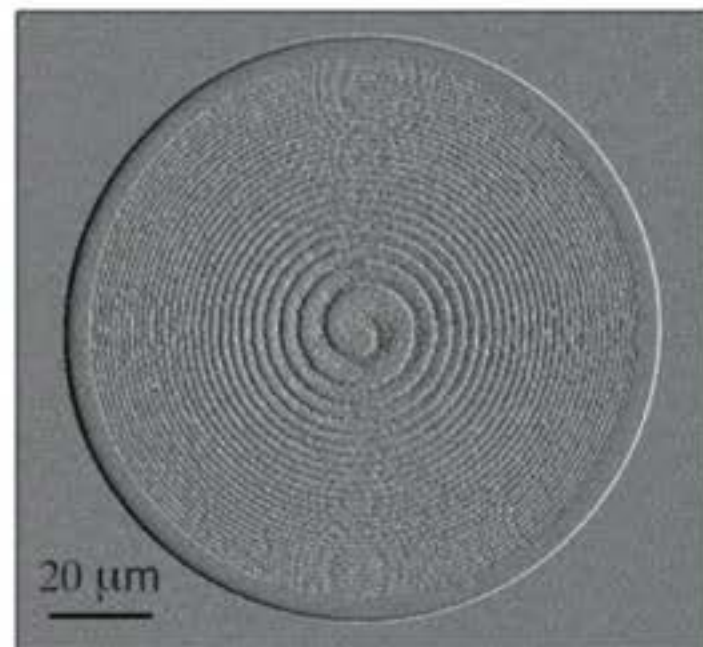
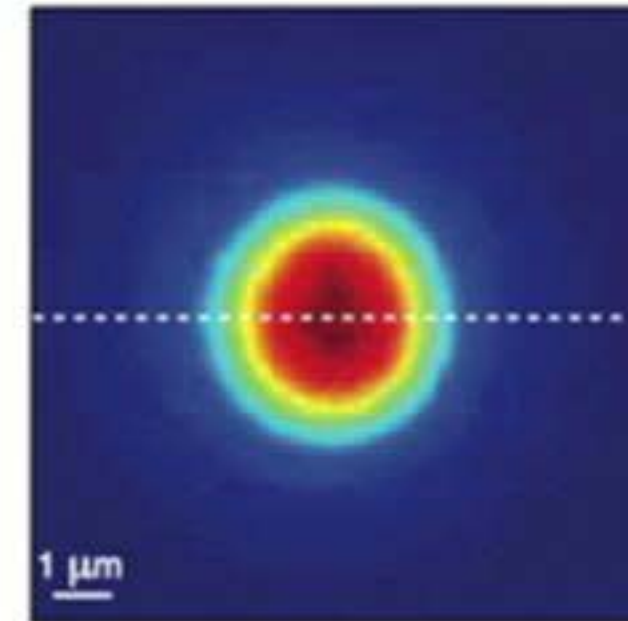
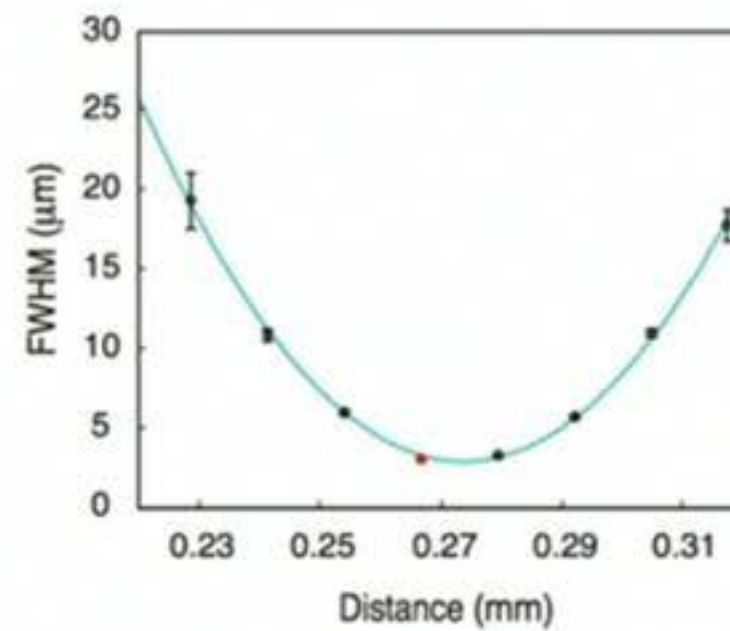
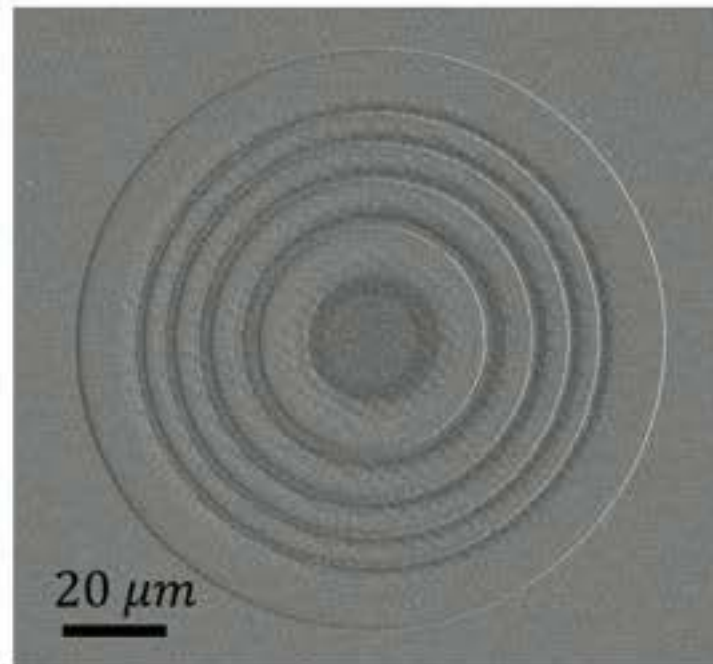
Fabricated structure

22



Fabricated structure

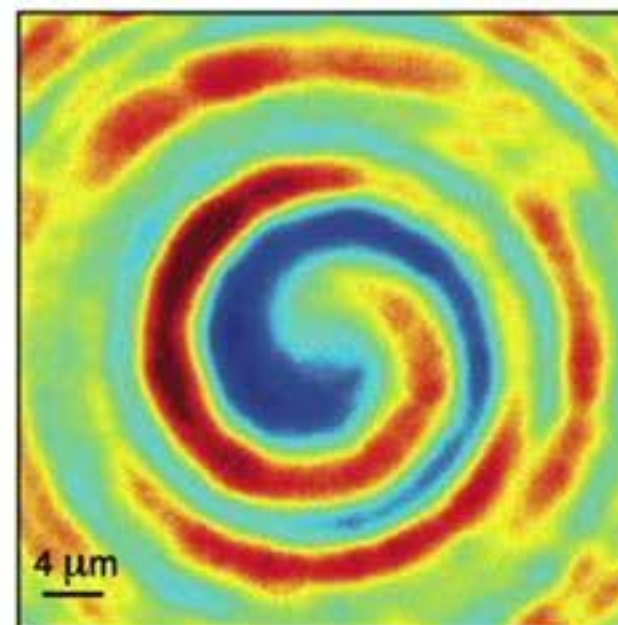
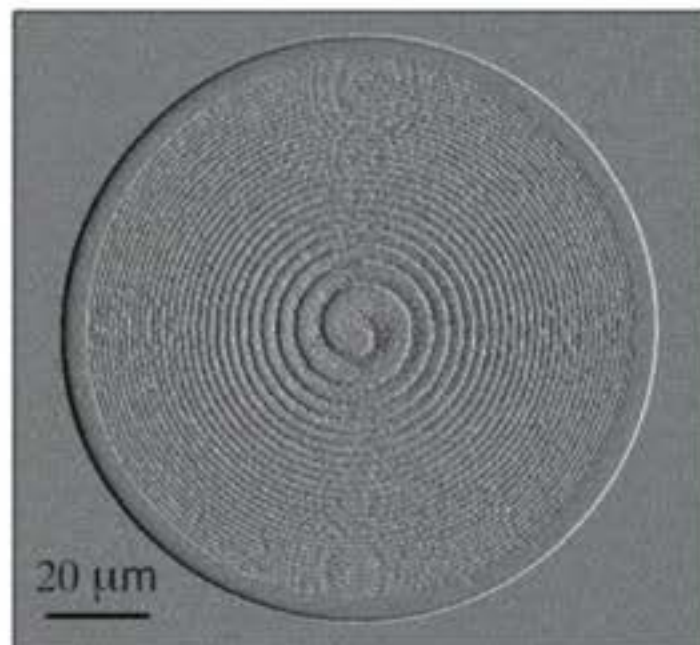
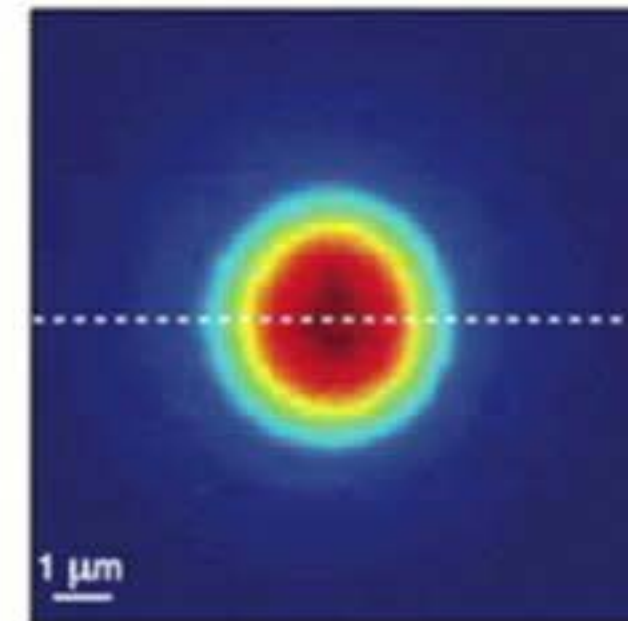
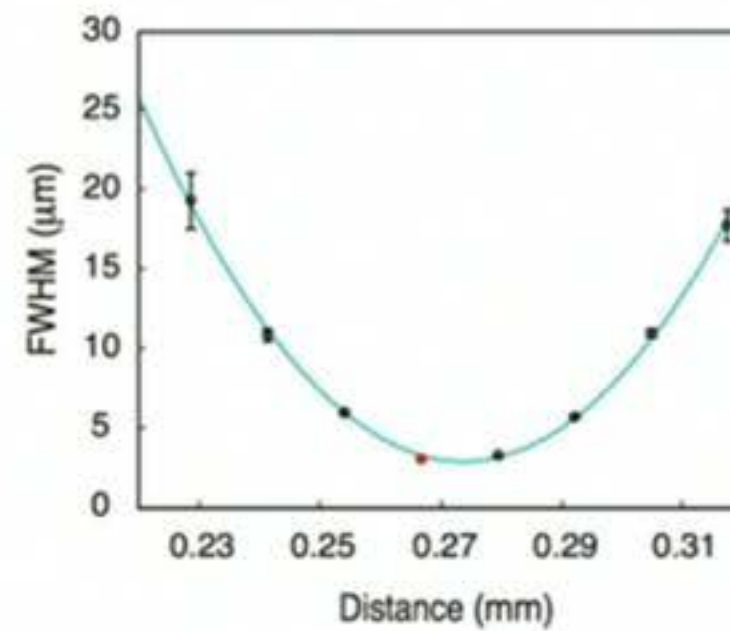
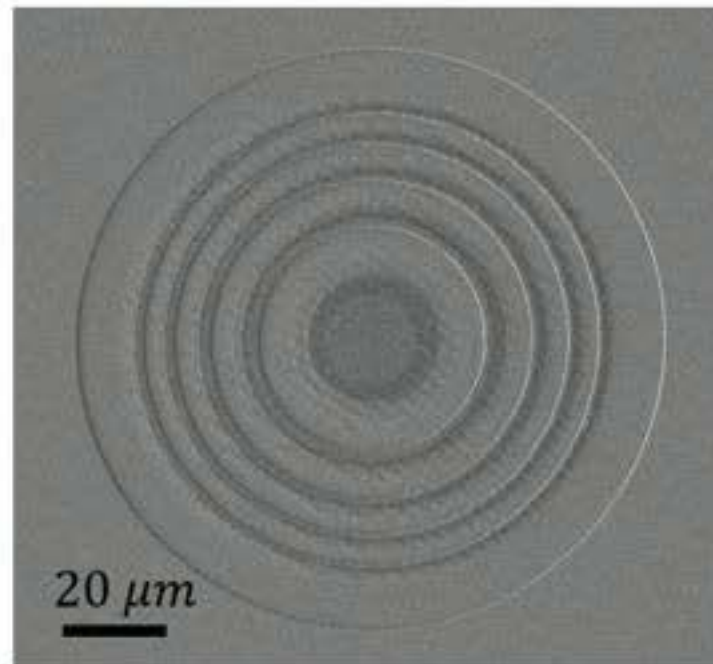
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A. Zhan et al, ACS Photonics. **3**, 2 (2016)

Fabricated structure

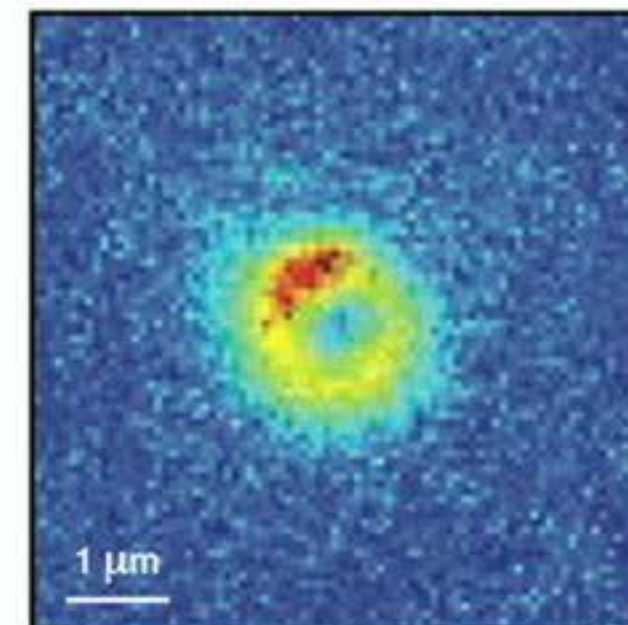
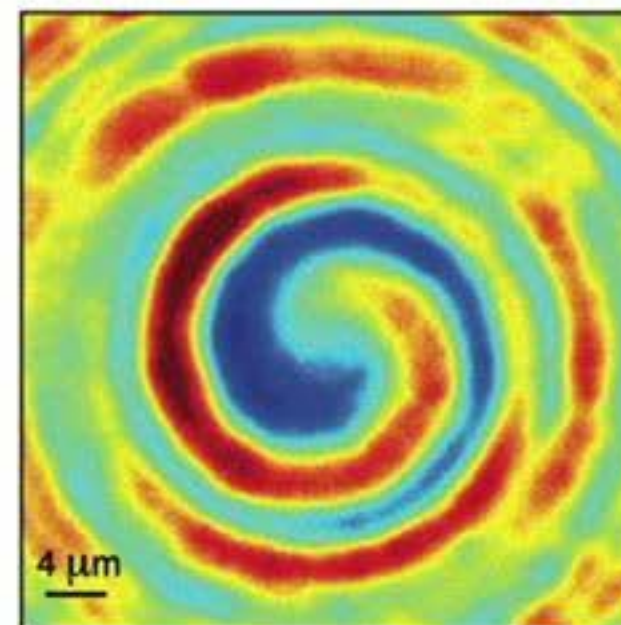
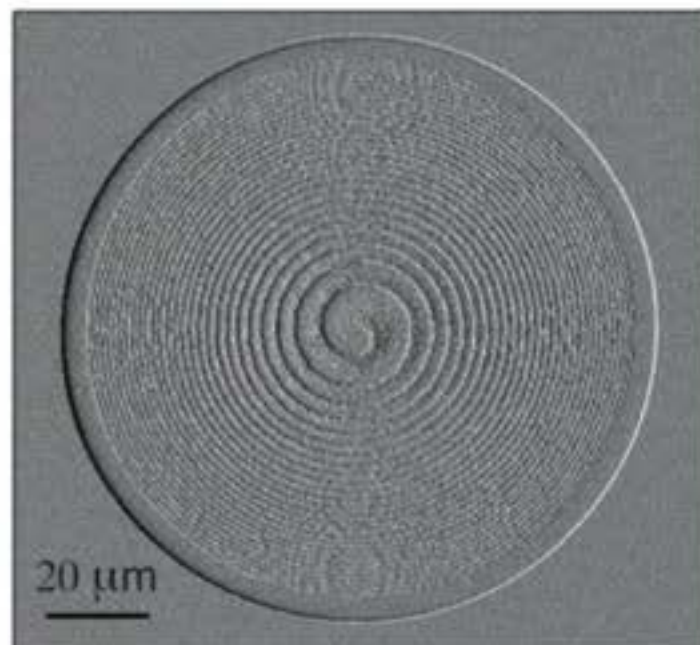
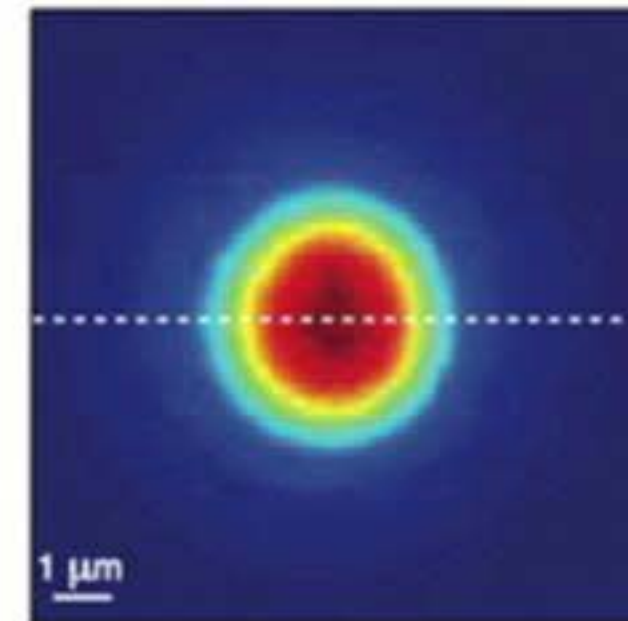
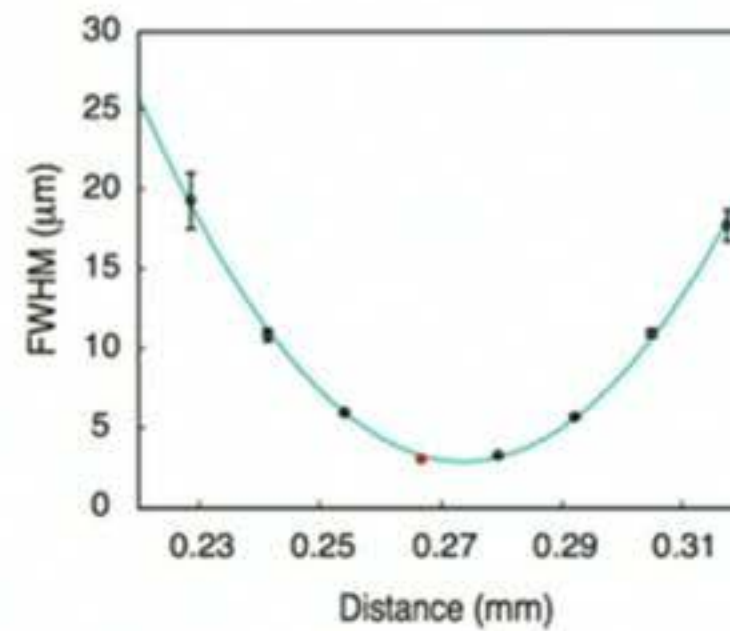
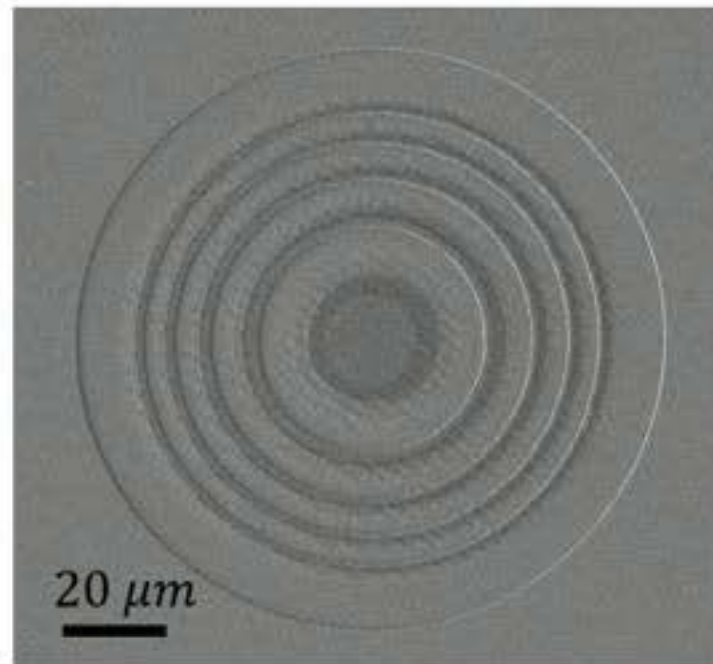
22



A. Zhan et al, ACS Photonics. **3**, 2 (2016)

Fabricated structure

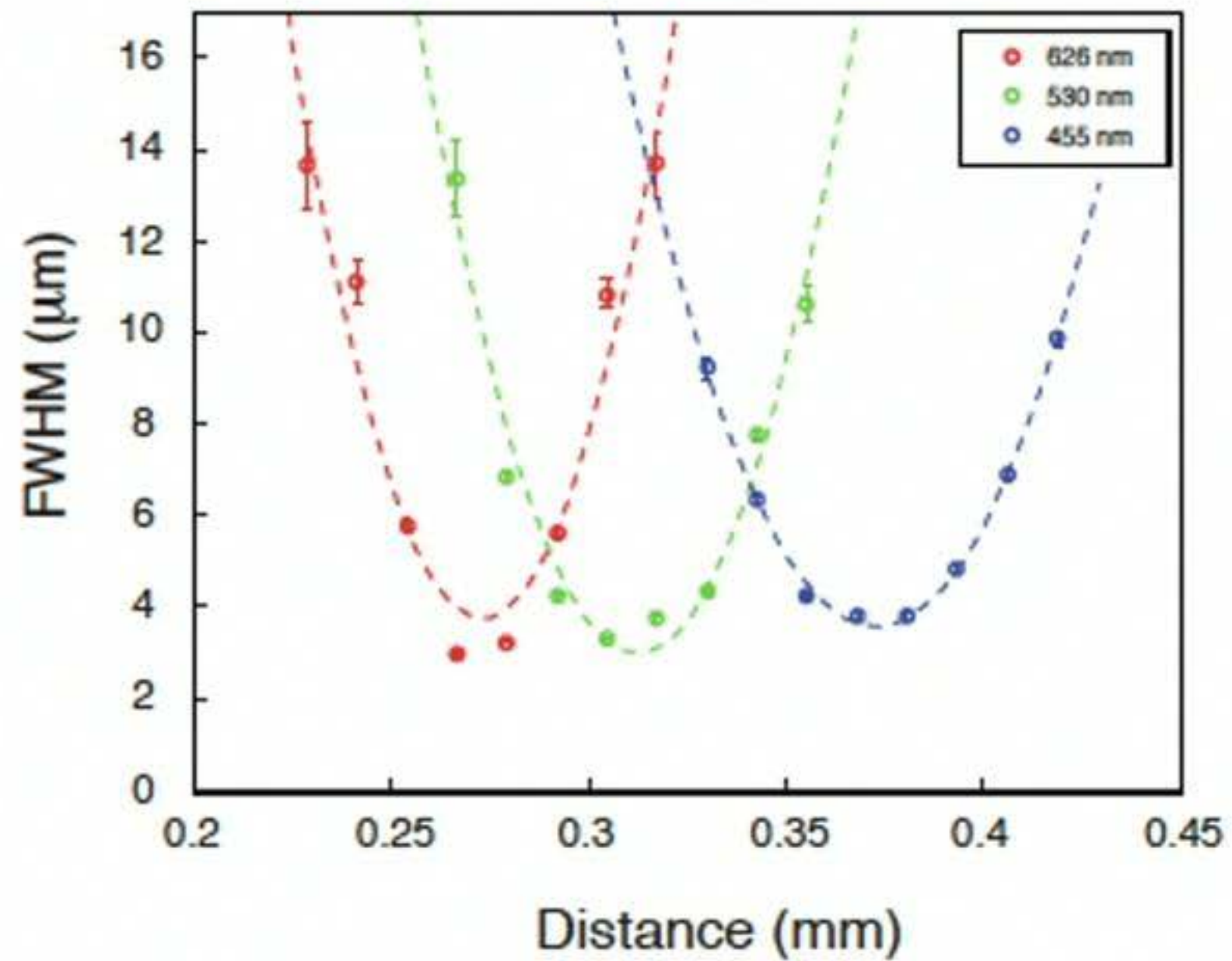
22



A. Zhan et al, ACS Photonics. **3**, 2 (2016)

Chromatic aberration

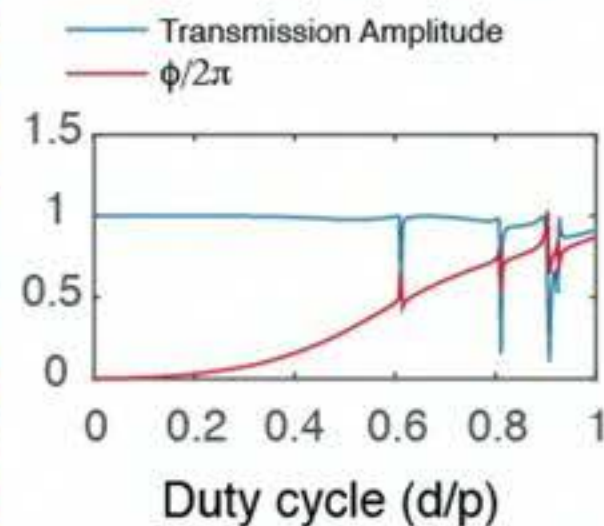
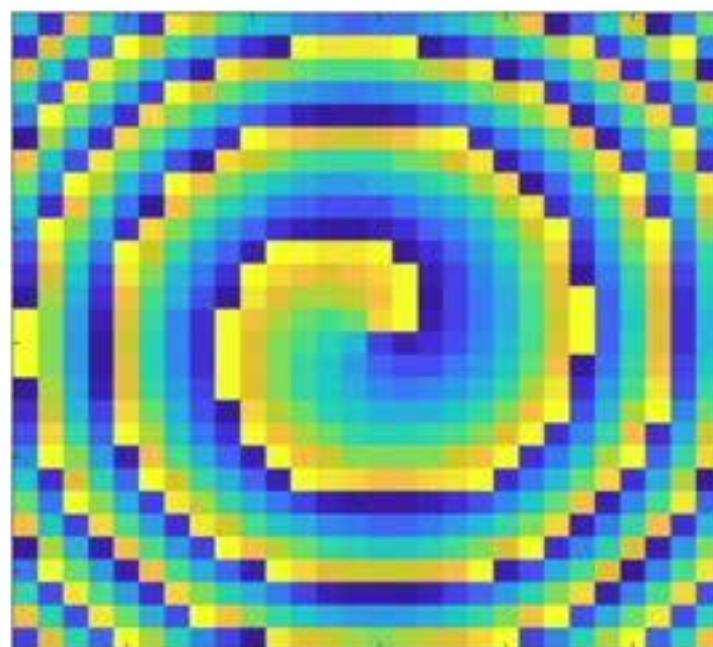
23



Implementing the phase profile

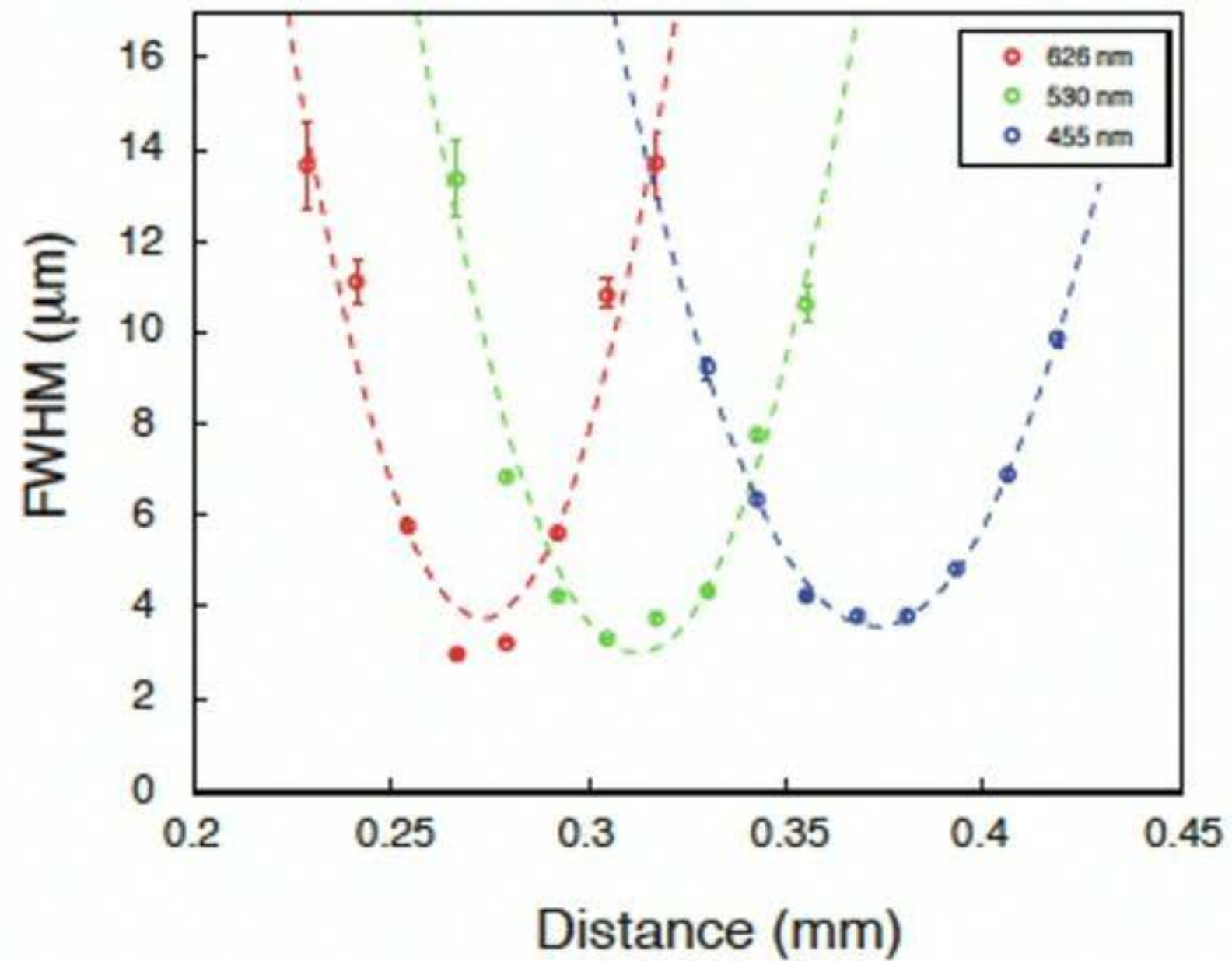
20

$$\varphi(r, \theta) = \text{mod} \left(\frac{2\pi}{\lambda} \left(\sqrt{r^2 + f^2} - f \right) + l\theta, 2\pi \right)$$



Chromatic aberration

23



Chromatic aberration in photography

24



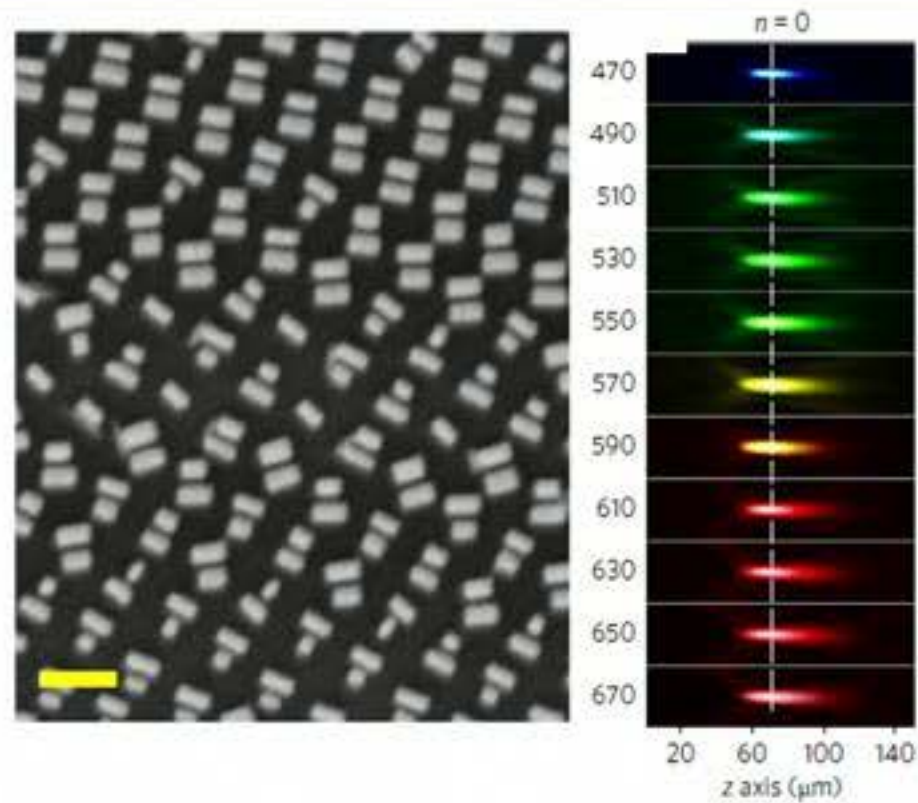
Stan Zurek [CC BY-SA 3.0 (<http://creativecommons.org/licenses/by-sa/3.0/>)]

Correcting chromatic aberrations

25

Correcting chromatic aberrations

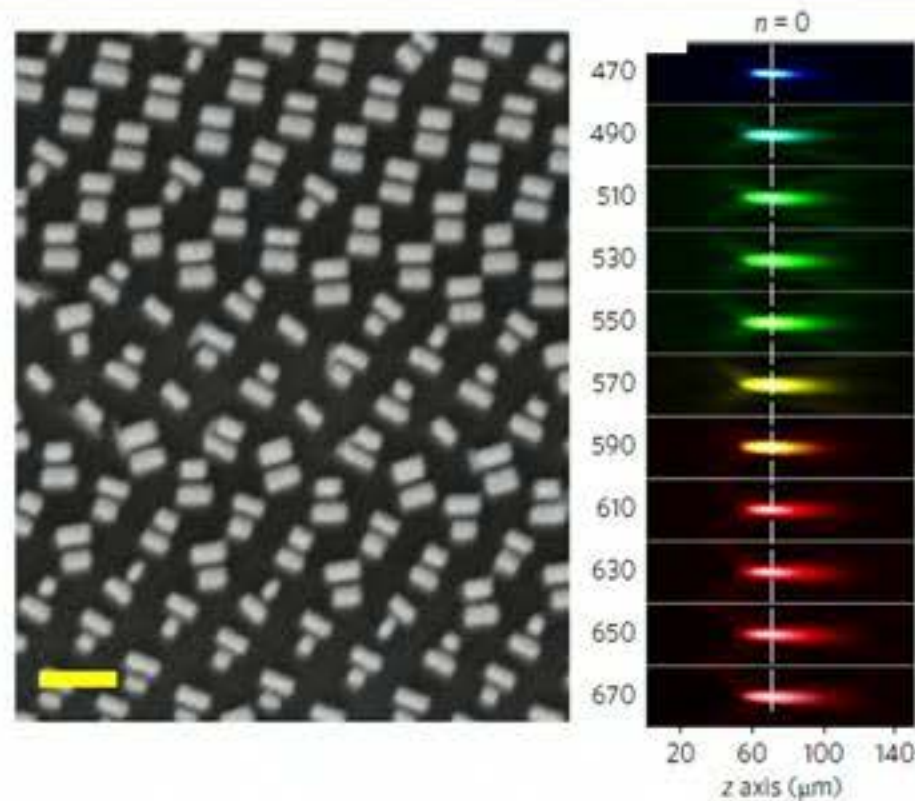
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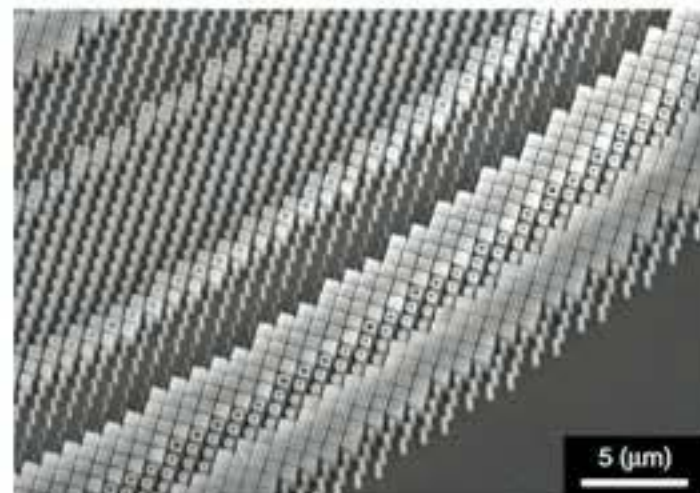
W. Chen et al, Nat. Nano. **13**, 220 (2018)

Correcting chromatic aberrations

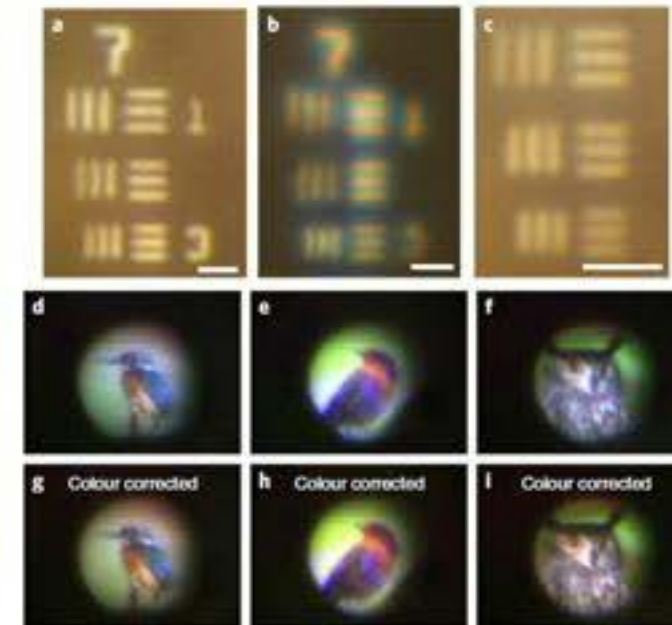
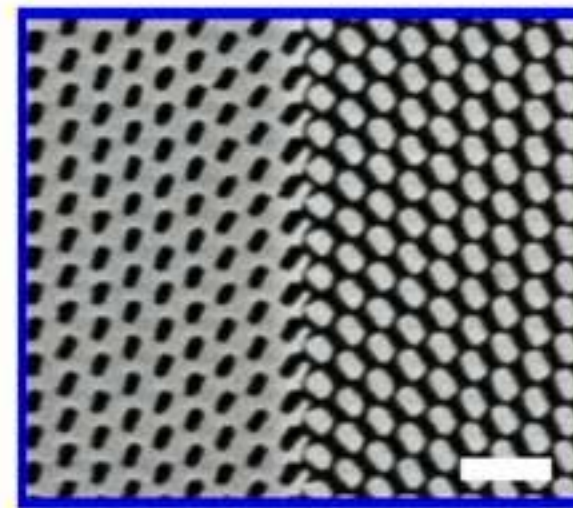
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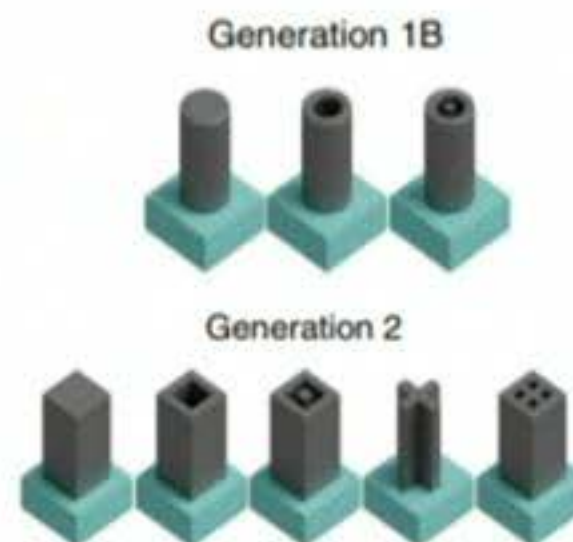
W. Chen et al, Nat. Nano. **13**, 220 (2018)



Shrestha et al. Light: Sci. and Appl. **7**, 95 (2018)



S. Wang et al, Nat. Nano. **13**, 227 (2018)

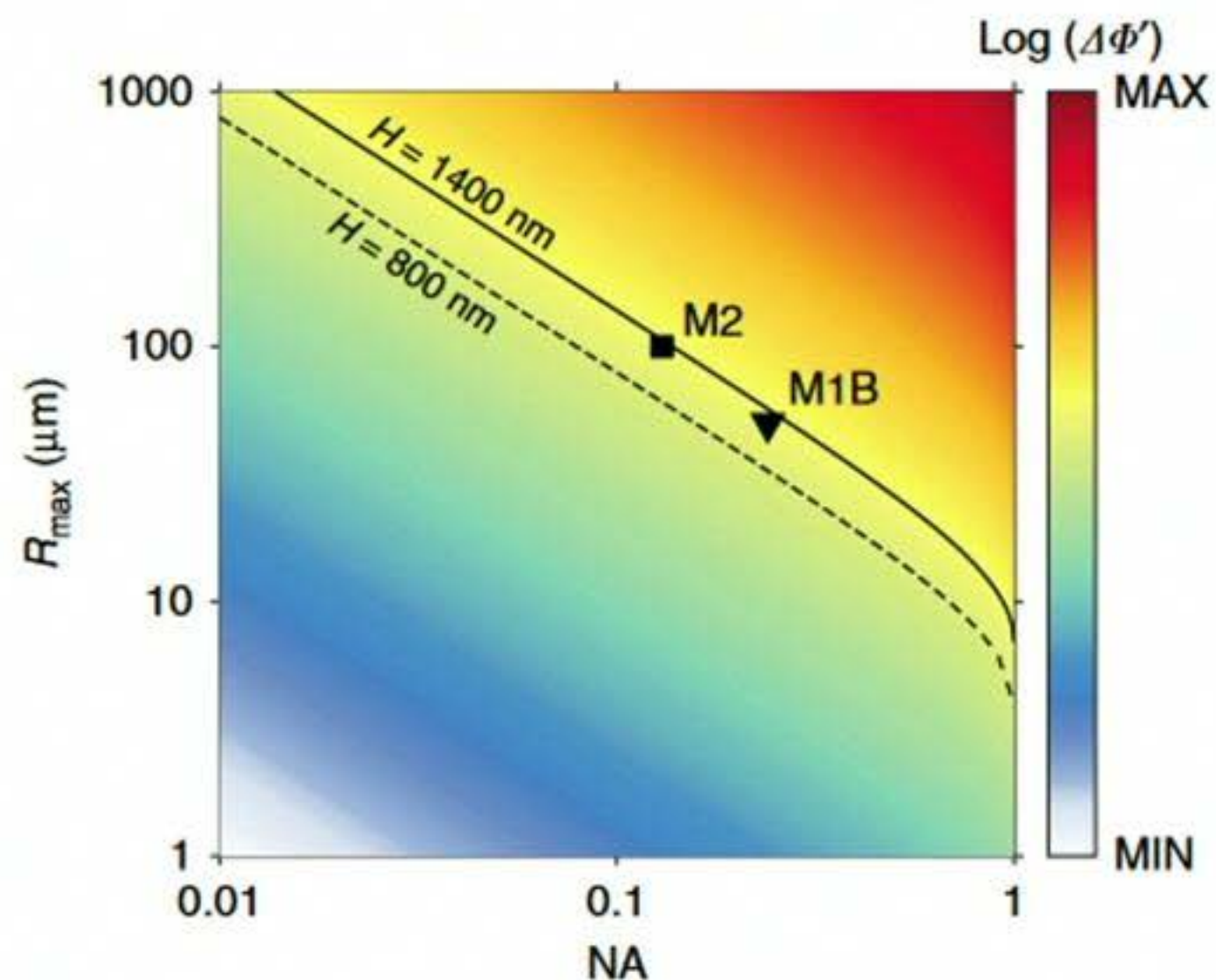


Limits of dispersion engineering

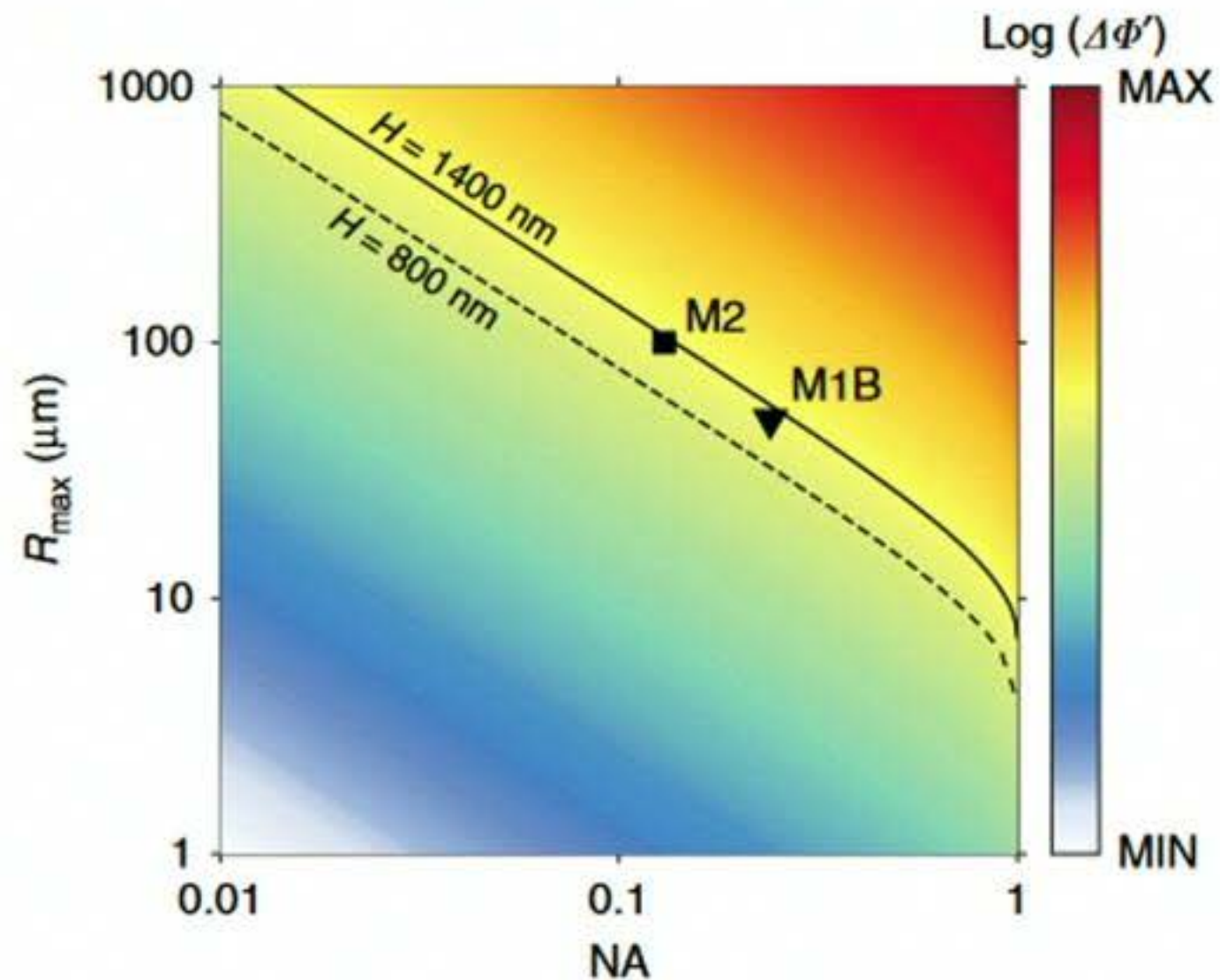
26

Limits of dispersion engineering

26



Shrestha et al. Light: Sci. and Appl.
7, 95 (2018)



$$R_{\max} = \frac{\Delta\Phi'}{\Delta\omega \left(\frac{1}{NA} - \sqrt{\frac{1}{NA^2} - 1} \right)}$$

Shrestha et al. Light: Sci. and Appl.
7, 95 (2018)

Computational imaging approach

27

$$\varphi = \frac{2\pi}{\lambda} (\sqrt{x^2 + y^2 + f^2} - f) + \frac{\alpha}{L^3} (x^3 + y^3)$$

Computational imaging approach

27

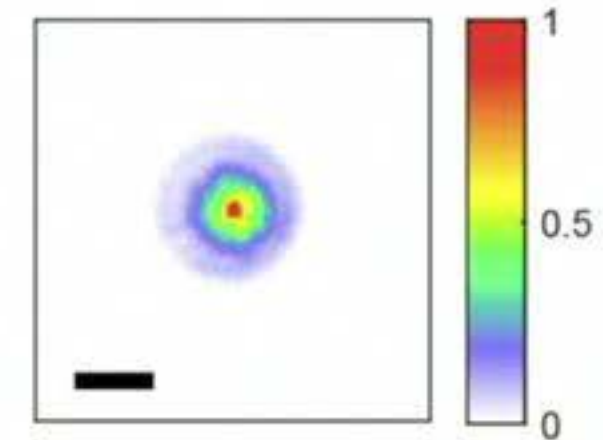
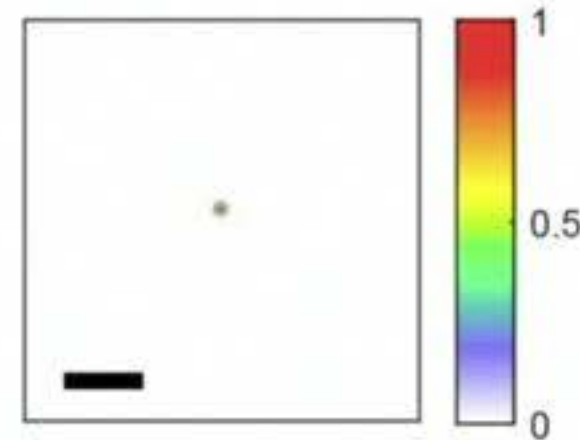
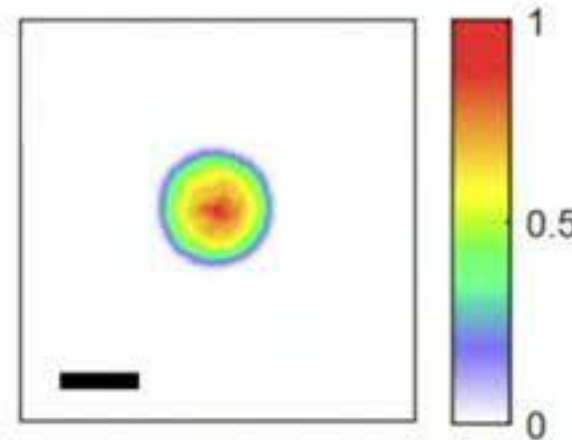
$$\varphi = \frac{2\pi}{\lambda} (\sqrt{x^2 + y^2 + f^2} - f) + \frac{\alpha}{L^3} (x^3 + y^3)$$

Blue

Green

Red

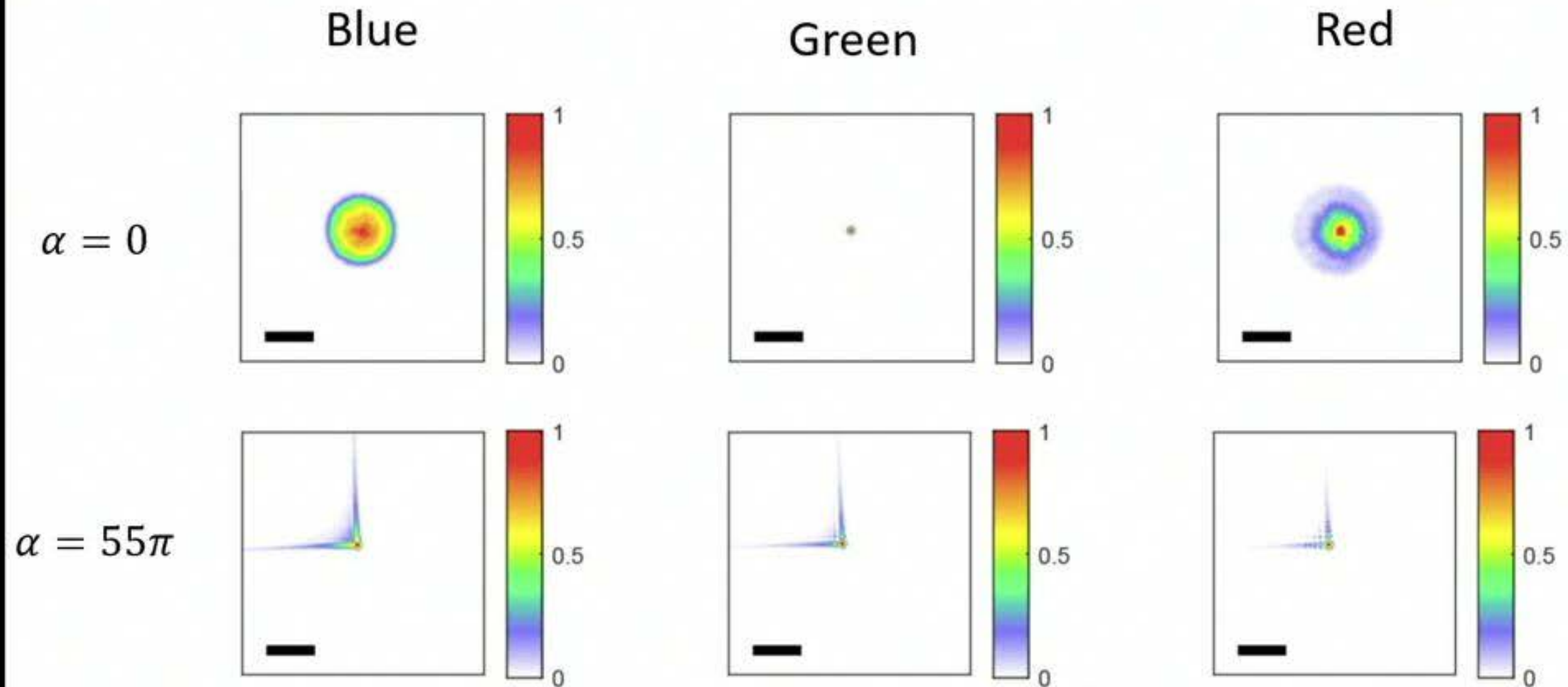
$\alpha = 0$



Computational imaging approach

27

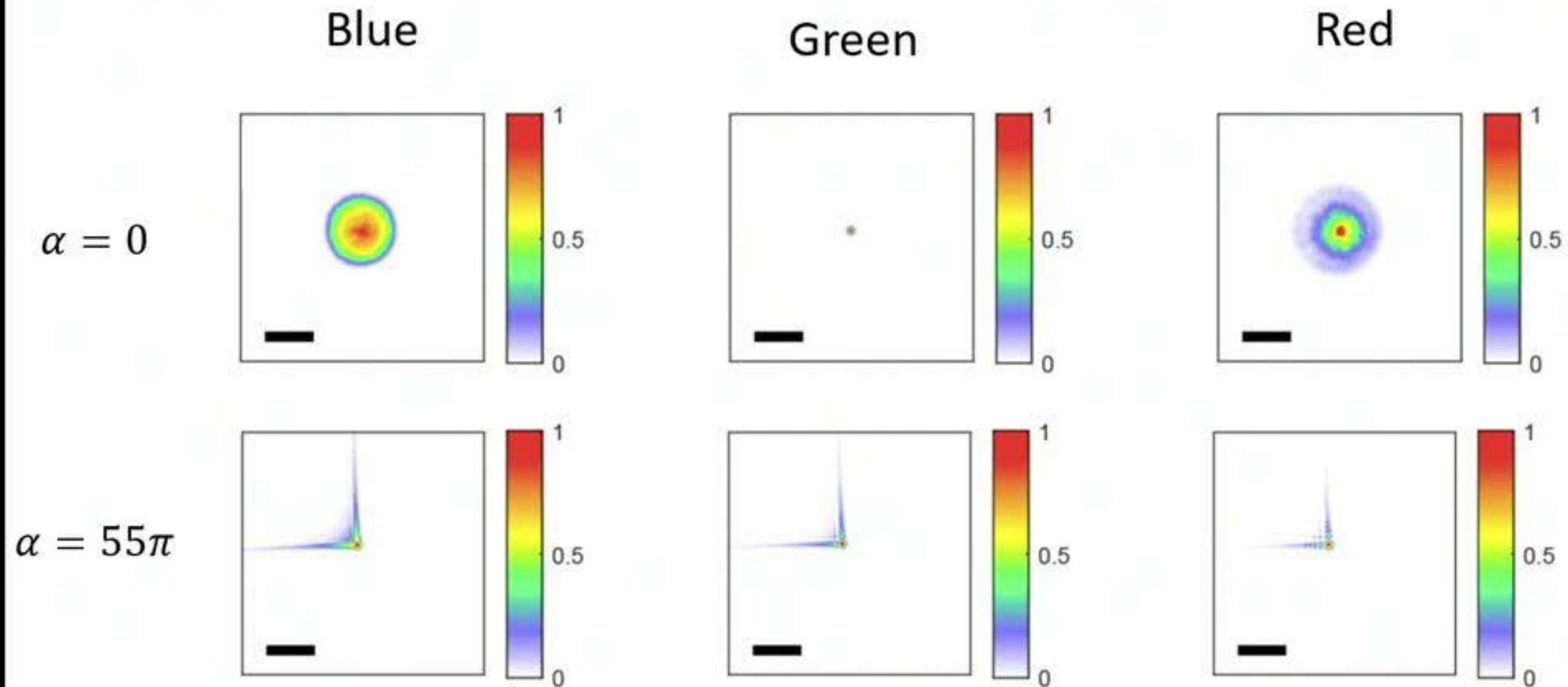
$$\varphi = \frac{2\pi}{\lambda} (\sqrt{x^2 + y^2 + f^2} - f) + \frac{\alpha}{L^3} (x^3 + y^3)$$



Computational imaging approach

27

$$\varphi = \frac{2\pi}{\lambda} (\sqrt{x^2 + y^2 + f^2} - f) + \frac{\alpha}{L^3} (x^3 + y^3)$$



E. Dowski et al. Applied Optics, **34**, 11 (1995)

H. Wach et al. Applied Optics, **37**, 23 (1998)

S. Colburn et al. Science Advances **4**, eaar2114 (2018)

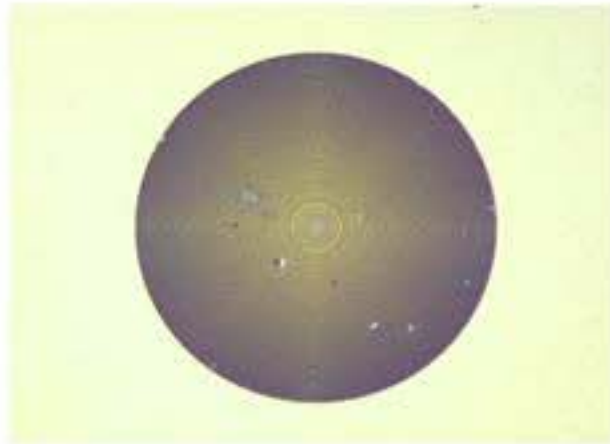
Computational imaging approach

28

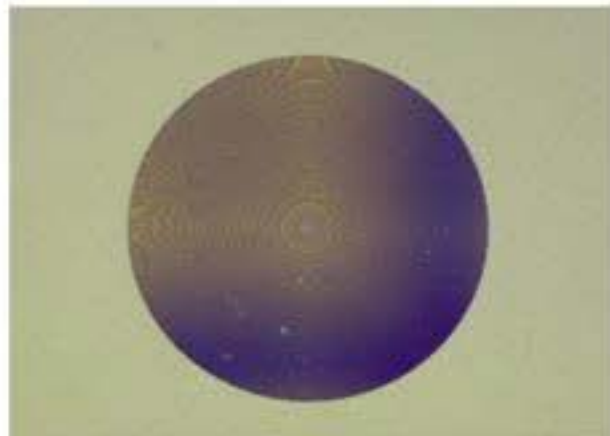
Singlet



Singlet

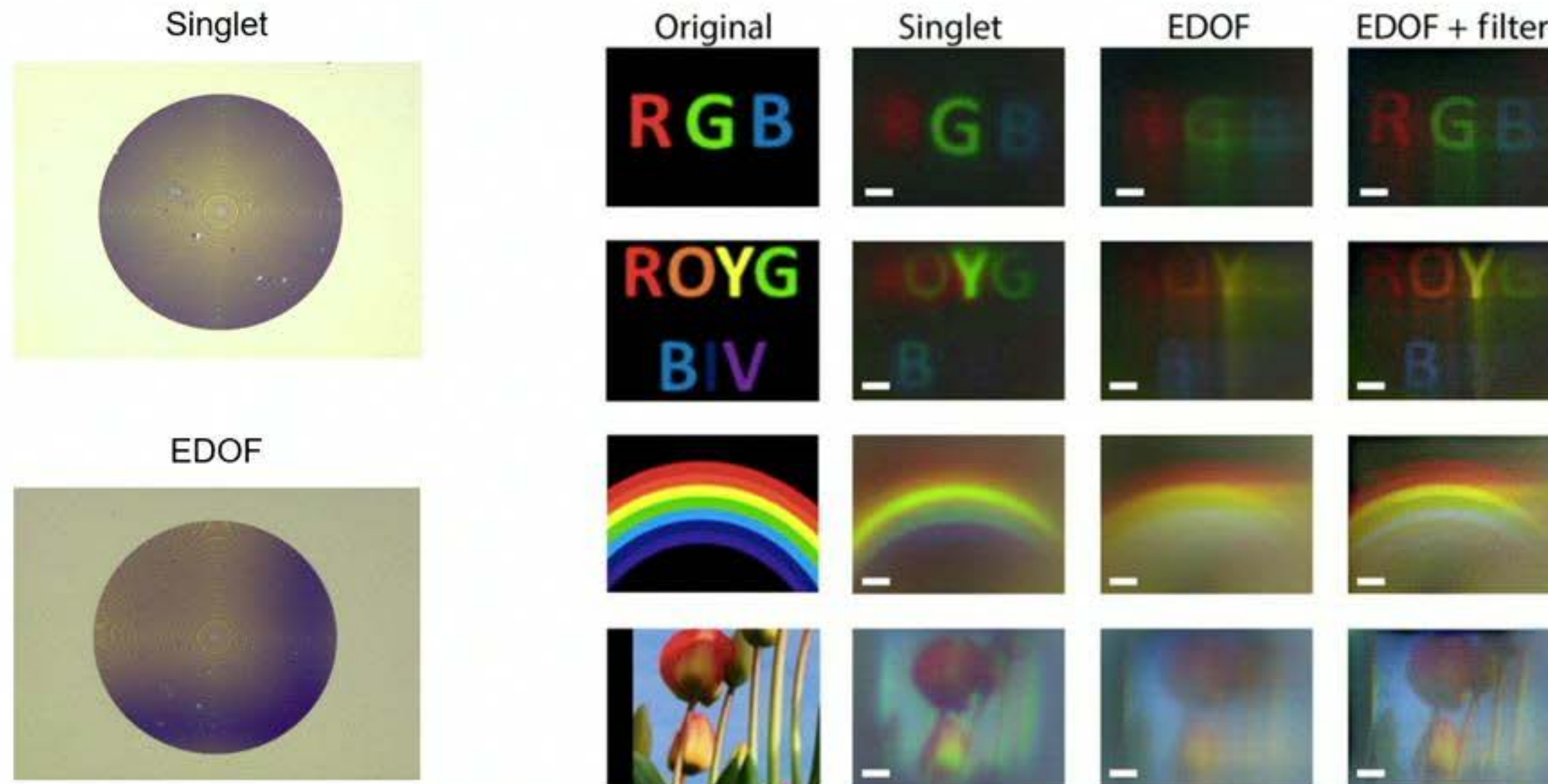


EDOF



Computational imaging approach

28



Holography

L. Huang et al. Nanophotonics **7**, 6 1169-1190 (2018)

Polarization optics

A. Arbabi et al. Nat. Nano. **10**, 937-943 (2015)

N. Rubin et al. Optics Express. **26**, 17 (2018)

Nonlinear optics

A. Krasnok et al. Materials Today. **21**, 1 (2018)

Review articles

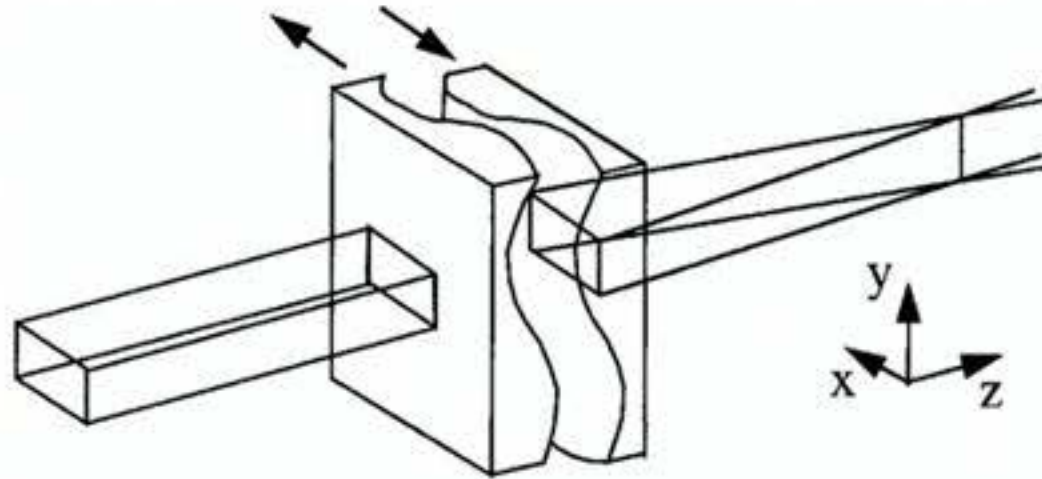
S. Kamali et al. Nanophotonics **7**, 6 (2018)

D. Neshev et al. Light, Sci. and Appl. **7**, 58 (2018)

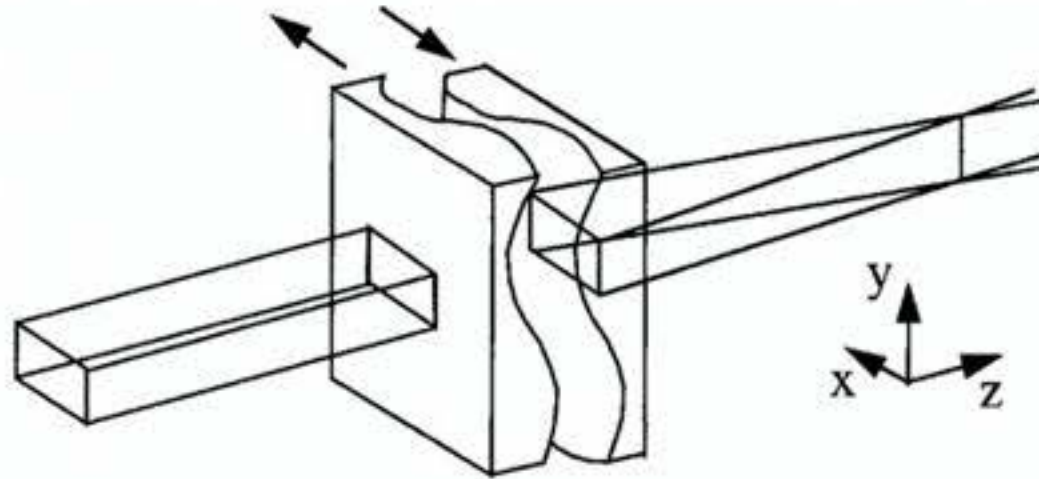
1. Single element metasurface optics
2. Towards metasurface optical systems
3. Inverse design and optimization of metasurfaces
4. Future work and outlook

Alvarez lens

31



31



31

Barton et al. Opt. Lett. **25**, 1 (2000)

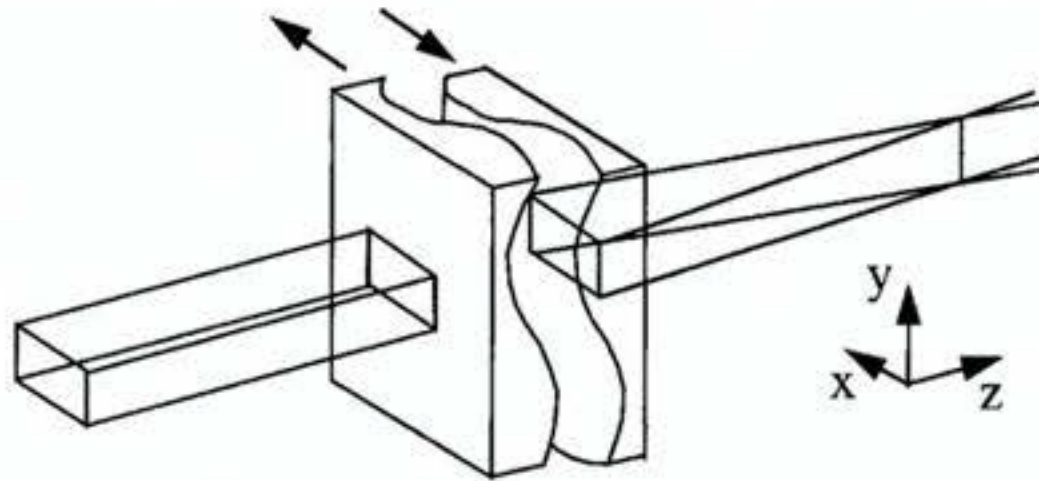
$$\varphi_{Alv}(x, y) = A \left(\frac{1}{3} x^3 + xy^2 \right)$$

$$\varphi_{Inv}(x, y) = -A \left(\frac{1}{3} x^3 + xy^2 \right)$$

$$f(d) = \frac{1}{4Ad}$$

Alvarez lens

31



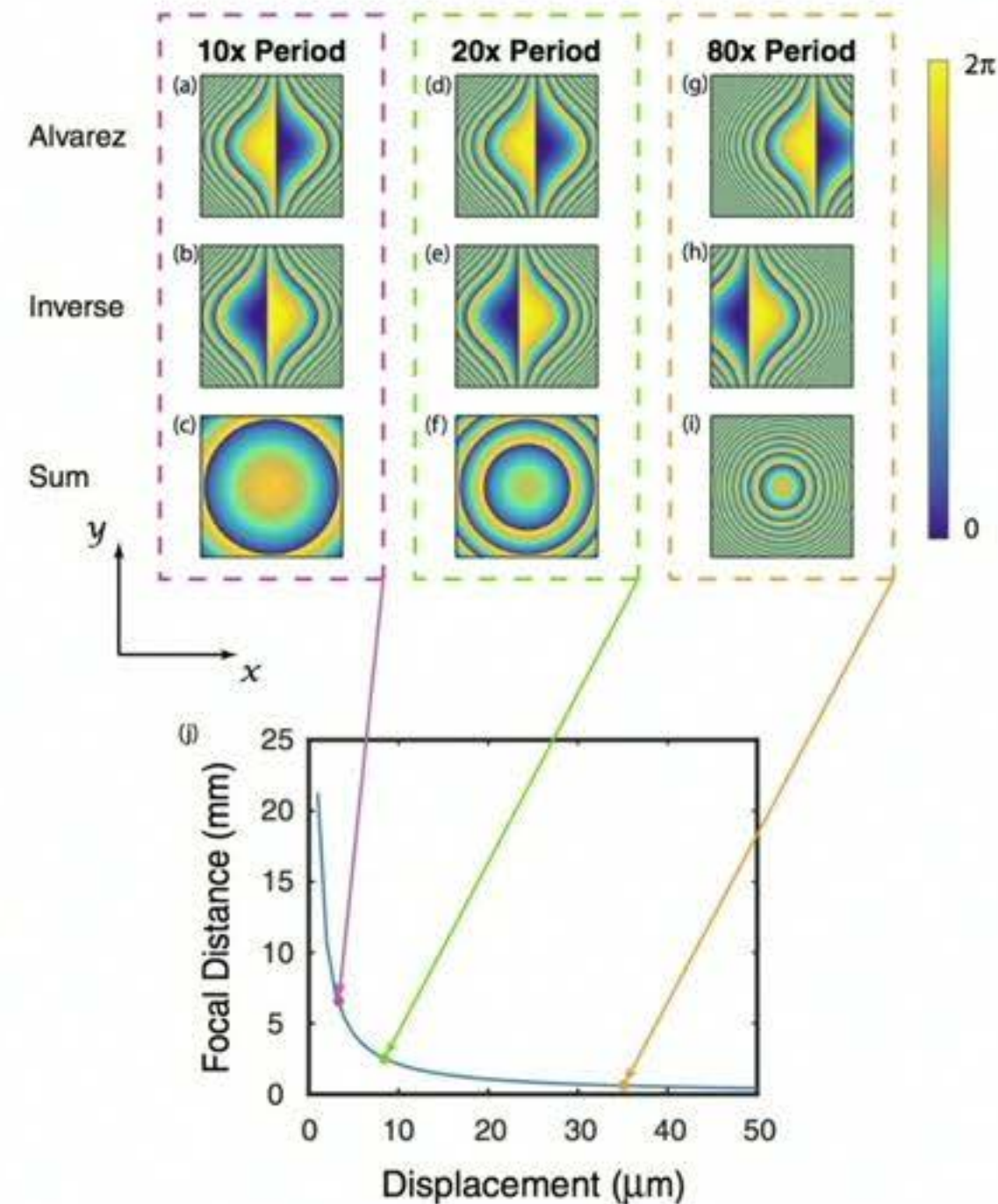
Barton et al. Opt. Lett. **25**, 1 (2000)

$$\varphi_{Alv}(x, y) = A \left(\frac{1}{3} x^3 + xy^2 \right)$$

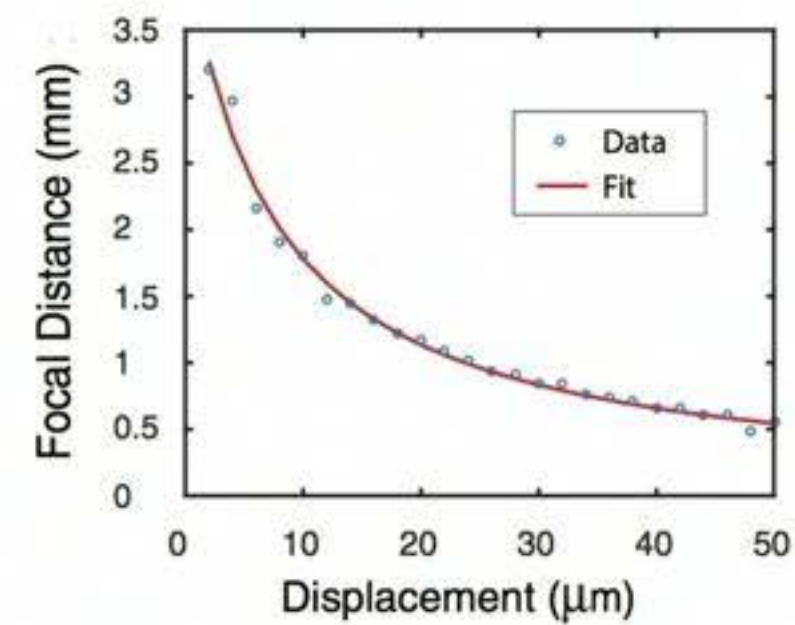
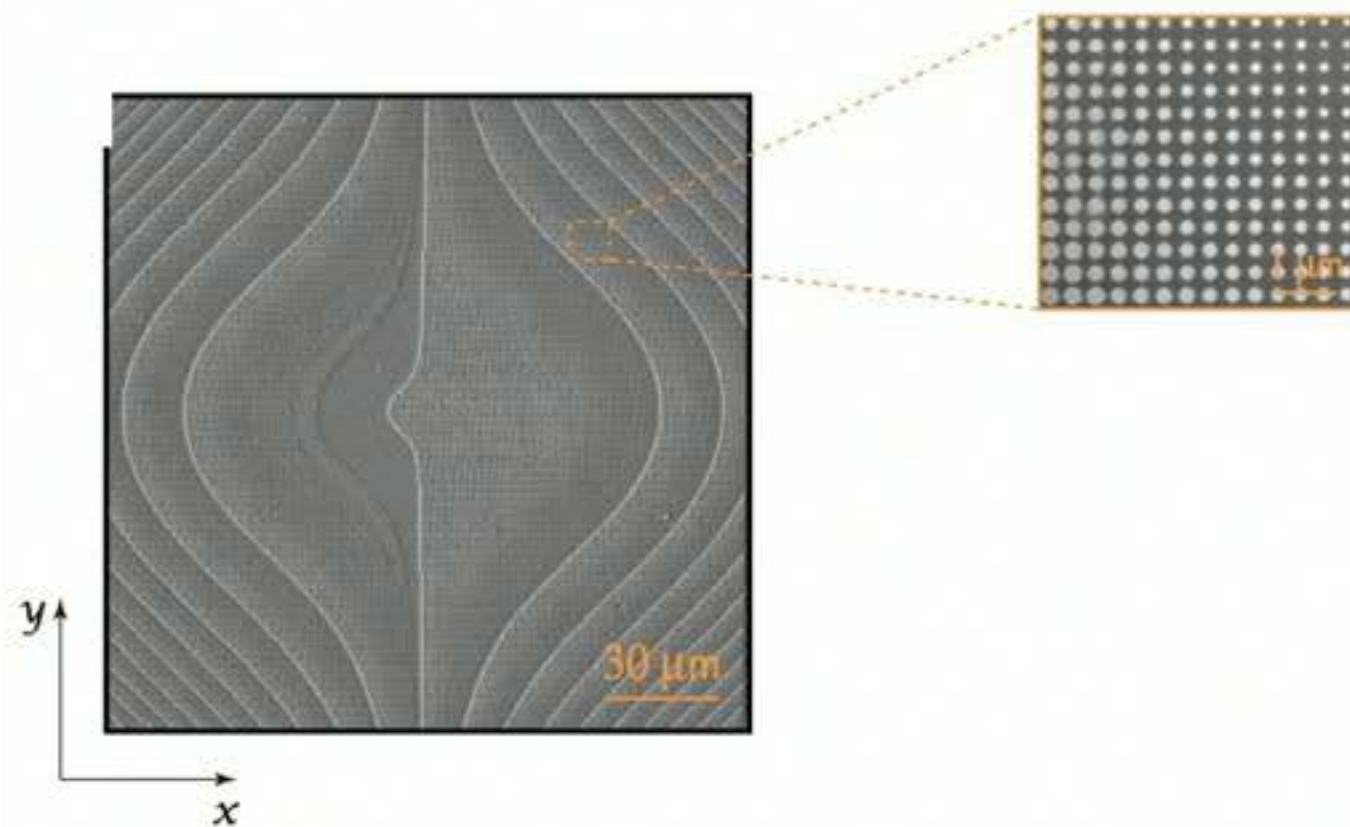
$$\varphi_{Inv}(x, y) = -A \left(\frac{1}{3} x^3 + xy^2 \right)$$

$$f(d) = \frac{1}{4Ad}$$

A. Zhan et al, Scientific Reports. **7**, 1 (2017).

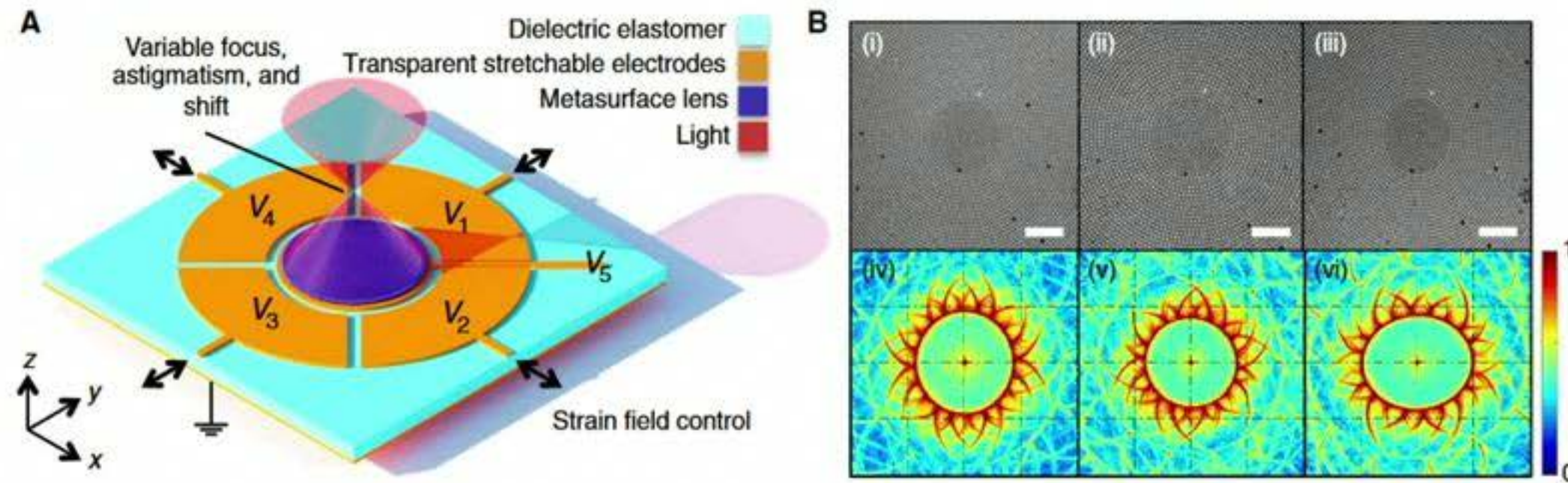


Alvarez lens



Other tunable systems

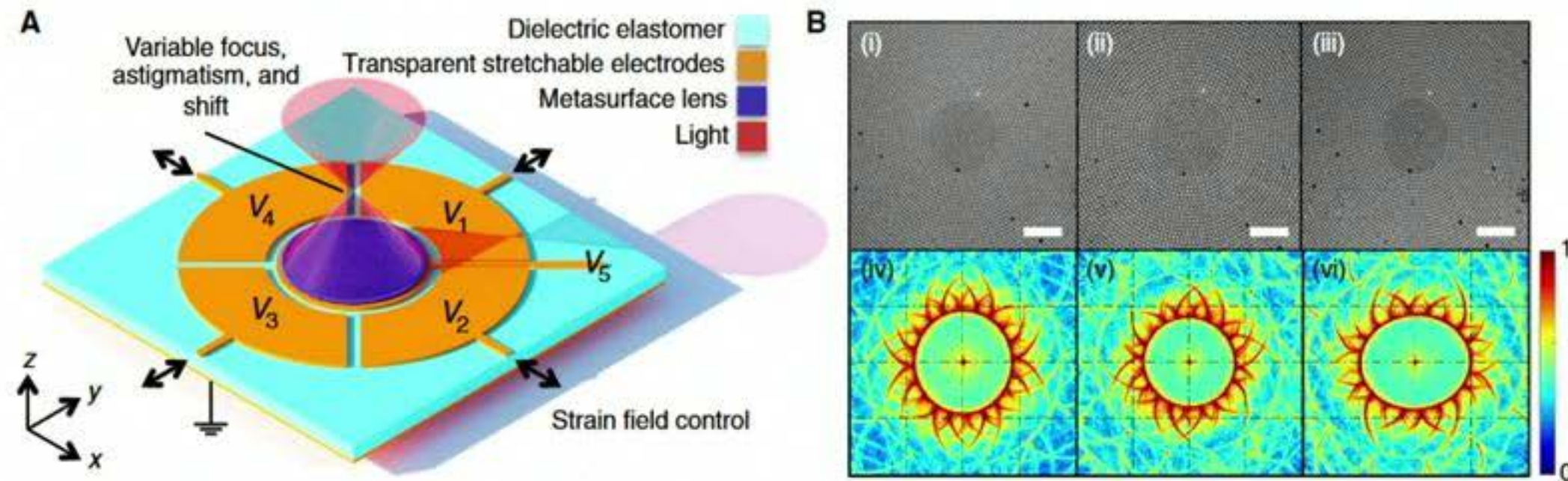
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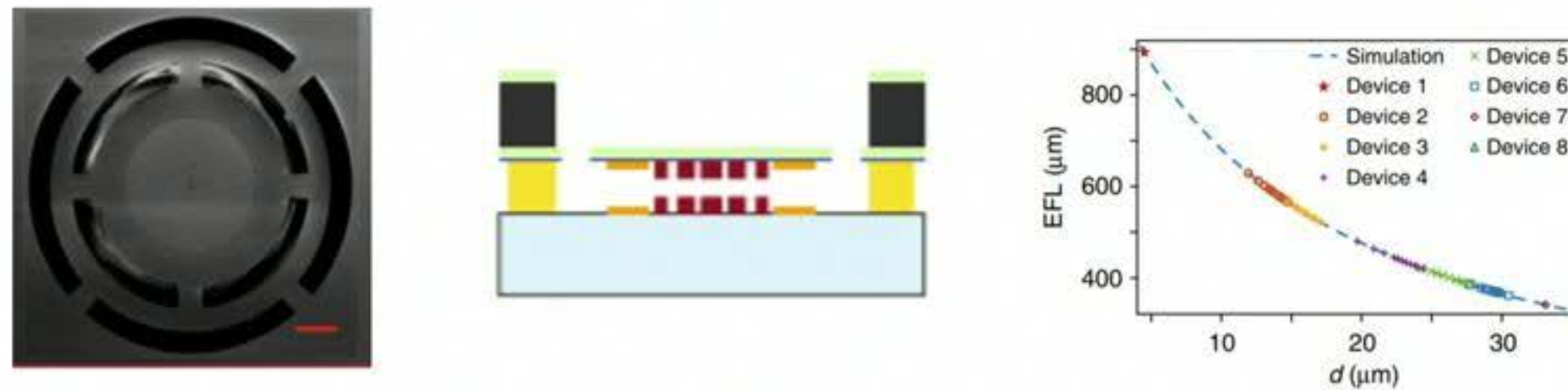
A. She et al, Science Advances. **4**, 2 eaap9957 (2018)

Other tunable systems

33



A. She et al, Science Advances. **4**, 2 eaap9957 (2018)



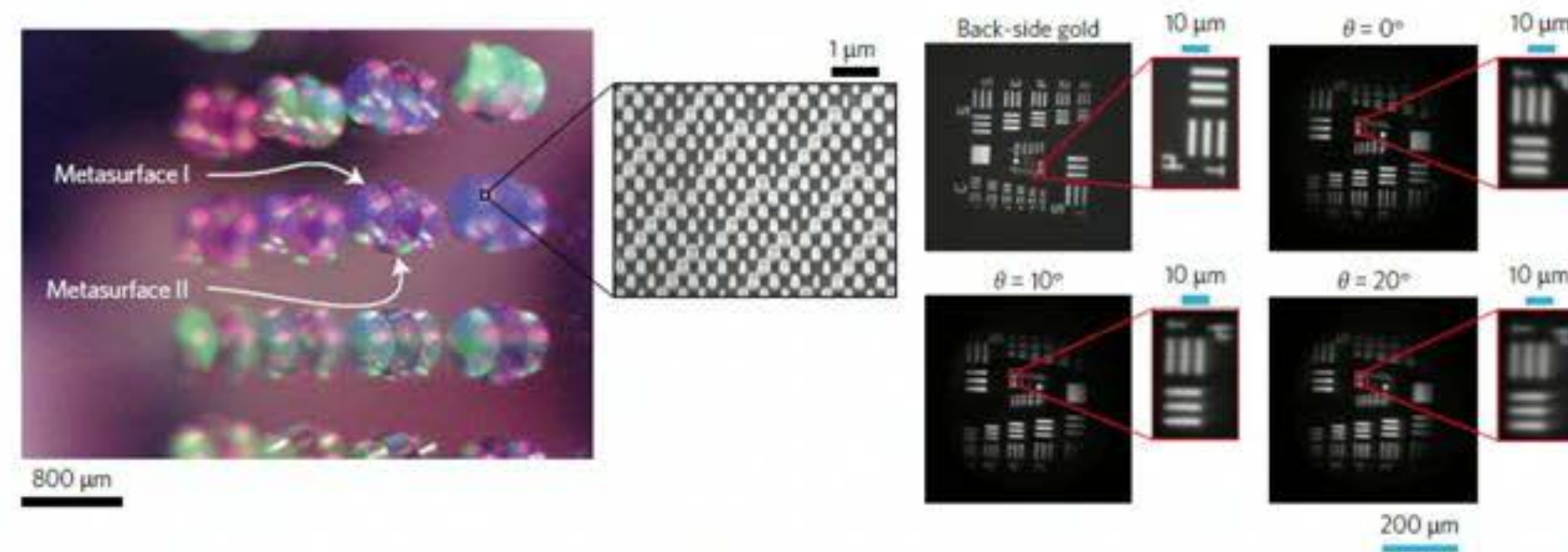
A. Arbabi et al, Nature Communications. **9**, 812 (2018)

Systems for angular incidence

34

Systems for angular incidence

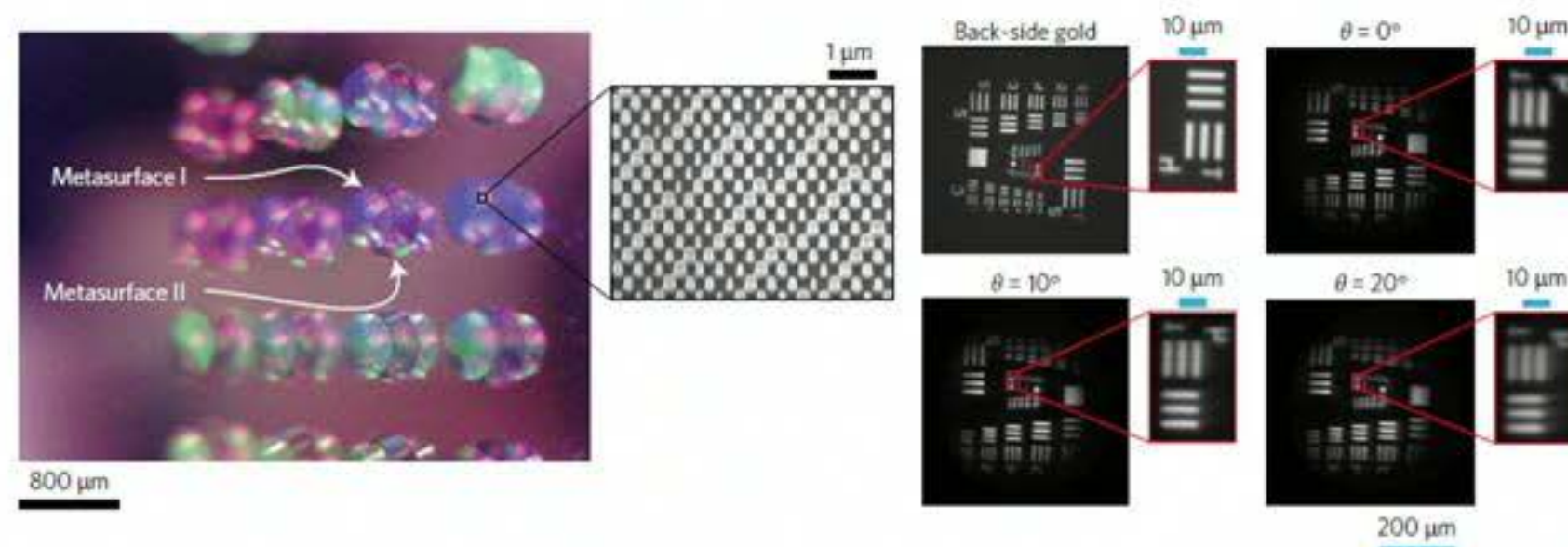
34



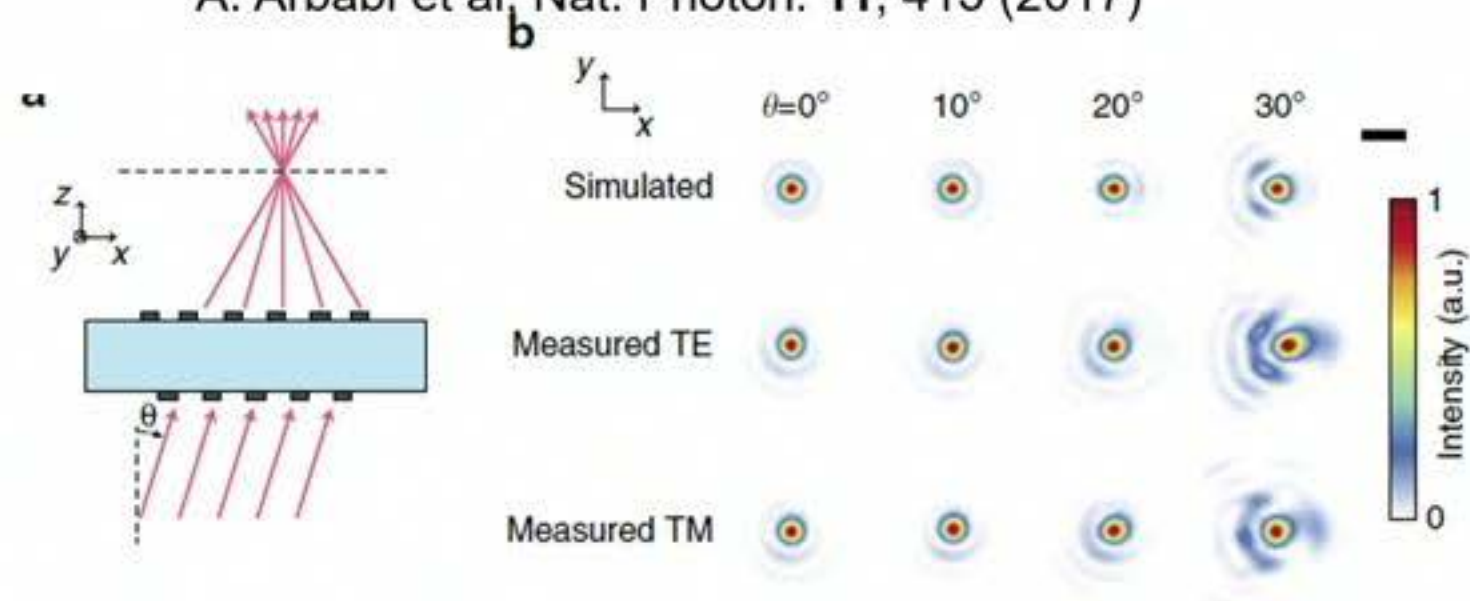
A. Arbabi et al, Nat. Photon. **11**, 415 (2017)

Systems for angular incidence

34



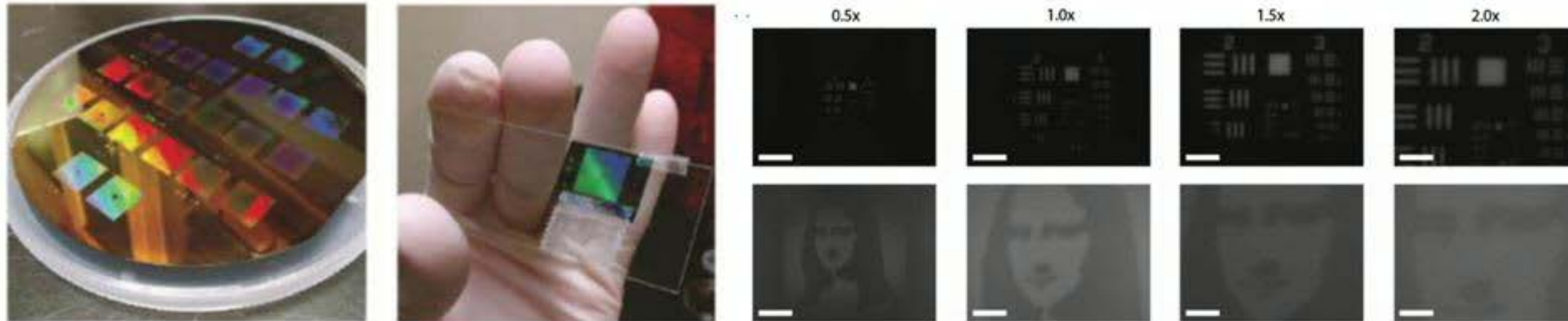
A. Arbabi et al, Nat. Photon. **11**, 415 (2017)



A. Arbabi et al, Nat. Comm. **7**, 13862 (2017)

Large area design

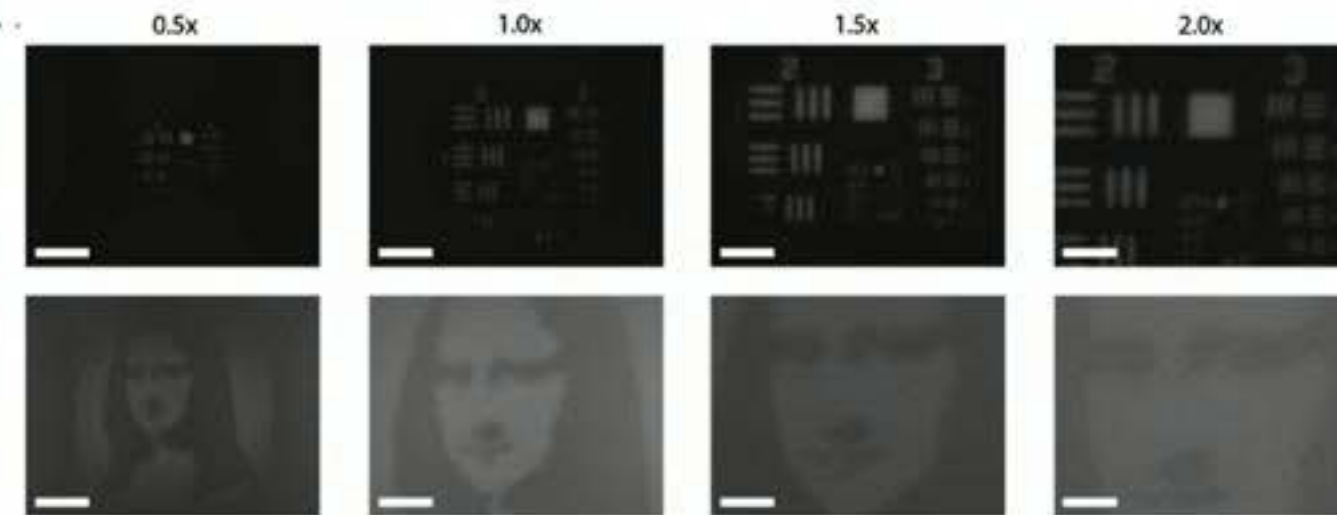
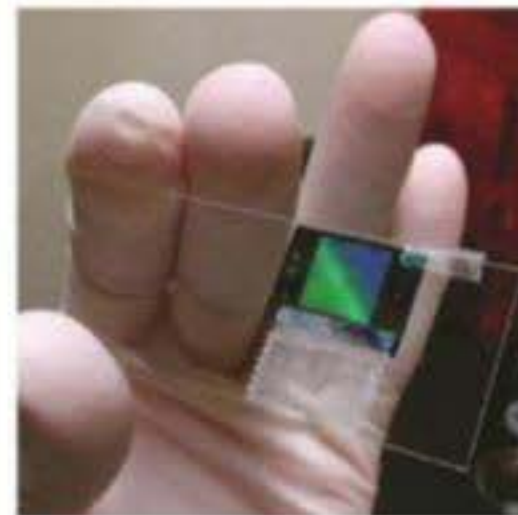
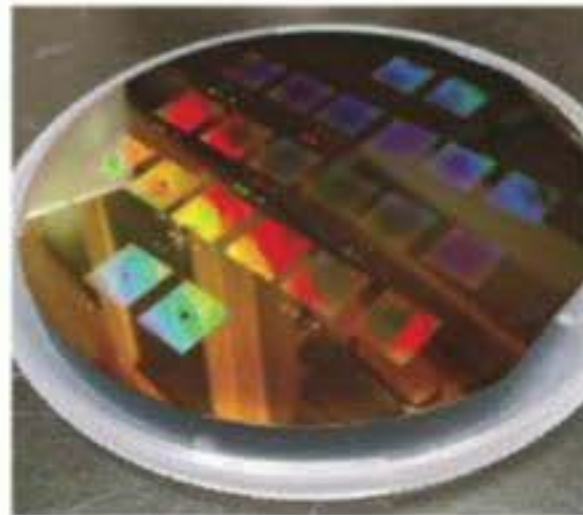
35



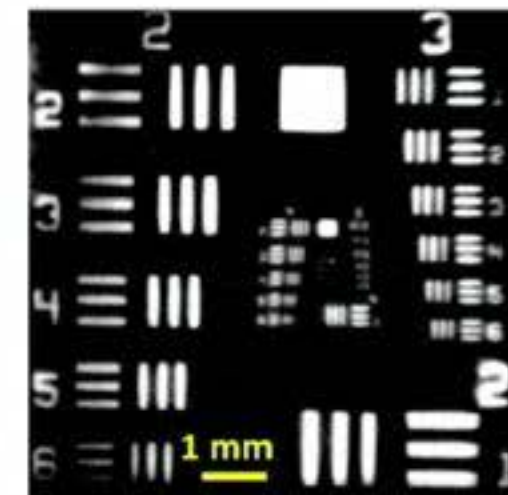
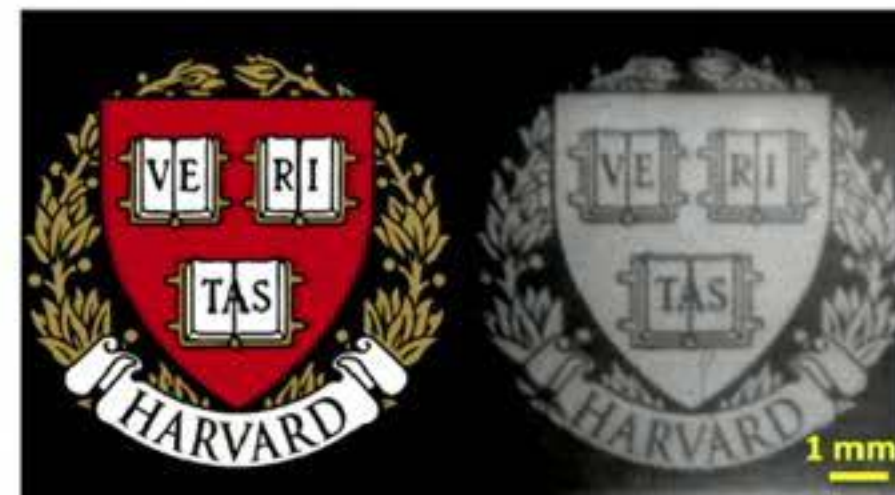
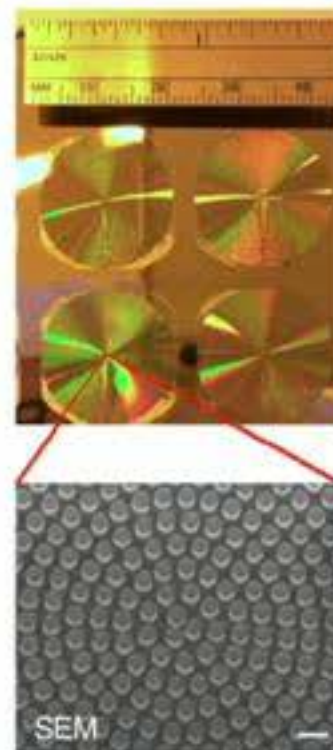
S. Colburn et al. Optica **5**, 7 (2018)

Large area design

35



S. Colburn et al. *Optica* **5**, 7 (2018)



A. She et al. *Optics Express* **26**, 2 (2018)

1. Single element metasurface optics
2. Towards metasurface optical systems
3. Inverse design and optimization of metasurfaces
4. Future work and outlook

Forward design

Intuition based

Forward design

Intuition based

Scatterers



Functionality

Inverse design

Computation based

Functionality



Scatterers

Inverse design

Computation based

Functionality $\longrightarrow$ Scatterers

**Formulated as a non-linear
optimization problem:**

Formulated as a non-linear
optimization problem:

Given some figure of merit $f(x(p))$
find some set of parameters p
that minimizes $f(x(p))$ while
 $x(p)$ is constrained to solve the
equation $A(p)x(p) = y(p)$

Formulated as a non-linear
optimization problem:

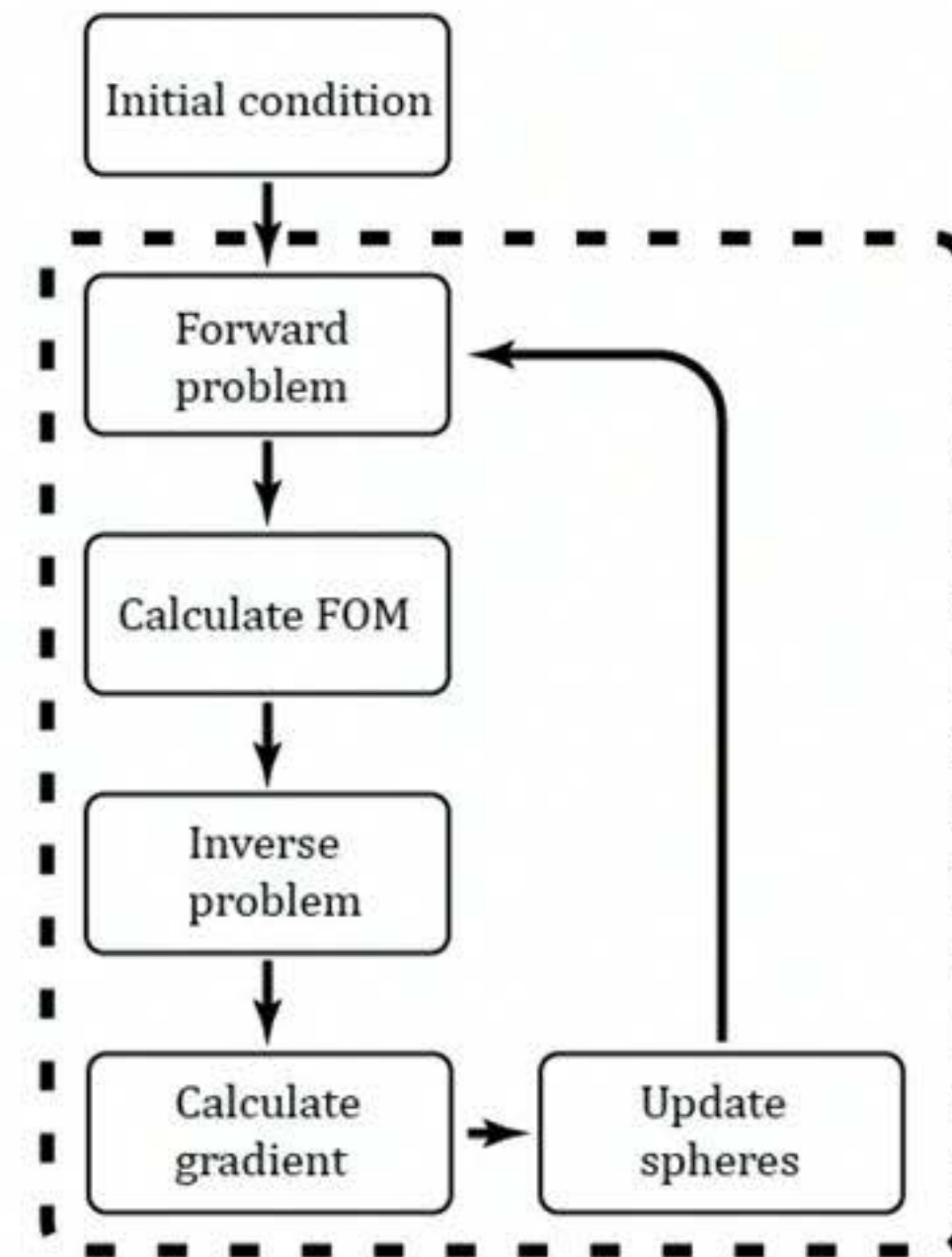
Given some figure of merit $f(x(p))$
find some set of parameters p
that minimizes $f(x(p))$ while
 $x(p)$ is constrained to solve the
equation $A(p)x(p) = y(p)$

In general, a gradient based solution
is used

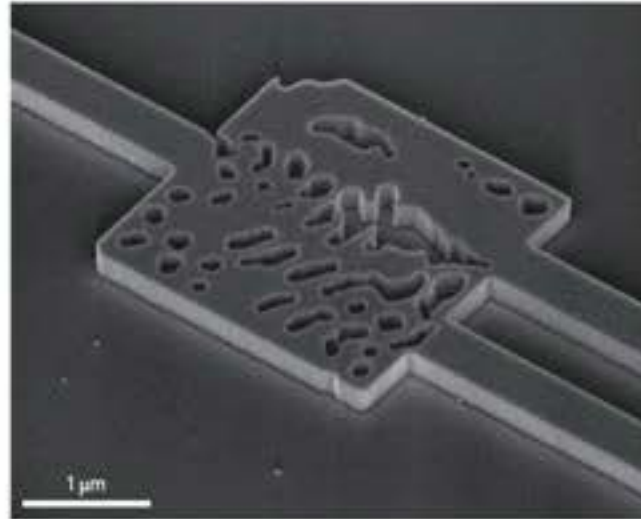
Formulated as a non-linear optimization problem:

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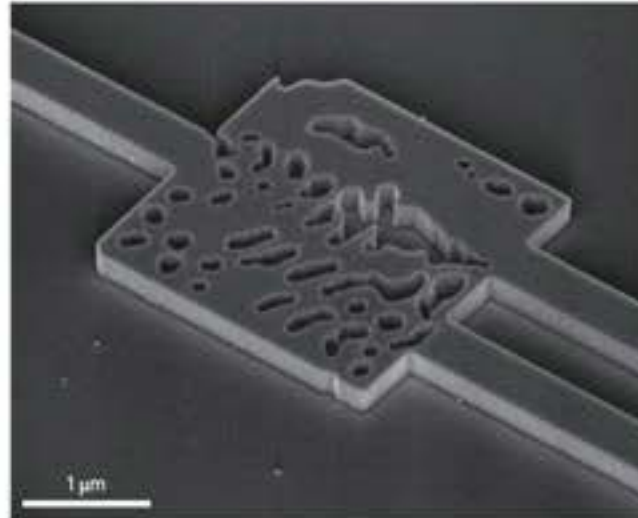
Inverse design based on Maxwell's equations 40



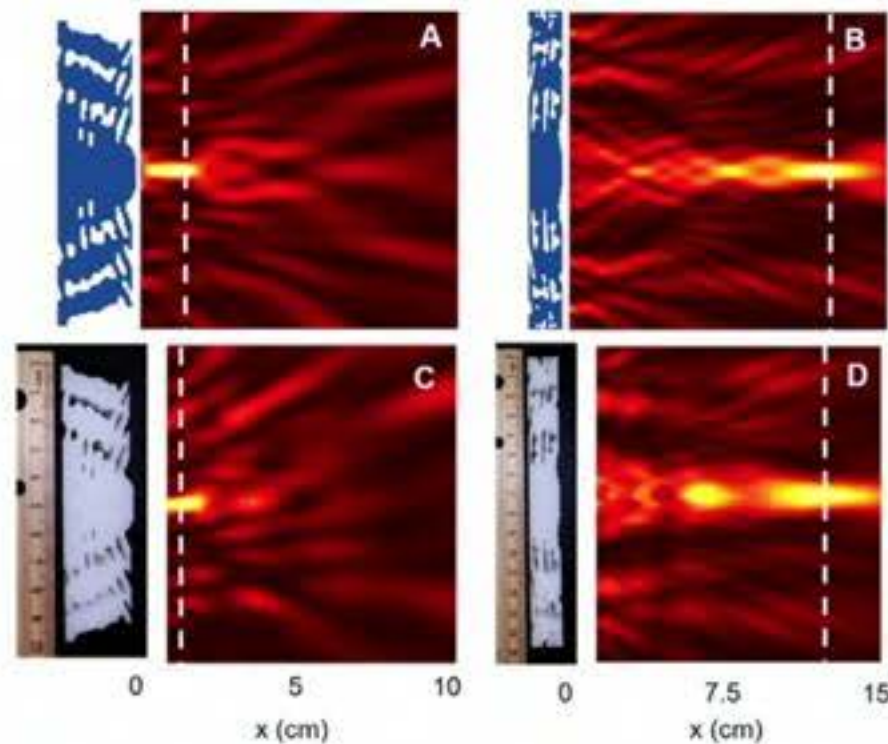
Piggot et al. Nat. Photon. **9**, 6 (2015)

Inverse design based on Maxwell's equations

40



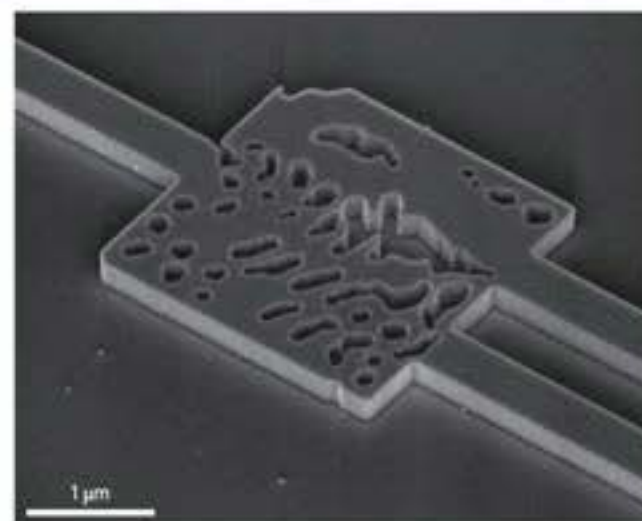
Piggot et al. Nat. Photon. **9**, 6 (2015)



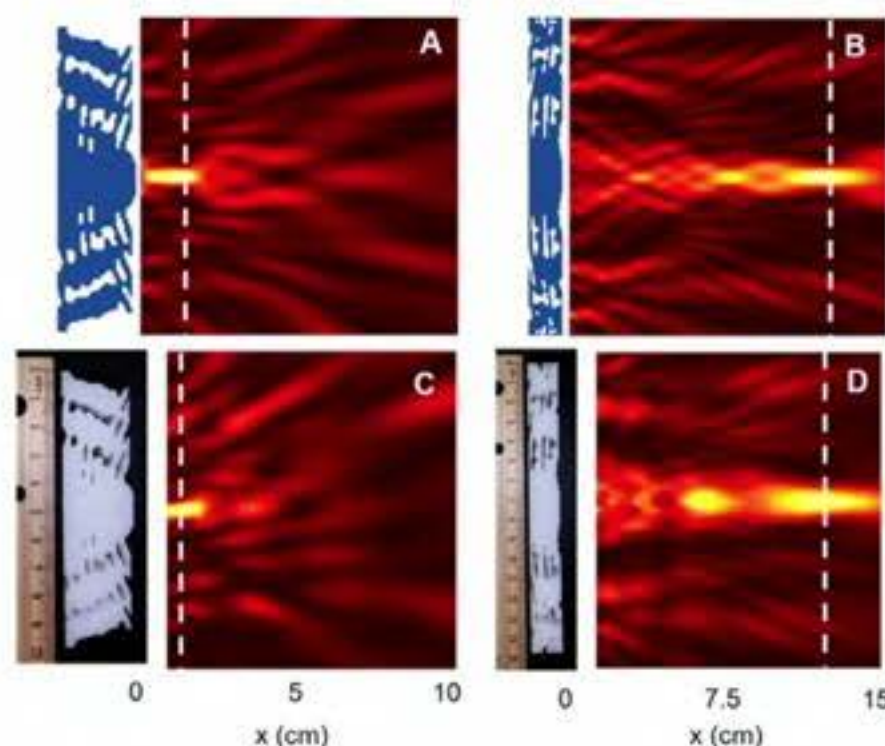
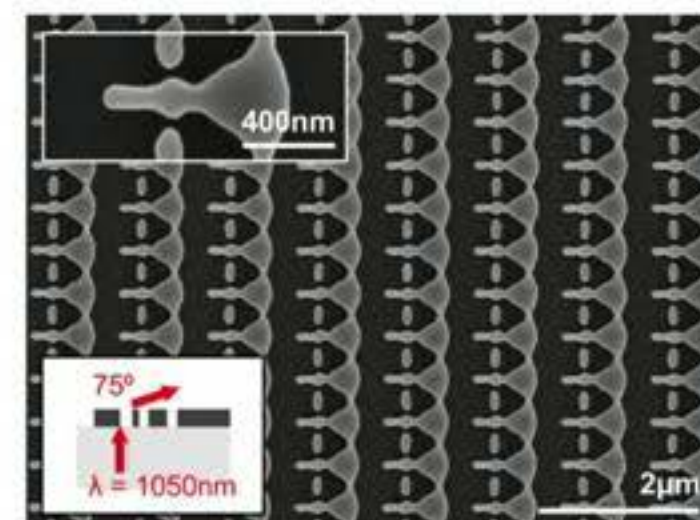
Callewaert et al. Appl. Phys. Lett. **112**, 91102 (2018)

Inverse design based on Maxwell's equations

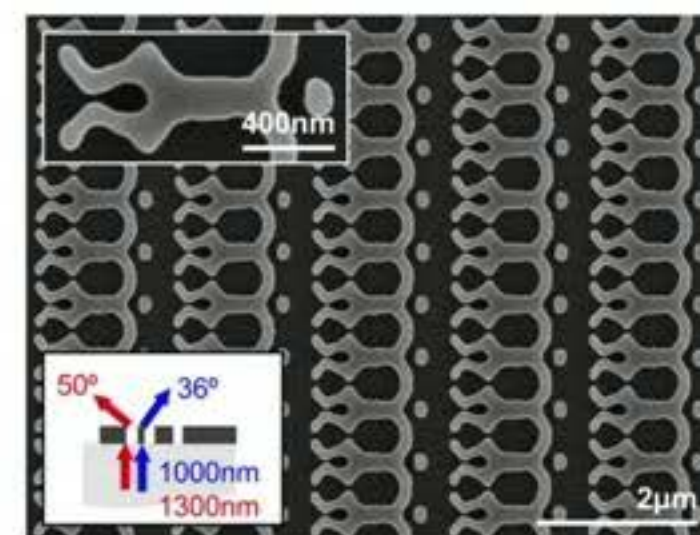
40



Piggot et al. Nat. Photon. **9**, 6 (2015)



Callewaert et al. Appl. Phys. Lett. **112**, 91102 (2018)



Sell et al. Nano Lett. **17**, 6 (2017)

Time Domain

$$\nabla \cdot (\epsilon \mathbf{E}) = \rho_f$$

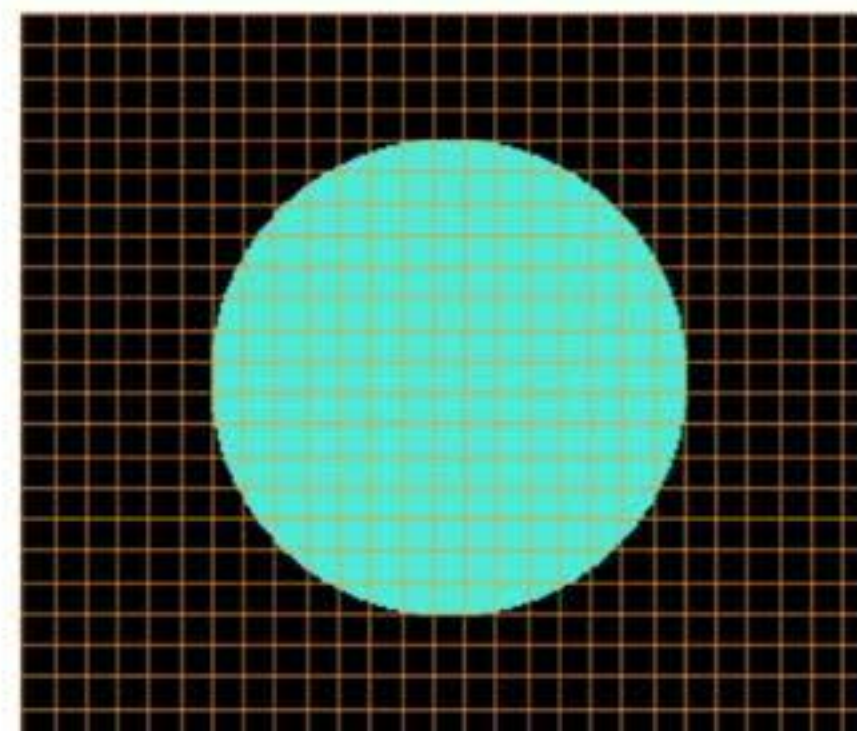
$$\nabla \cdot \mathbf{H} = 0$$

$$\nabla \times \mathbf{E} = -\mu_0 \frac{\partial \mathbf{H}}{\partial t}$$

$$\nabla \times \mathbf{H} = \mathbf{J}_f + \frac{\partial(\epsilon \mathbf{E})}{\partial t}$$

Frequency Domain

$$\nabla \times \nabla \times \mathbf{E} - \omega^2 \mu_0 \epsilon \mathbf{E} = -i\omega \mu_0 \mathbf{J}_f$$



Time Domain

$$\nabla \cdot (\epsilon \mathbf{E}) = \rho_f$$

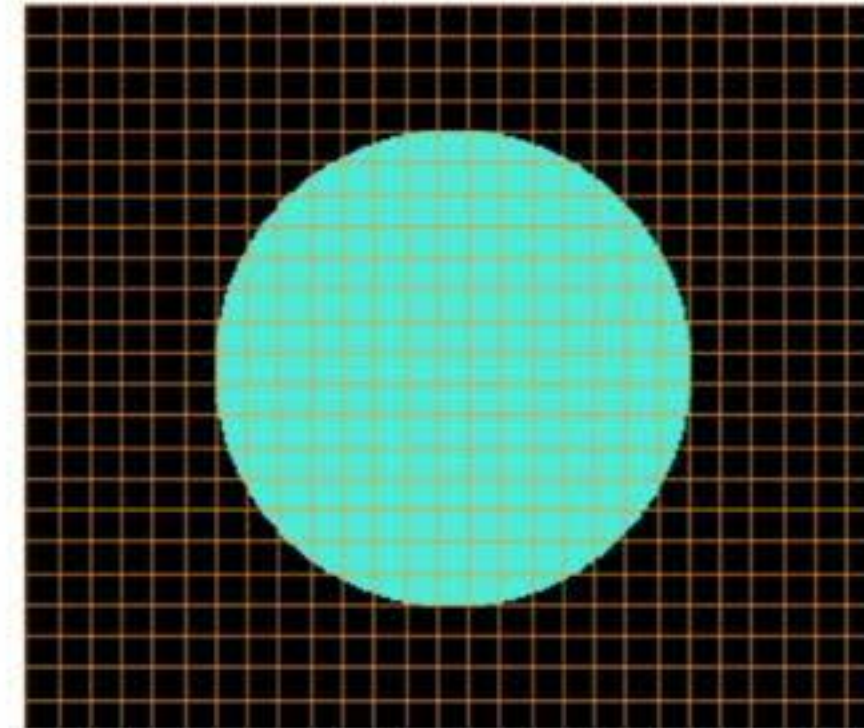
$$\nabla \cdot \mathbf{H} = 0$$

$$\nabla \times \mathbf{E} = -\mu_0 \frac{\partial \mathbf{H}}{\partial t}$$

$$\nabla \times \mathbf{H} = \mathbf{J}_f + \frac{\partial(\epsilon \mathbf{E})}{\partial t}$$

Frequency Domain

$$\nabla \times \nabla \times \mathbf{E} - \omega^2 \mu_0 \epsilon \mathbf{E} = -i\omega \mu_0 \mathbf{J}_f$$



Problem: Memory scales with the volume of the system!

Two main challenges:

Two main challenges:

1. Fast and memory efficient simulation method

Two main challenges:

1. Fast and memory efficient simulation method
2. Faithfully numerically simulate the physical system

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The idea:

Achieve both with an analytical scattering theory, namely the generalized multi-sphere Mie method (GMMT)

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1. Fast and memory efficient simulation method
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The idea:

Achieve both with an analytical scattering theory, namely the generalized multi-sphere Mie method (GMMT)



celes



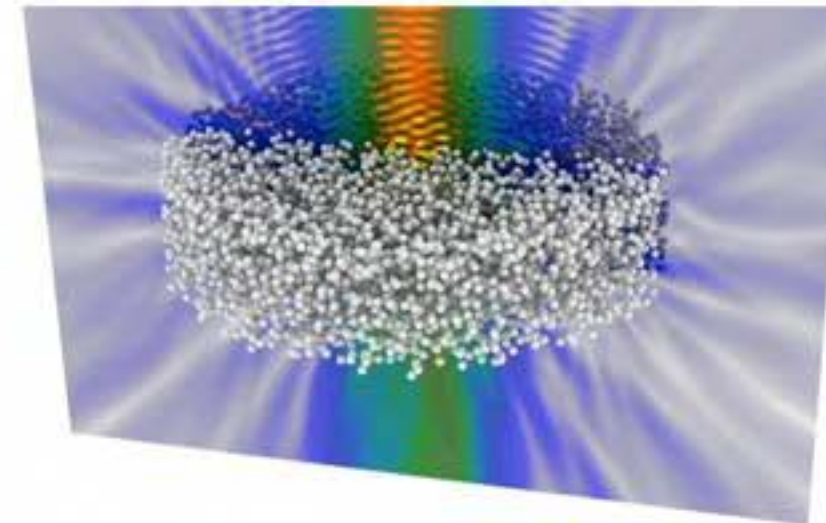
celes

$$M(\mathbf{R})b(\mathbf{R}) = T(\mathbf{R})a$$

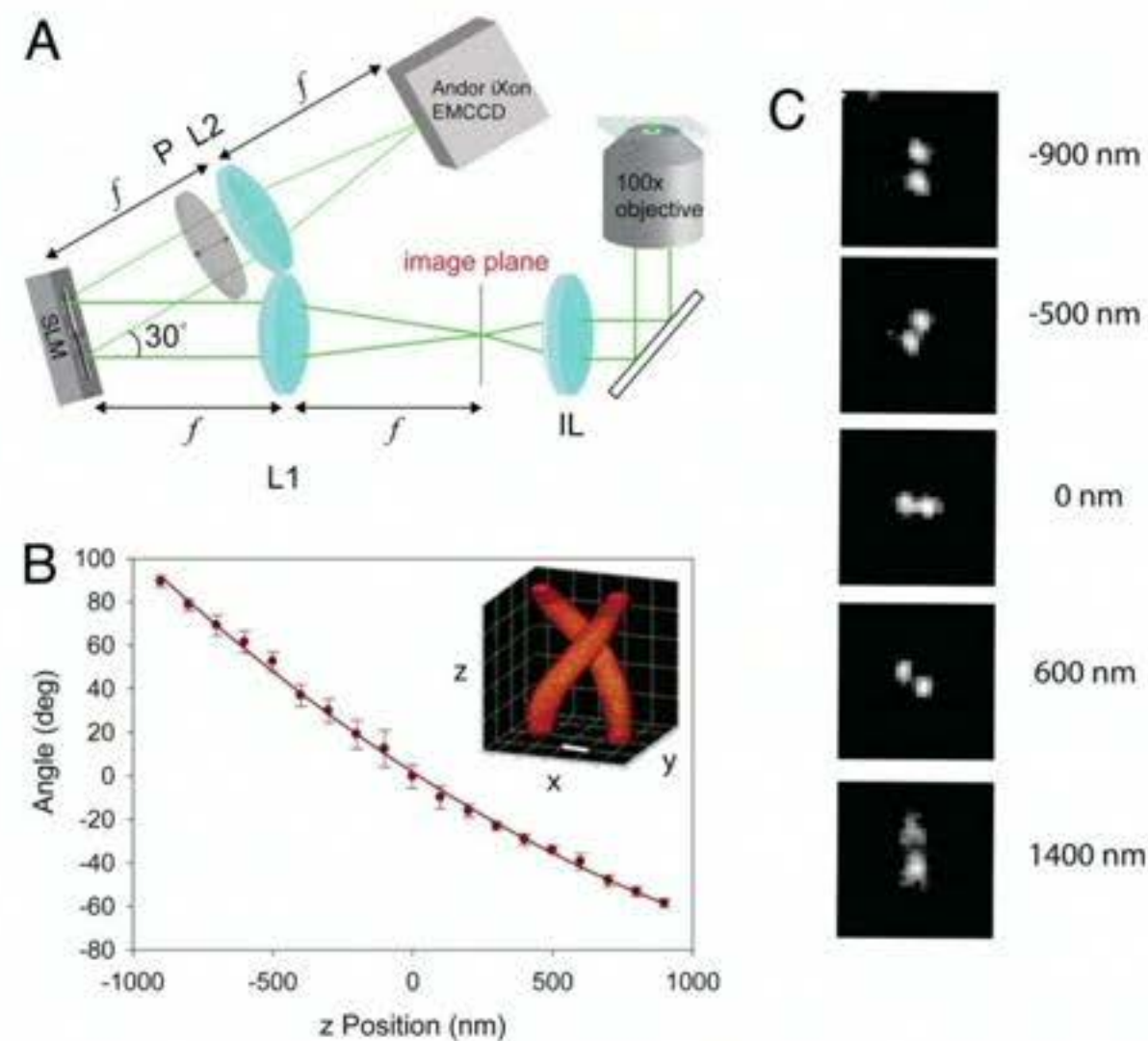


celes

$$M(\mathbf{R})b(\mathbf{R}) = T(\mathbf{R})a$$

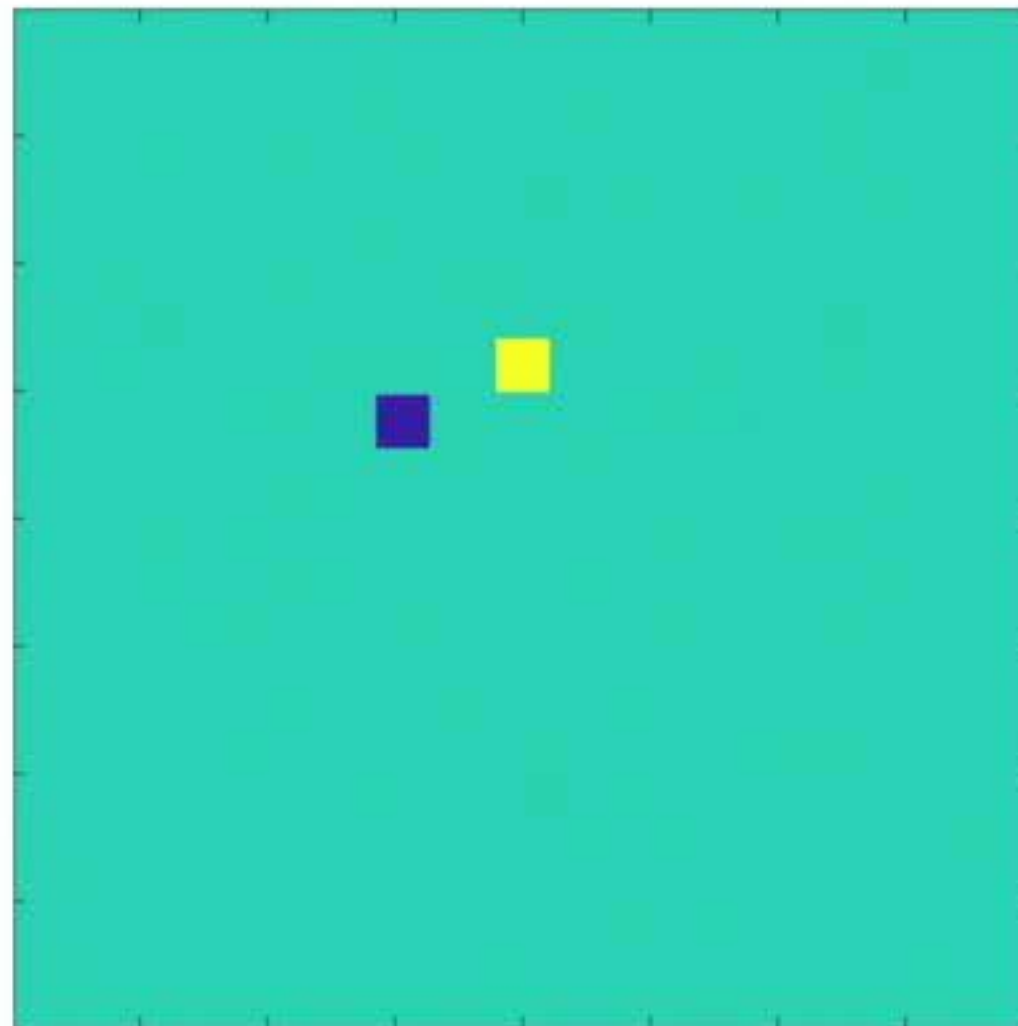


Egel et al. J of Quant. Spec and Rad. Trans.
199 (2017)

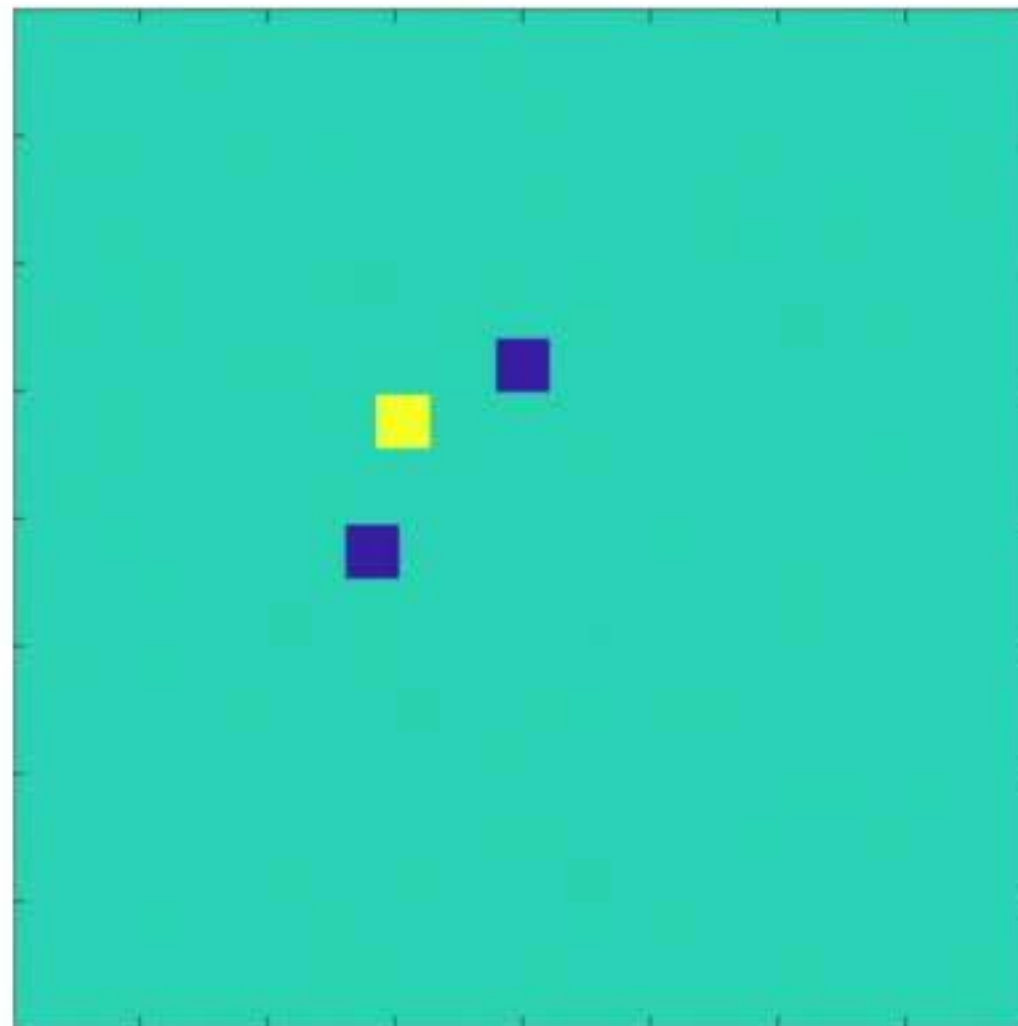


S. R. P. Pavani et al, PNAS **106**, 9 (2009).

100 μm



128 μm



157 μm

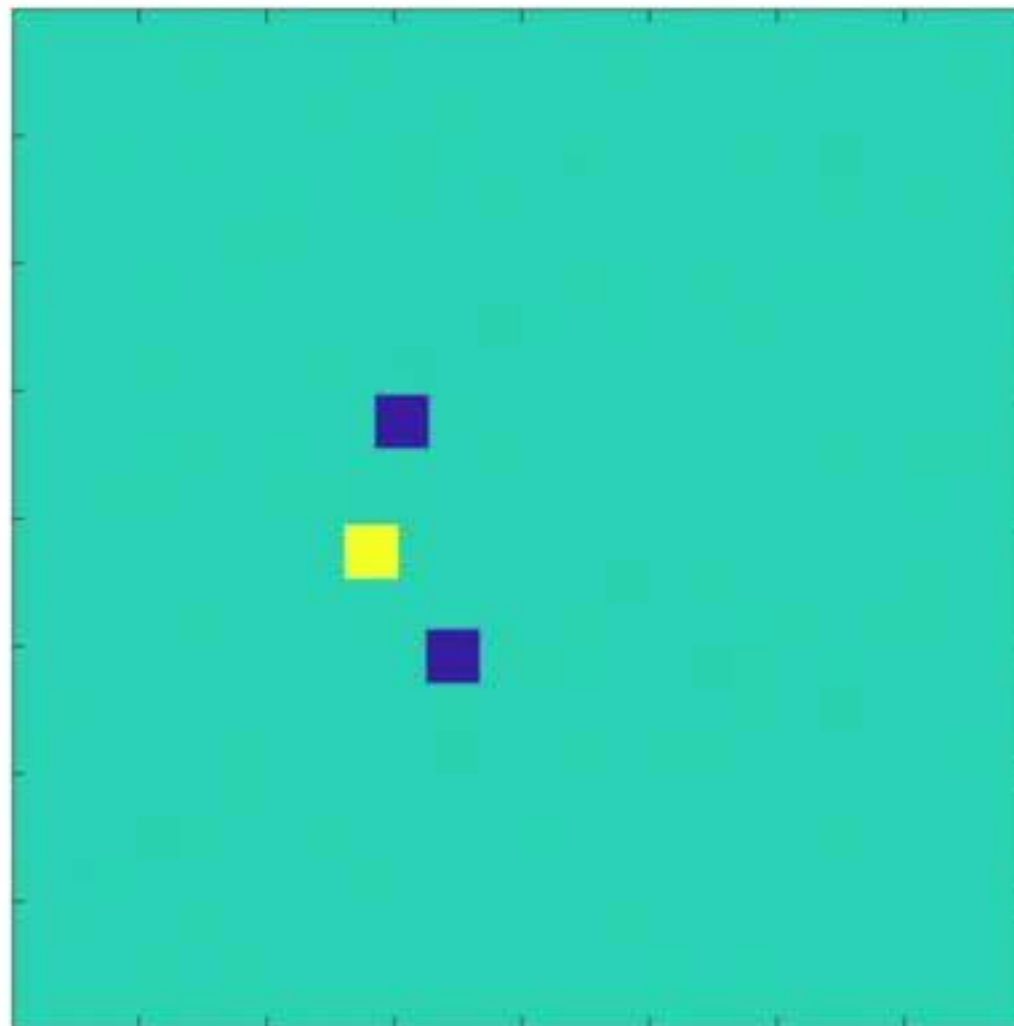


Figure of merit definition

48

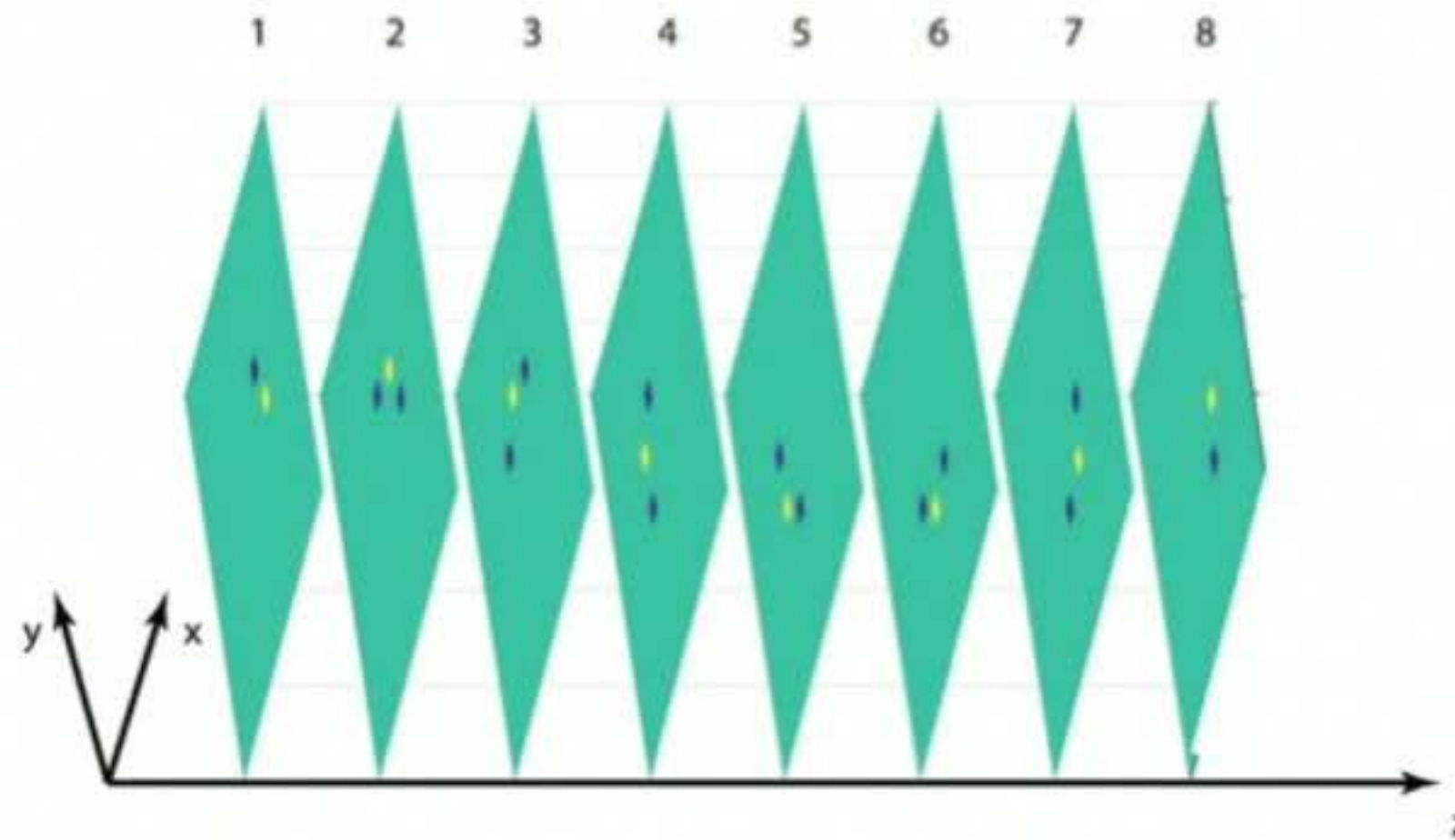
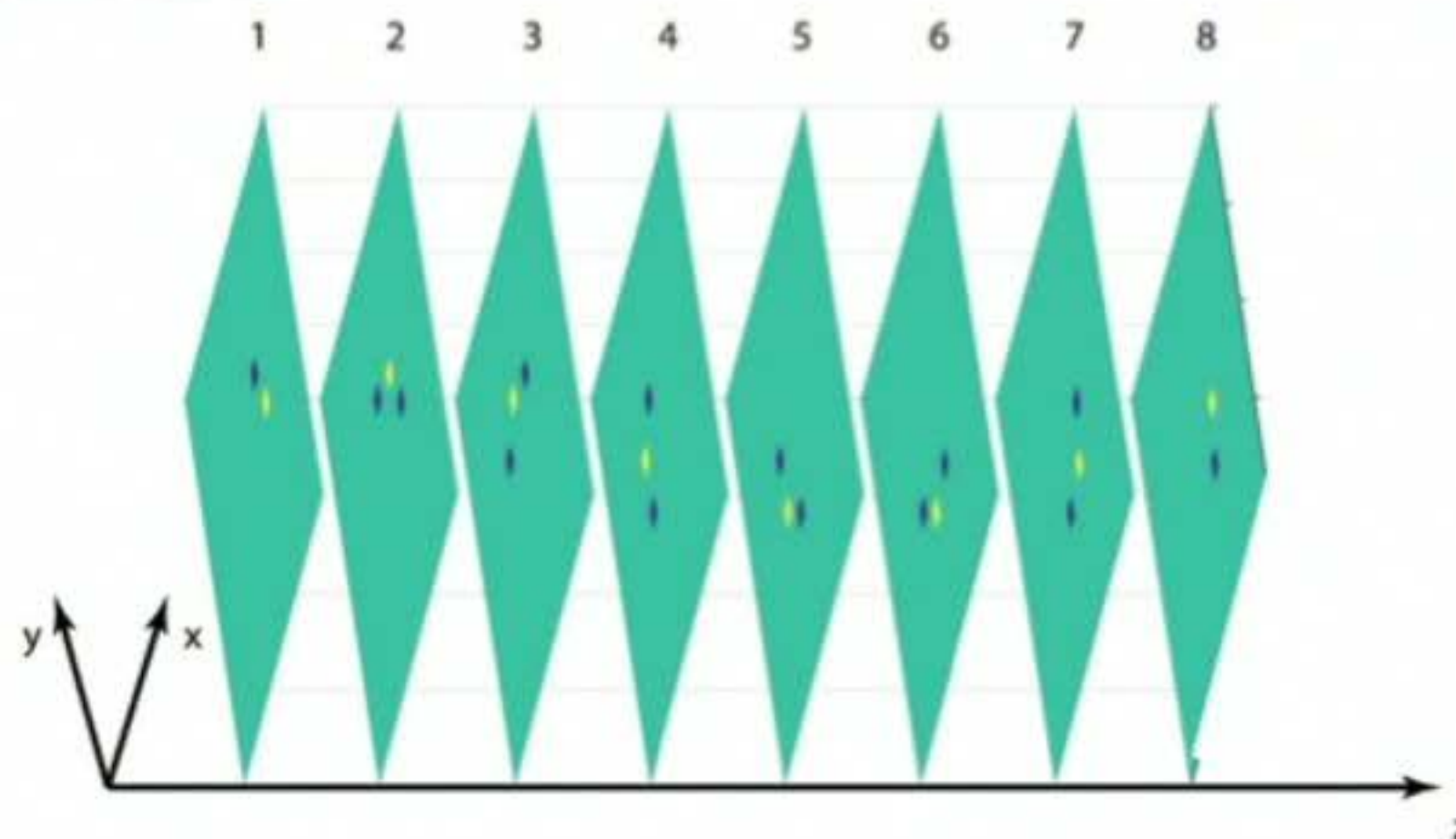


Figure of merit definition

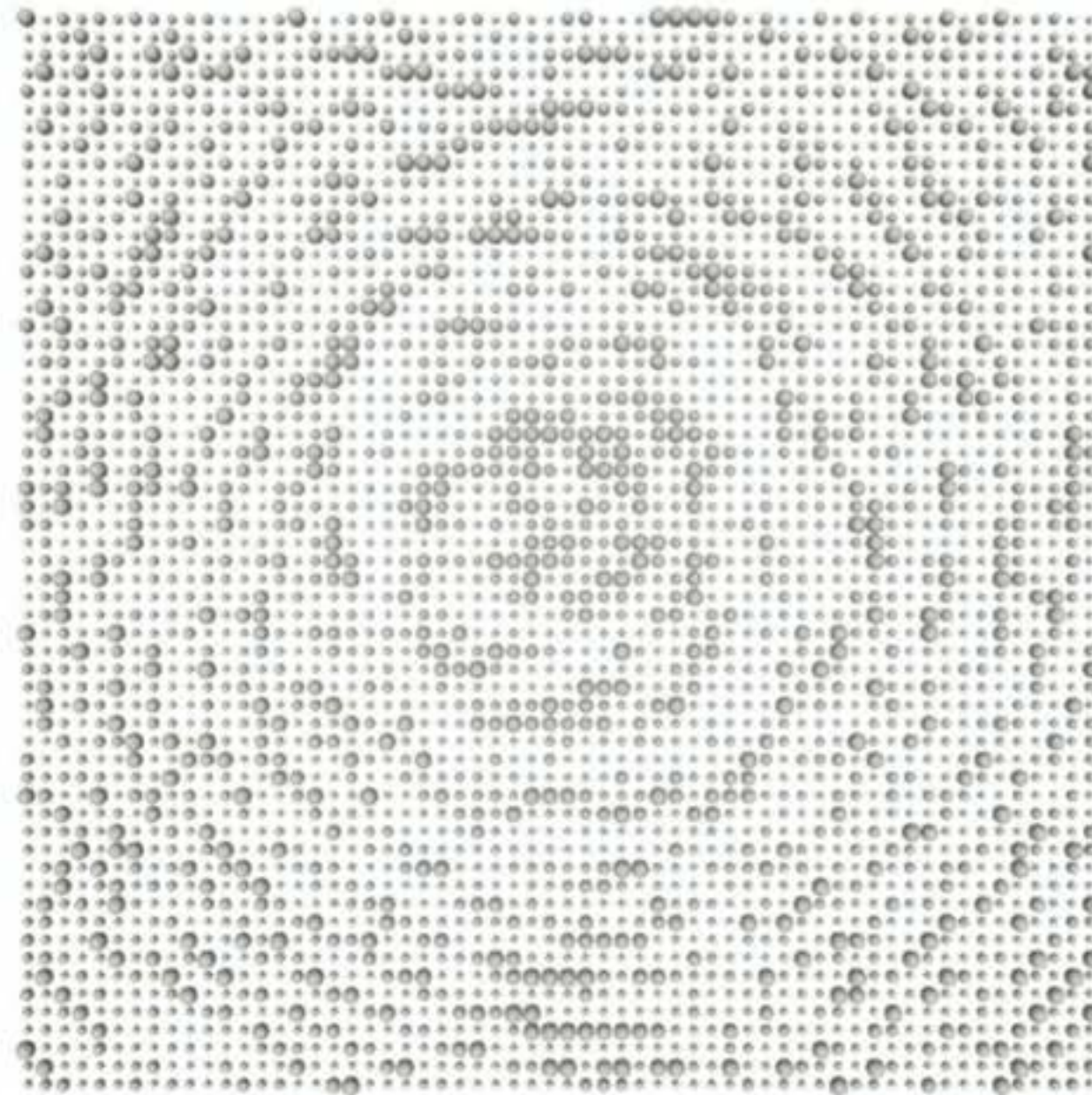
49



$$FOM_i = \sum_{j=1}^8 (I_{yellow}(\mathbf{r}_j) - I_i(\mathbf{r}_j))^2 + \sum_{k=1}^{14} (I_{blue}(\mathbf{r}_k) - I_i(\mathbf{r}_k))^2$$

Radius output

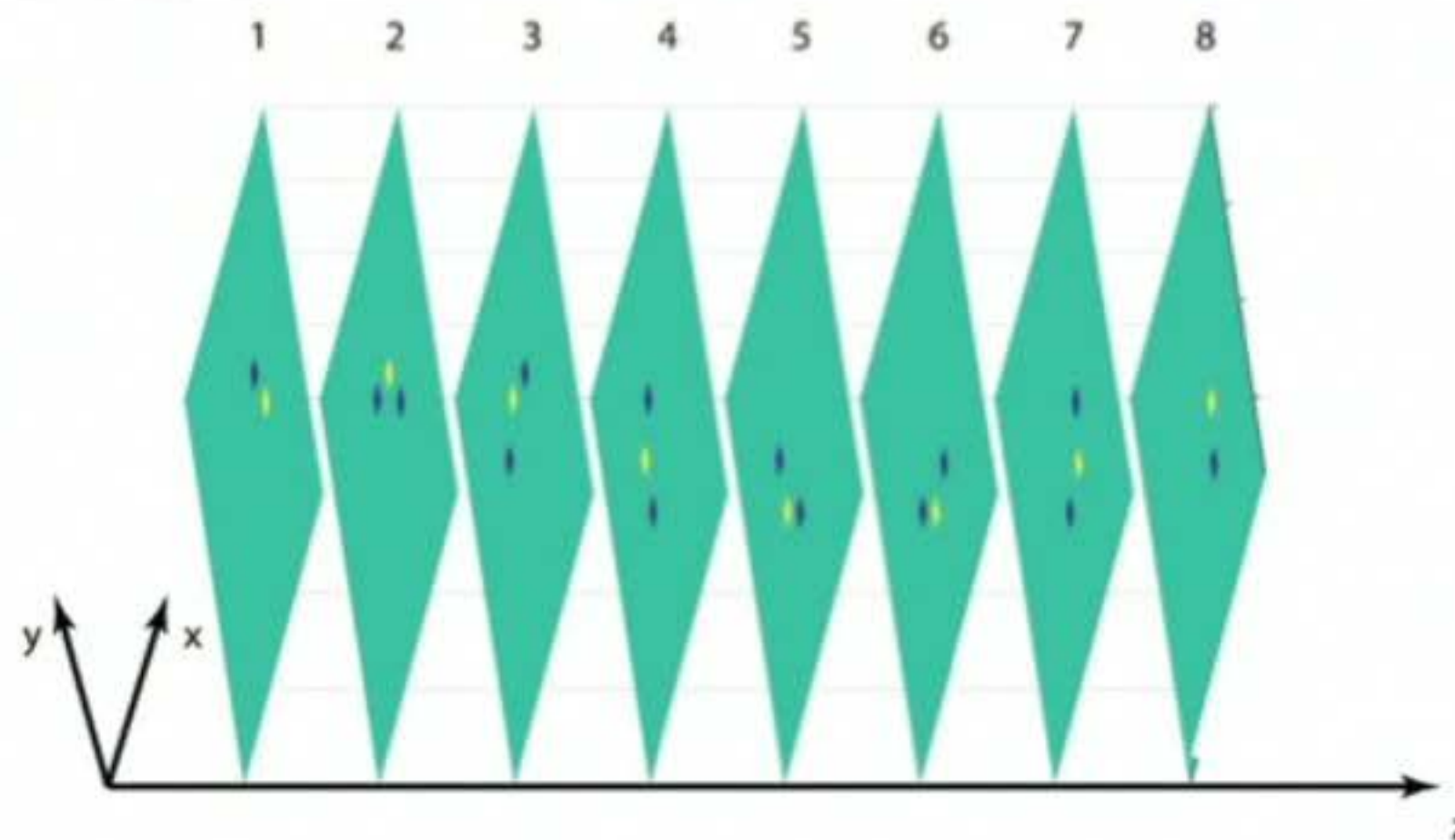
50



20 μm

Figure of merit definition

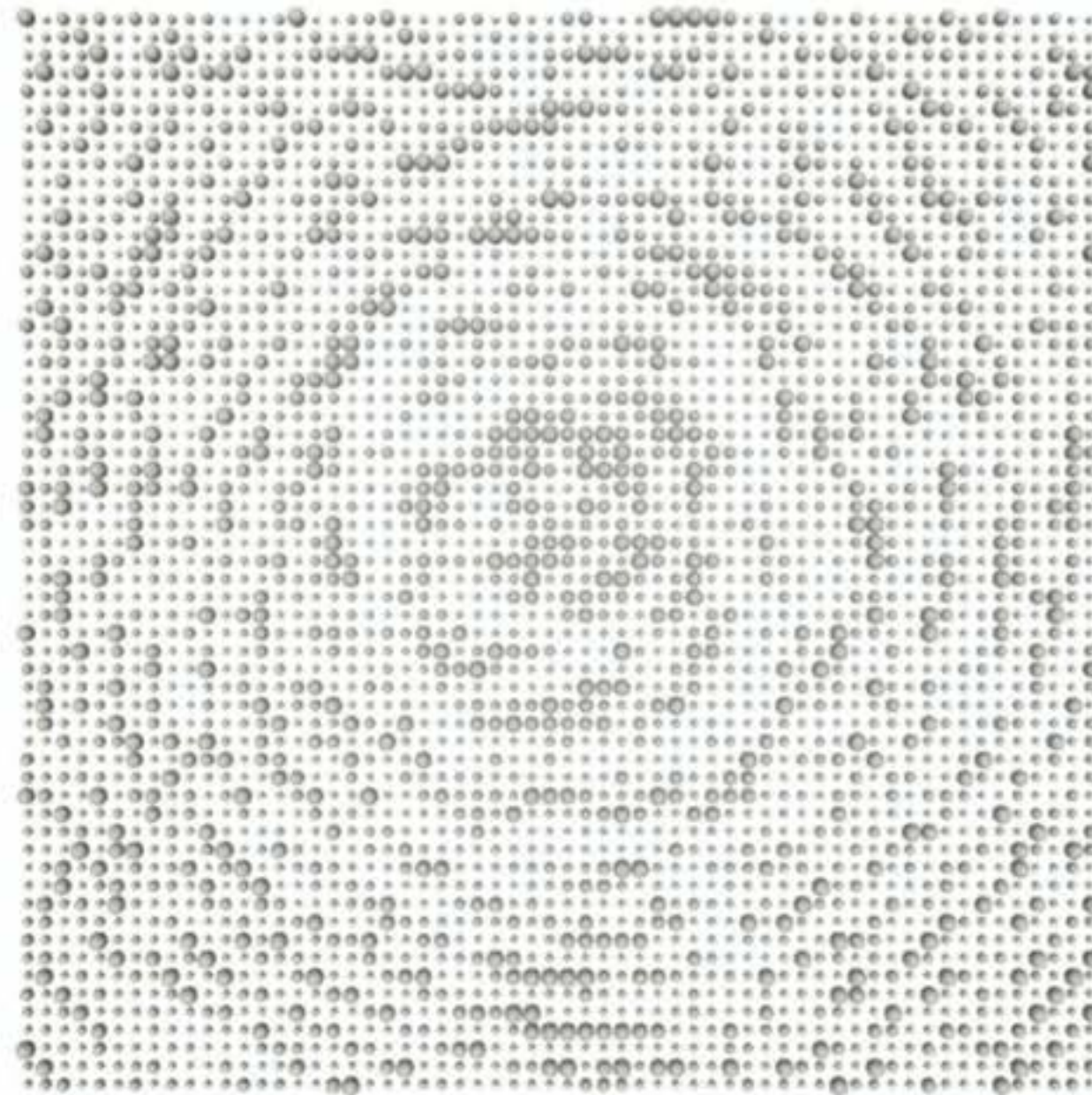
49



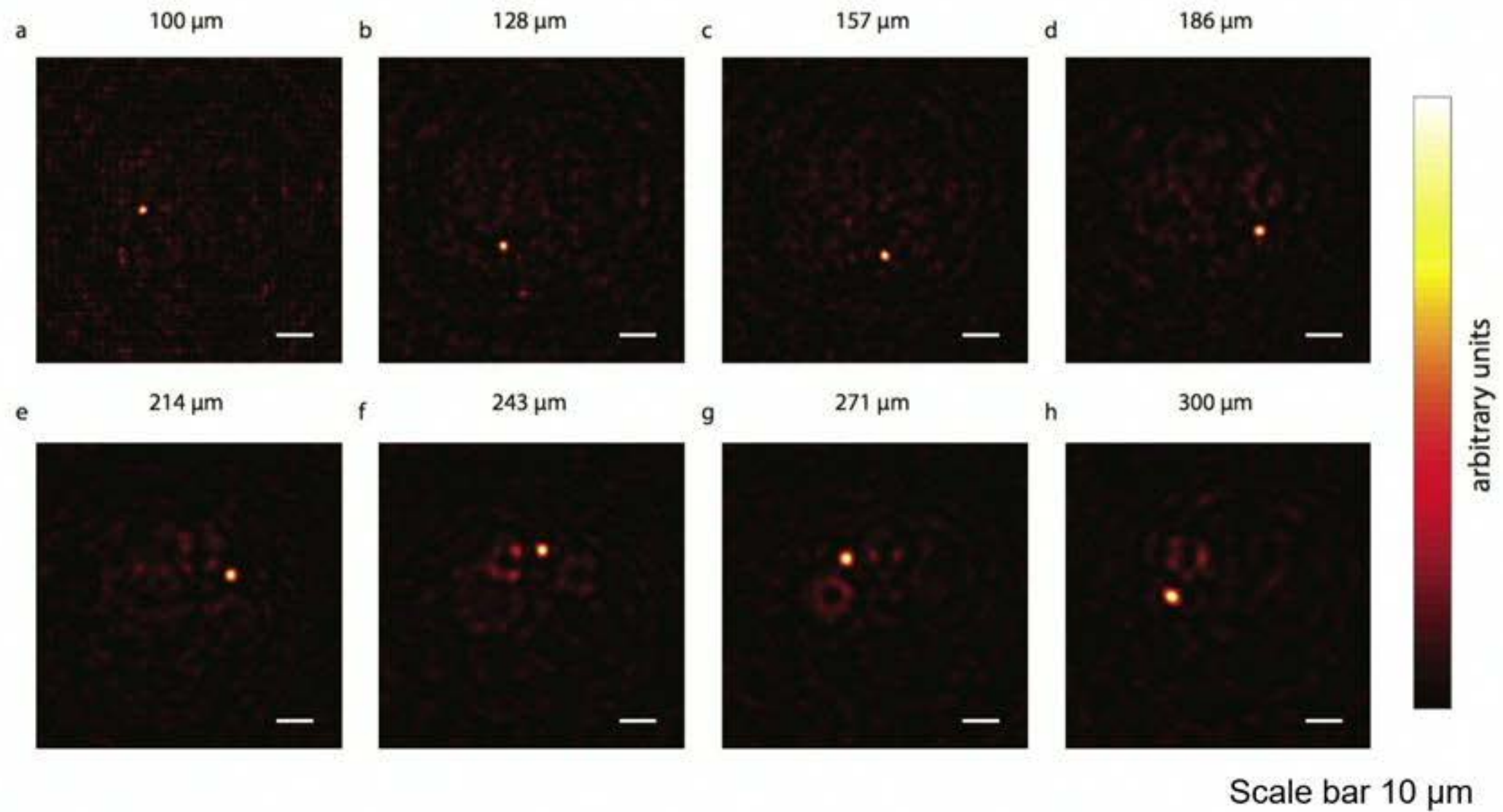
$$FOM_i = \sum_{j=1}^8 (I_{yellow}(\mathbf{r}_j) - I_i(\mathbf{r}_j))^2 + \sum_{k=1}^{14} (I_{blue}(\mathbf{r}_k) - I_i(\mathbf{r}_k))^2$$

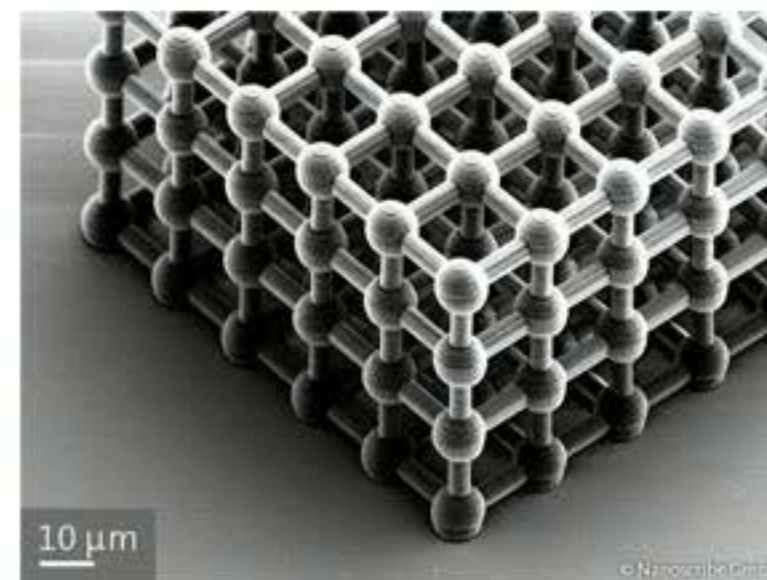
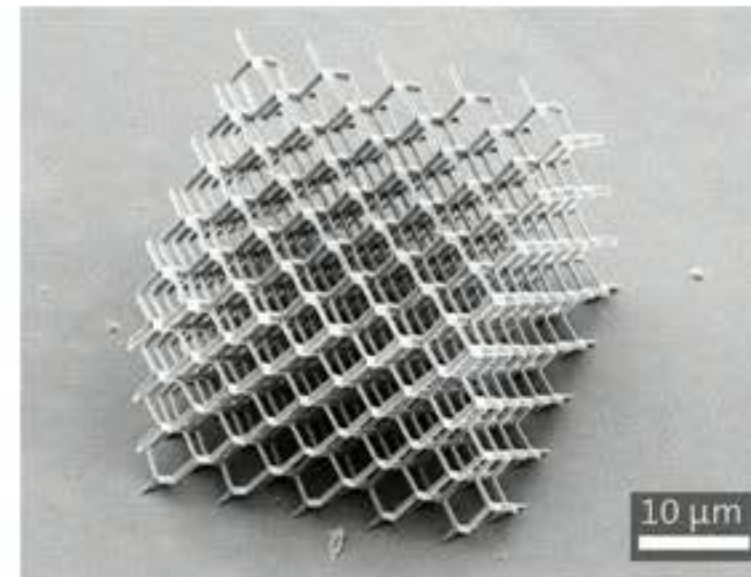
Radius output

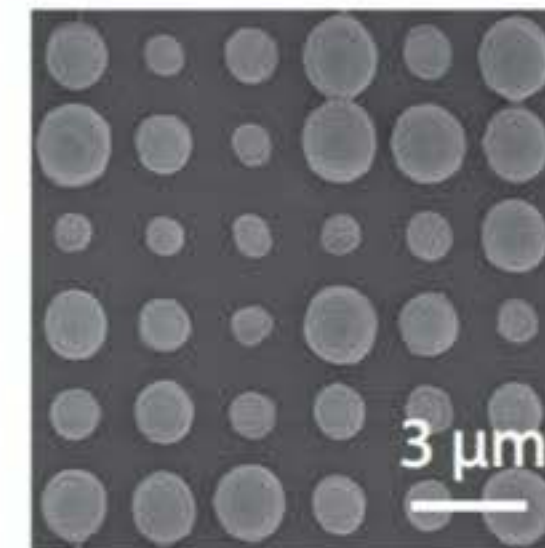
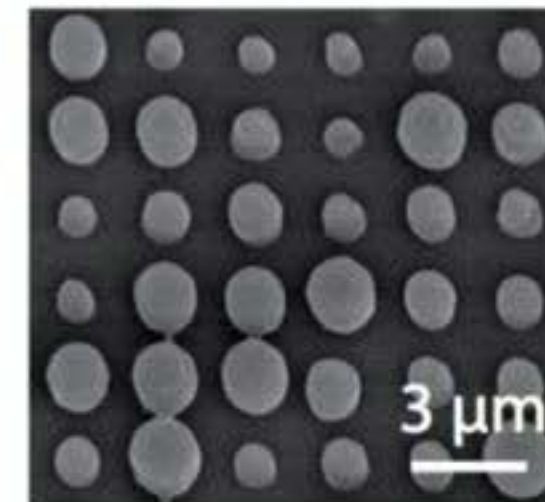
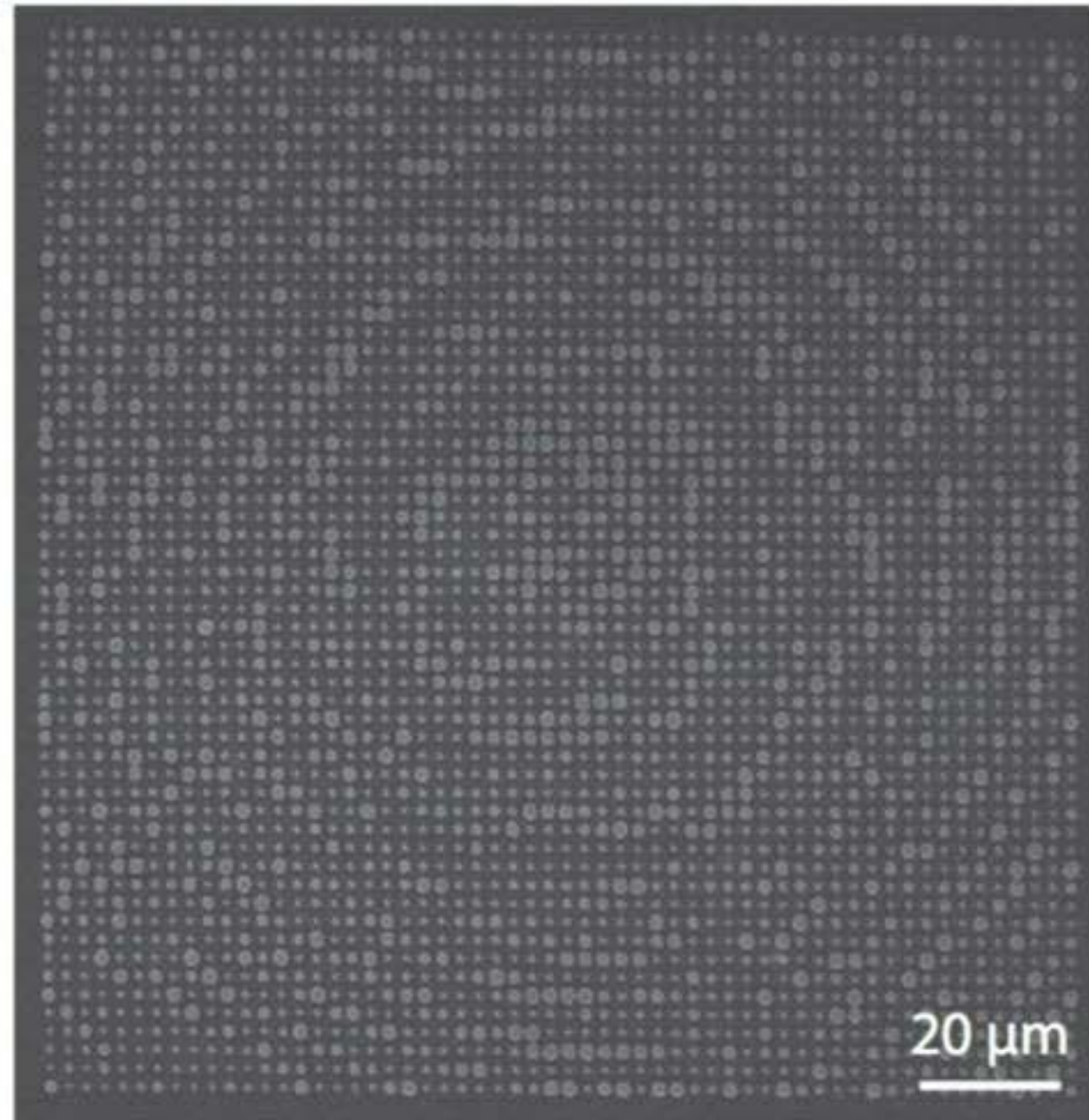
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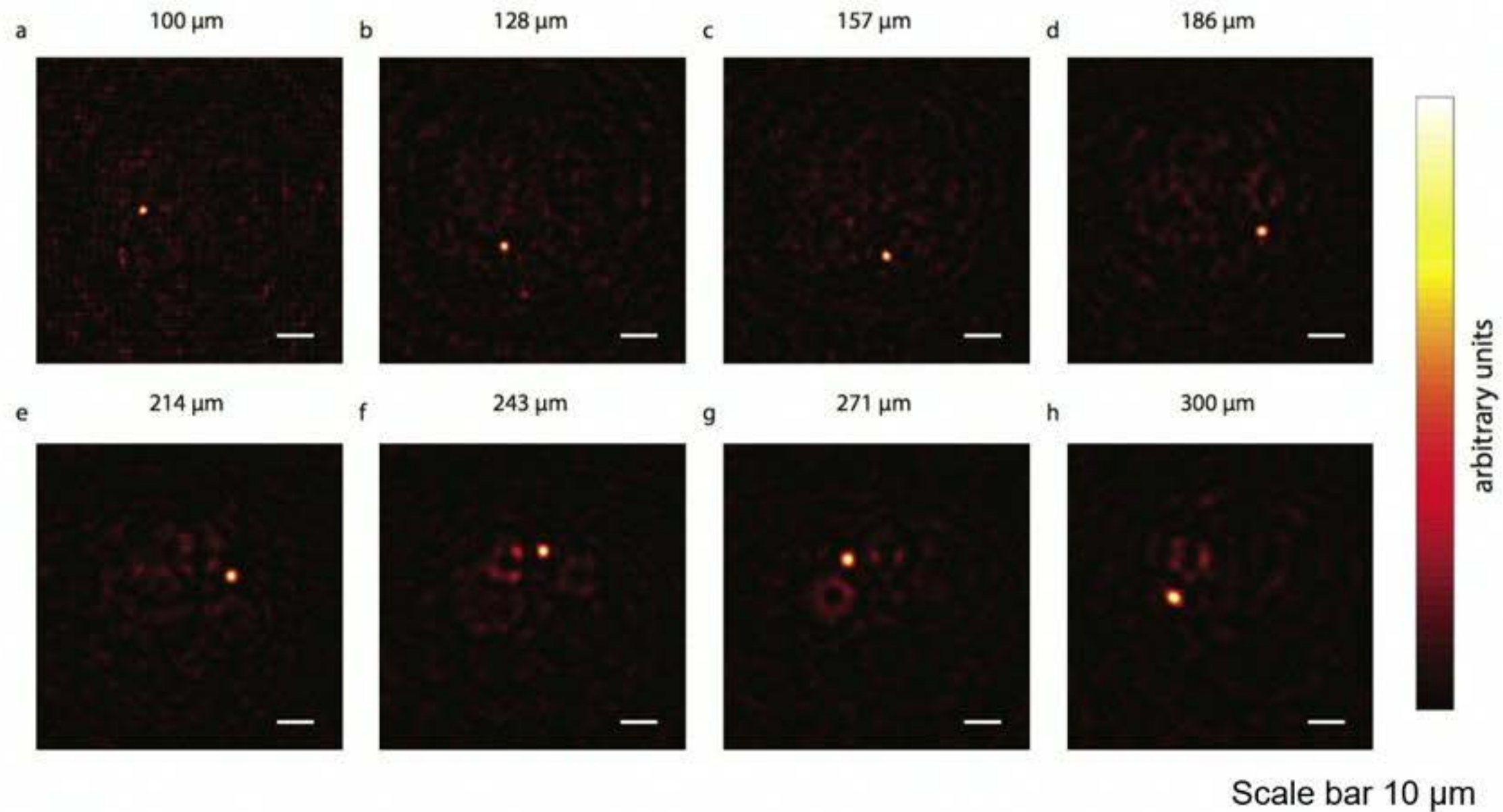


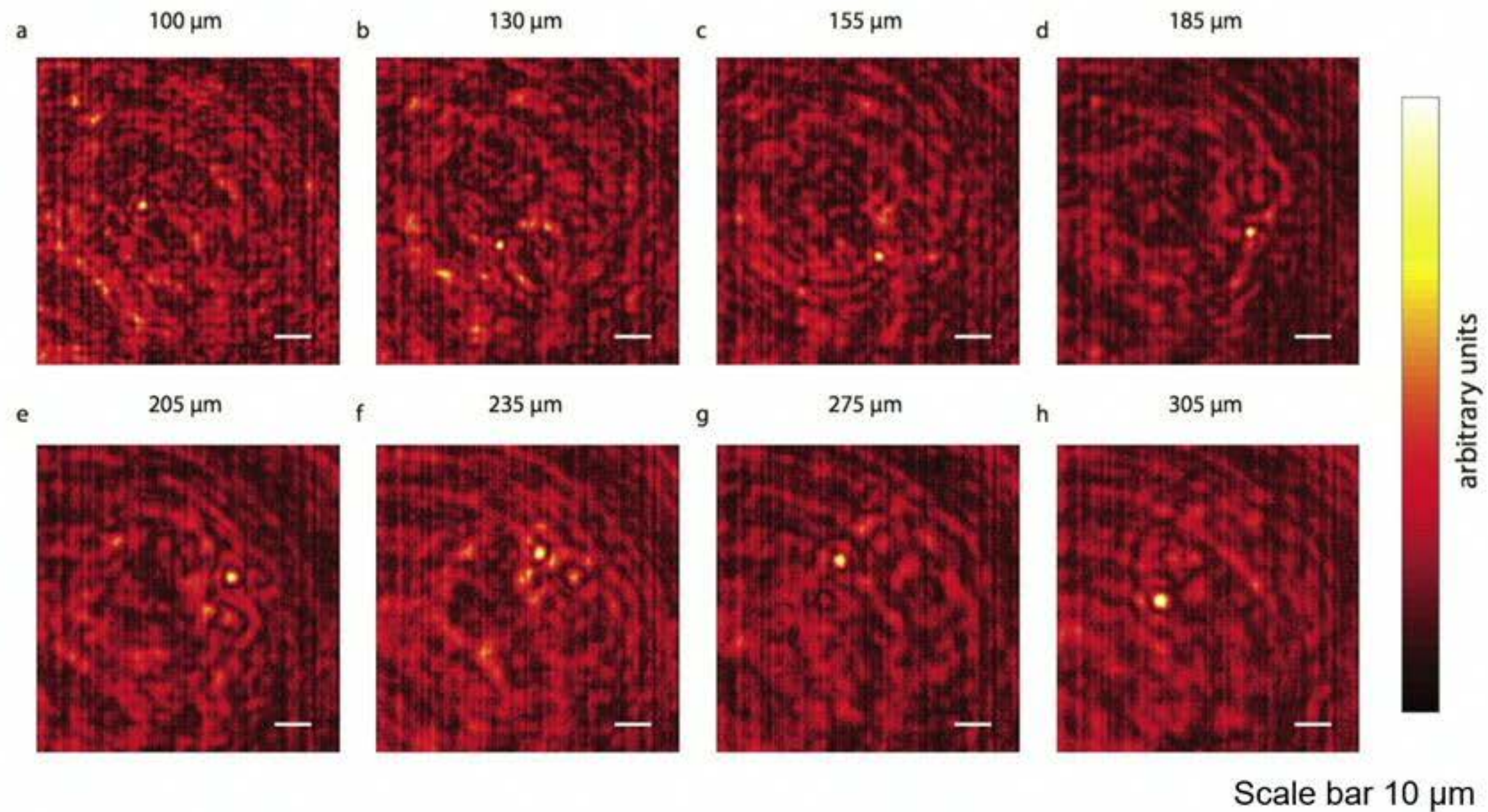
20 μm

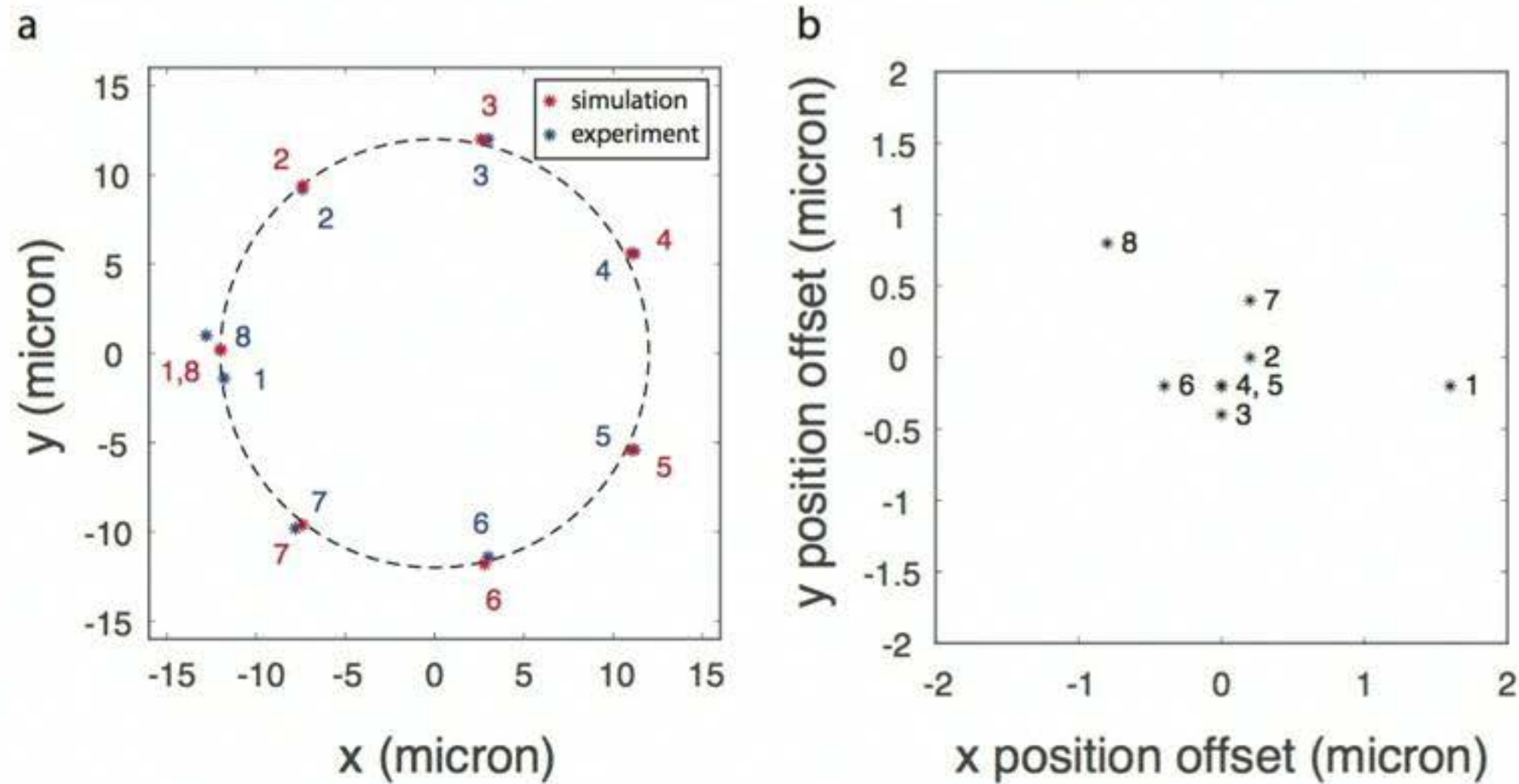




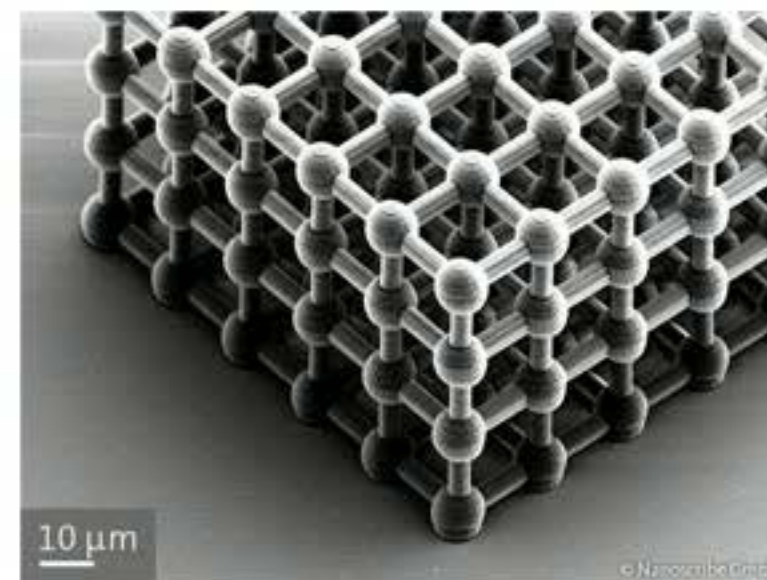
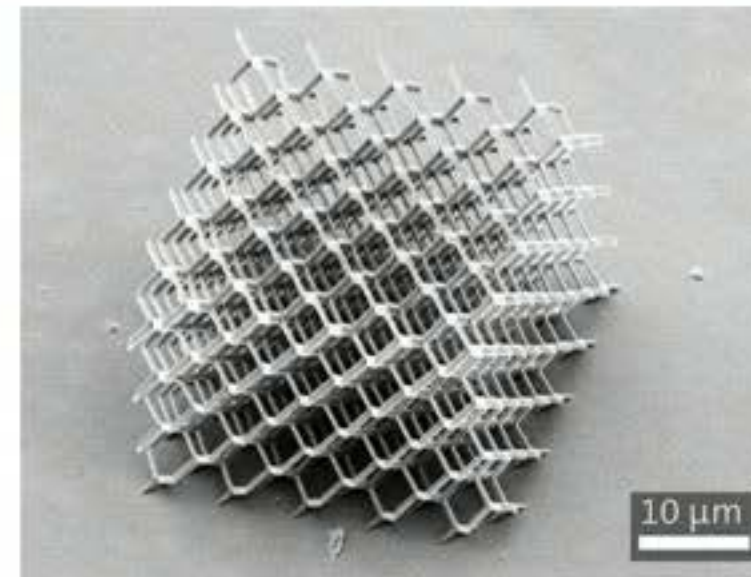


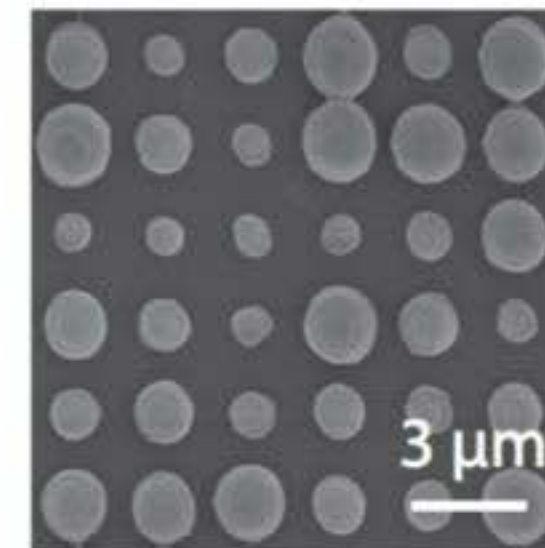
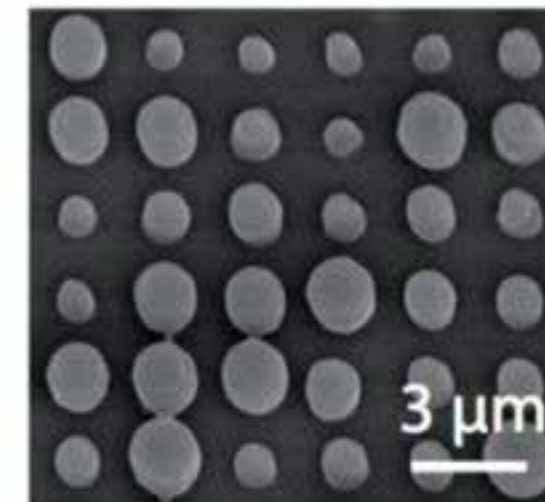
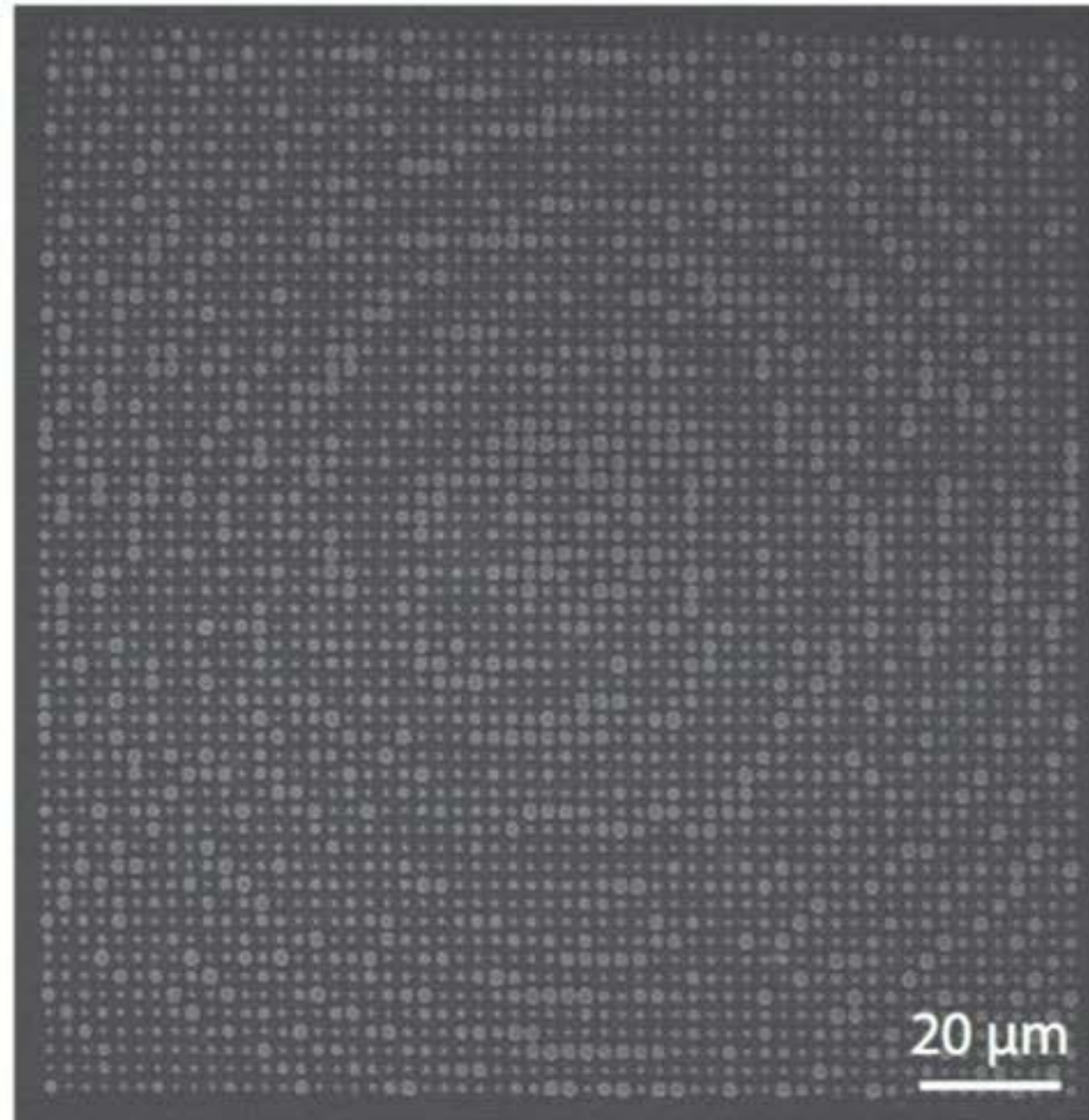


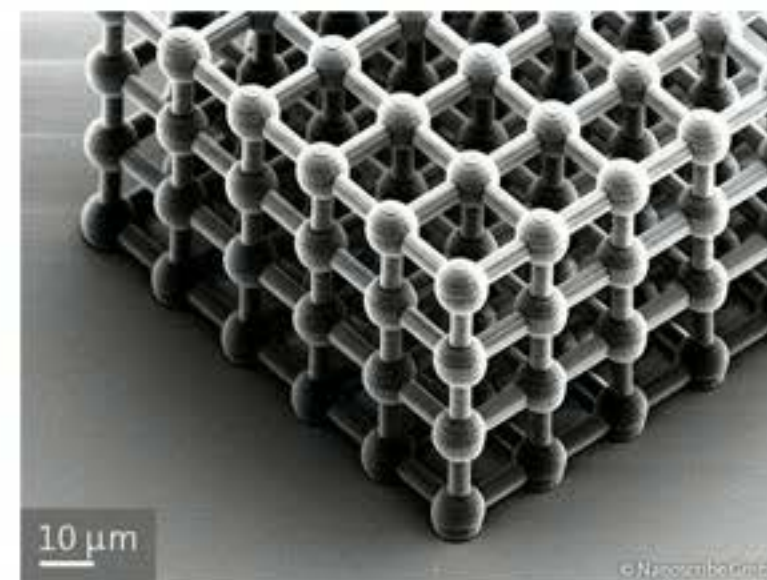
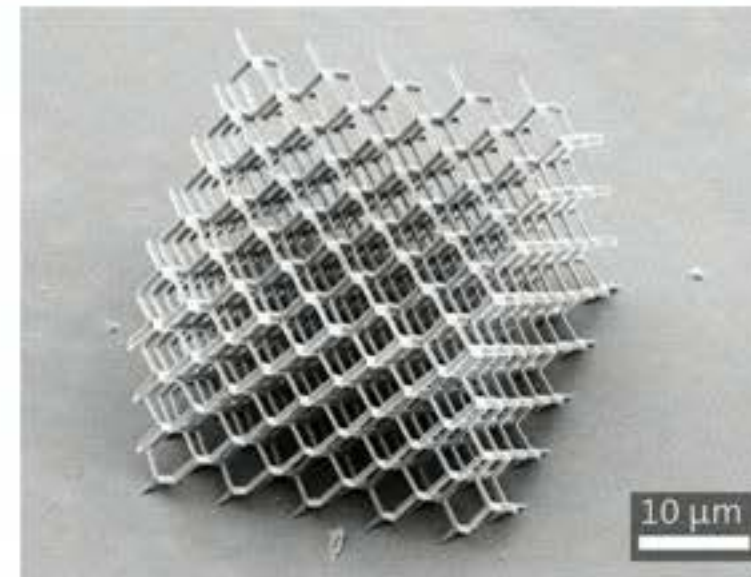




1. Single element metasurface optics
2. Towards metasurface optical systems
3. Inverse design and optimization of metasurfaces
4. Future work and outlook

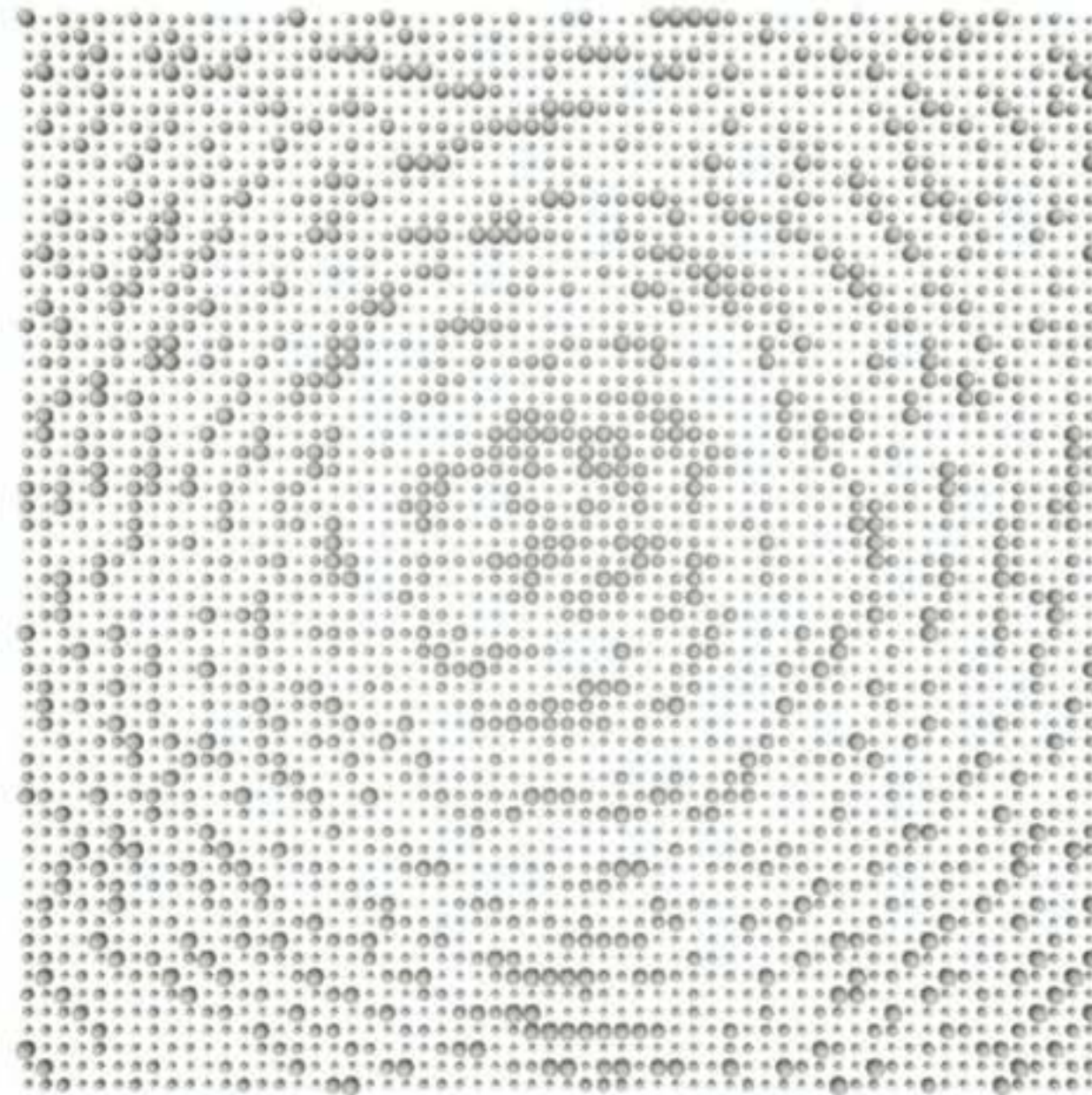






Radius output

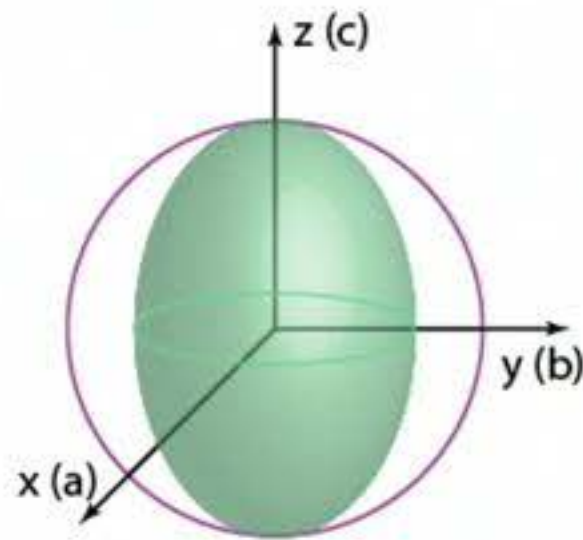
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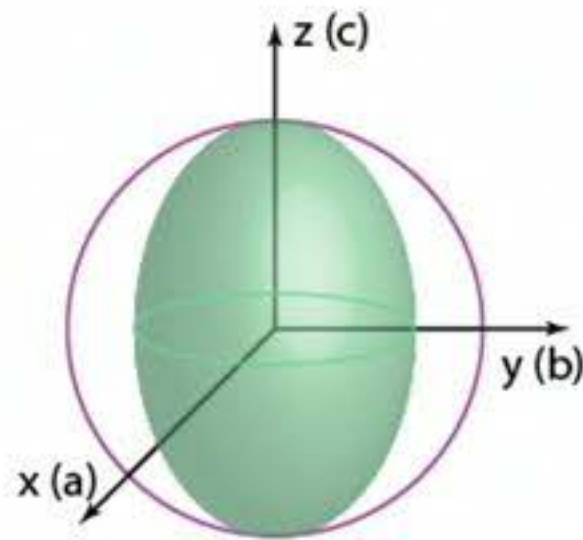
20 μm

1. Single element metasurface optics
2. Towards metasurface optical systems
3. Inverse design and optimization of metasurfaces
4. Future work and outlook

There is a straightforward extension to arbitrary shapes using the T-matrix method



There is a straightforward extension to arbitrary shapes using the T-matrix method



There is a straightforward extension to arbitrary shapes using the T-matrix method

Preliminary result shows we can increase efficiency of a 0.83 NA lens from 20% to 26% using ellipsoidal scatterers

Currently, the model for optical elements is to buy off a shelf.



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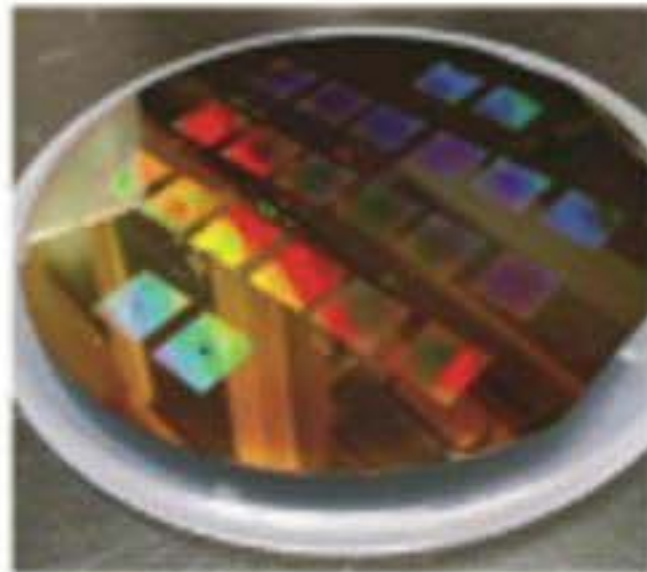
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This is partly due to manufacturing restrictions.



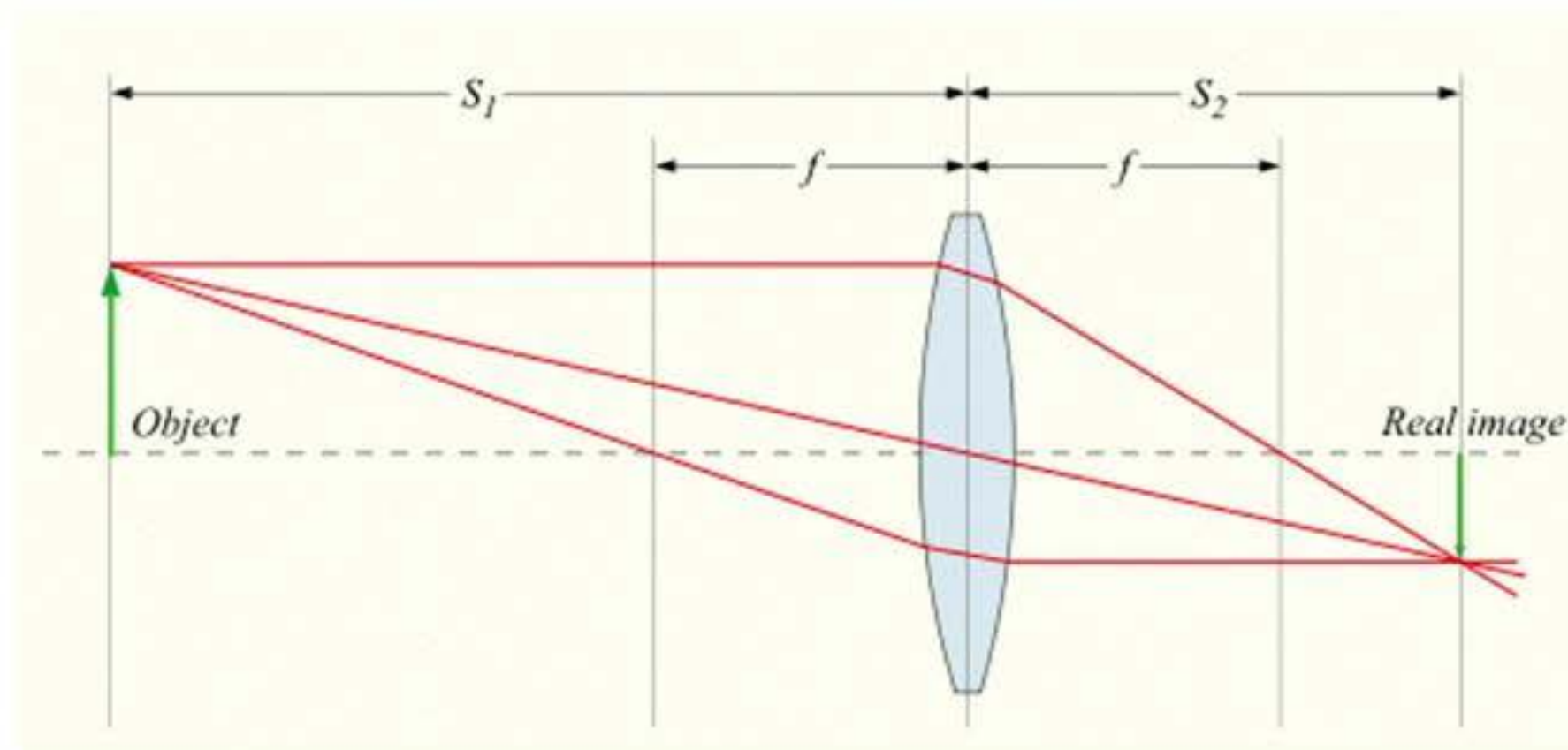
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This is partly due to manufacturing restrictions.

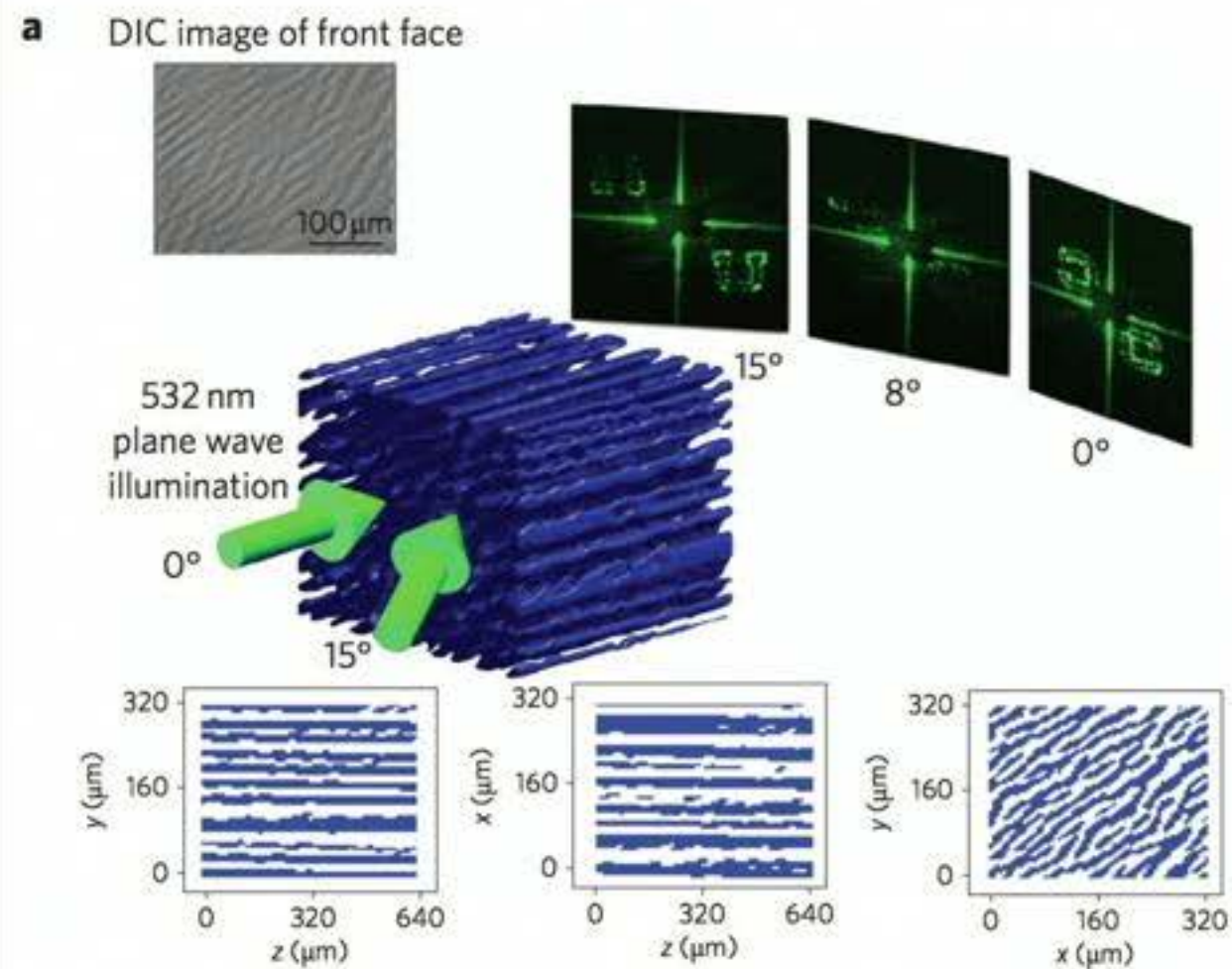


A new model where custom optical elements are tailored and designed for specific applications

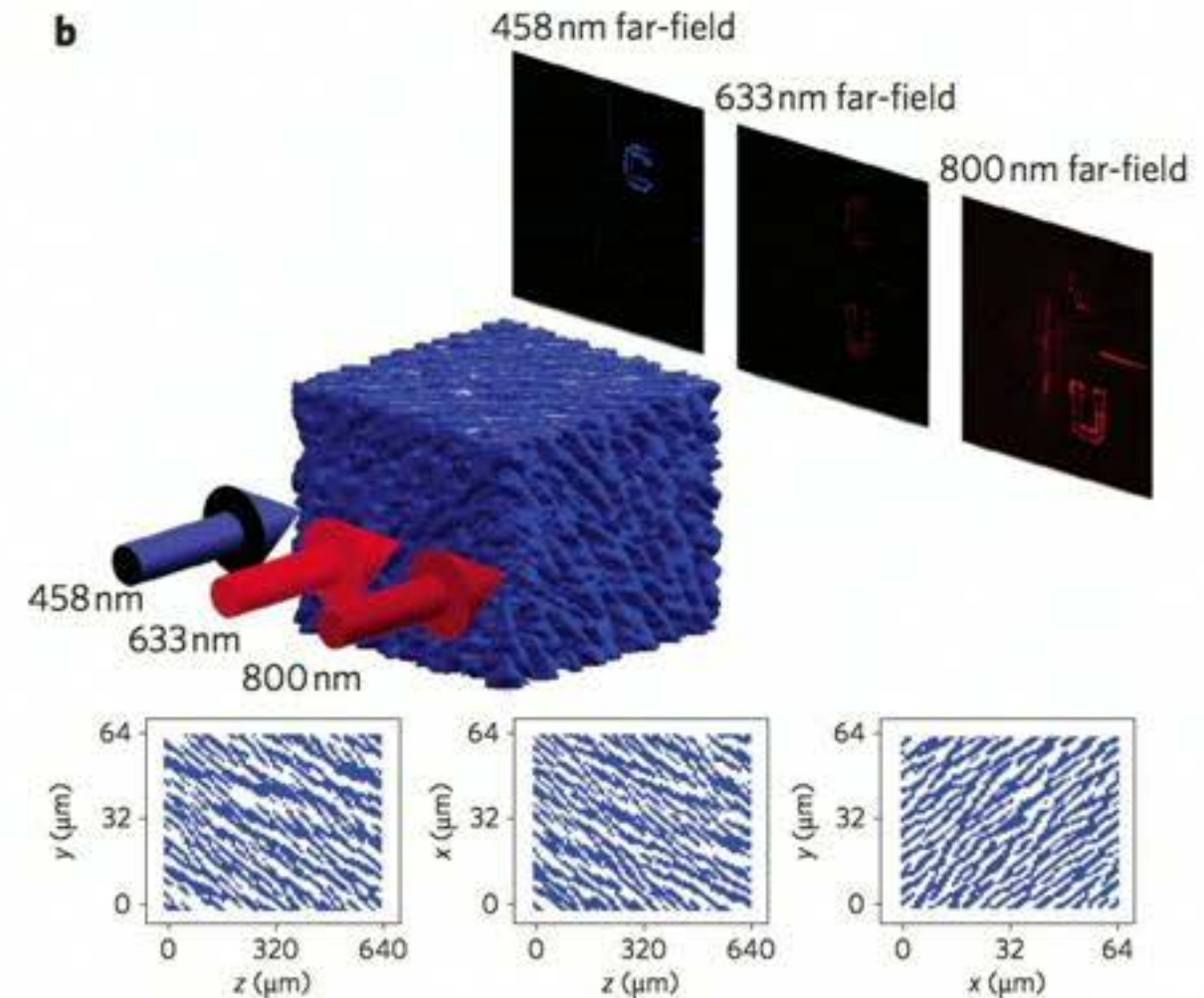
When we think about optical elements, generally we think about a 2D input plane incident on a 2D object forming a 2D output plane...



... But why restrict ourselves to that?



Gerke et al. Nat. Photon. **4**, 3 (2010)



Optics and computational algorithm co-optimization

62



Optics and computational algorithm co-optimization

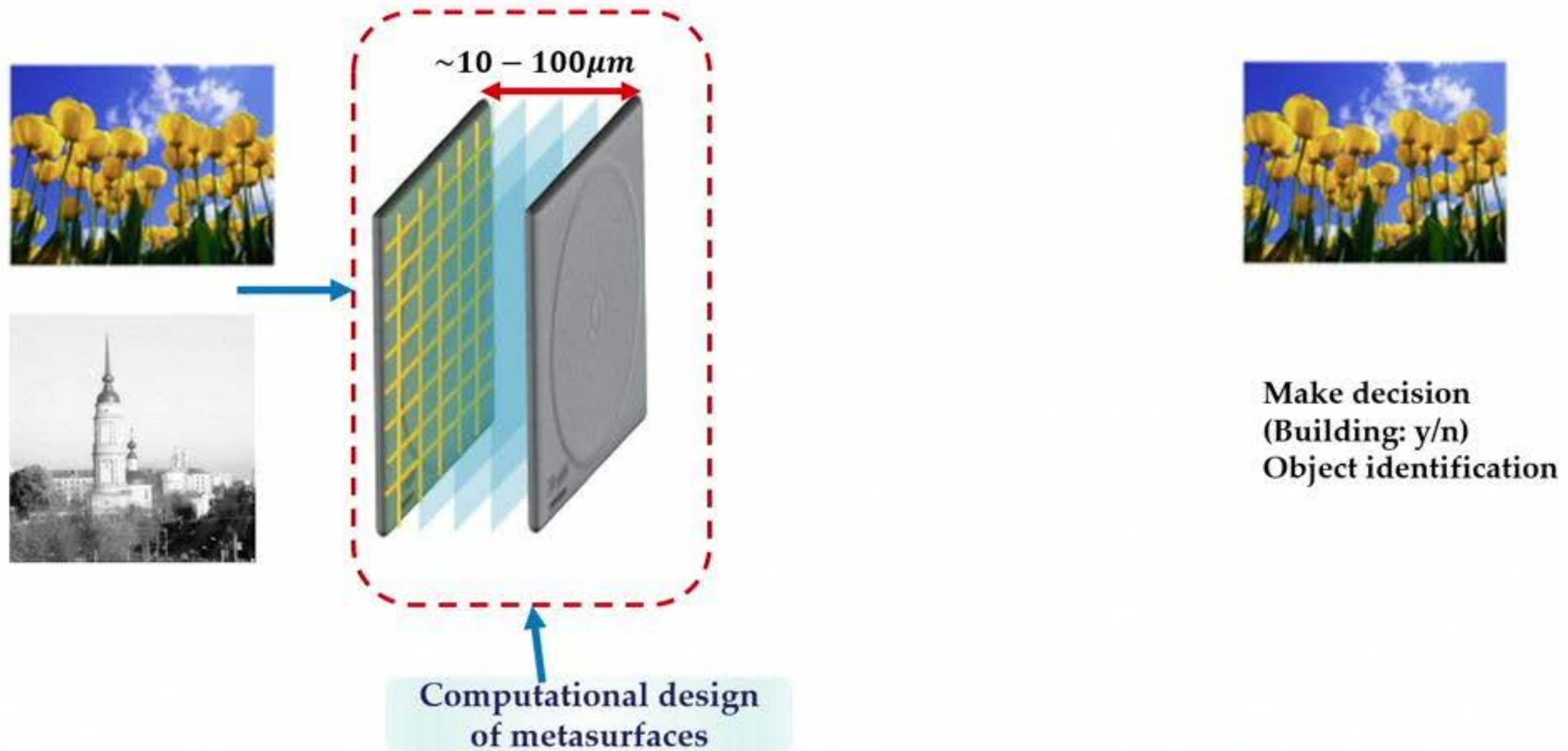
62



Make decision
(Building: y/n)
Object identification

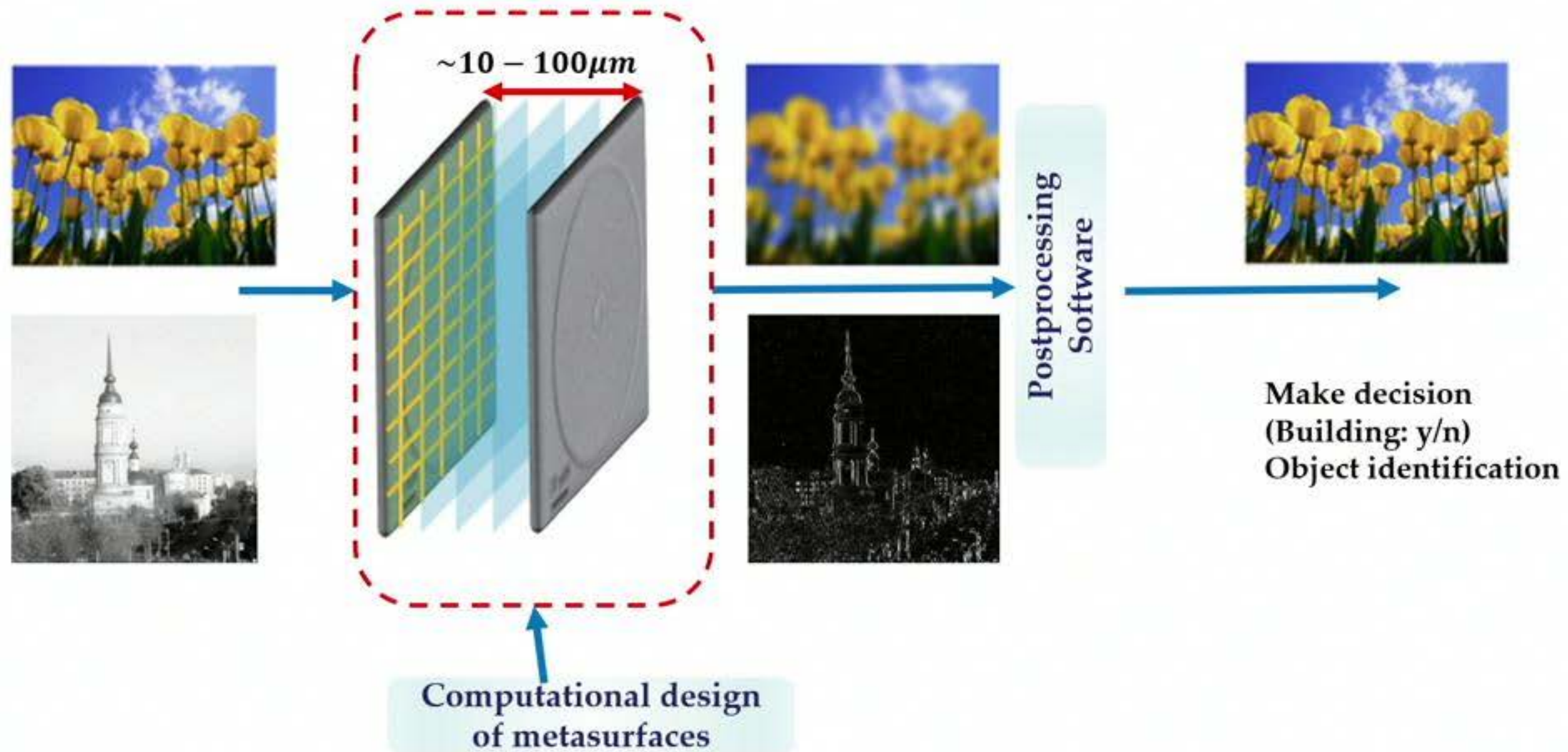
Optics and computational algorithm co-optimization

62



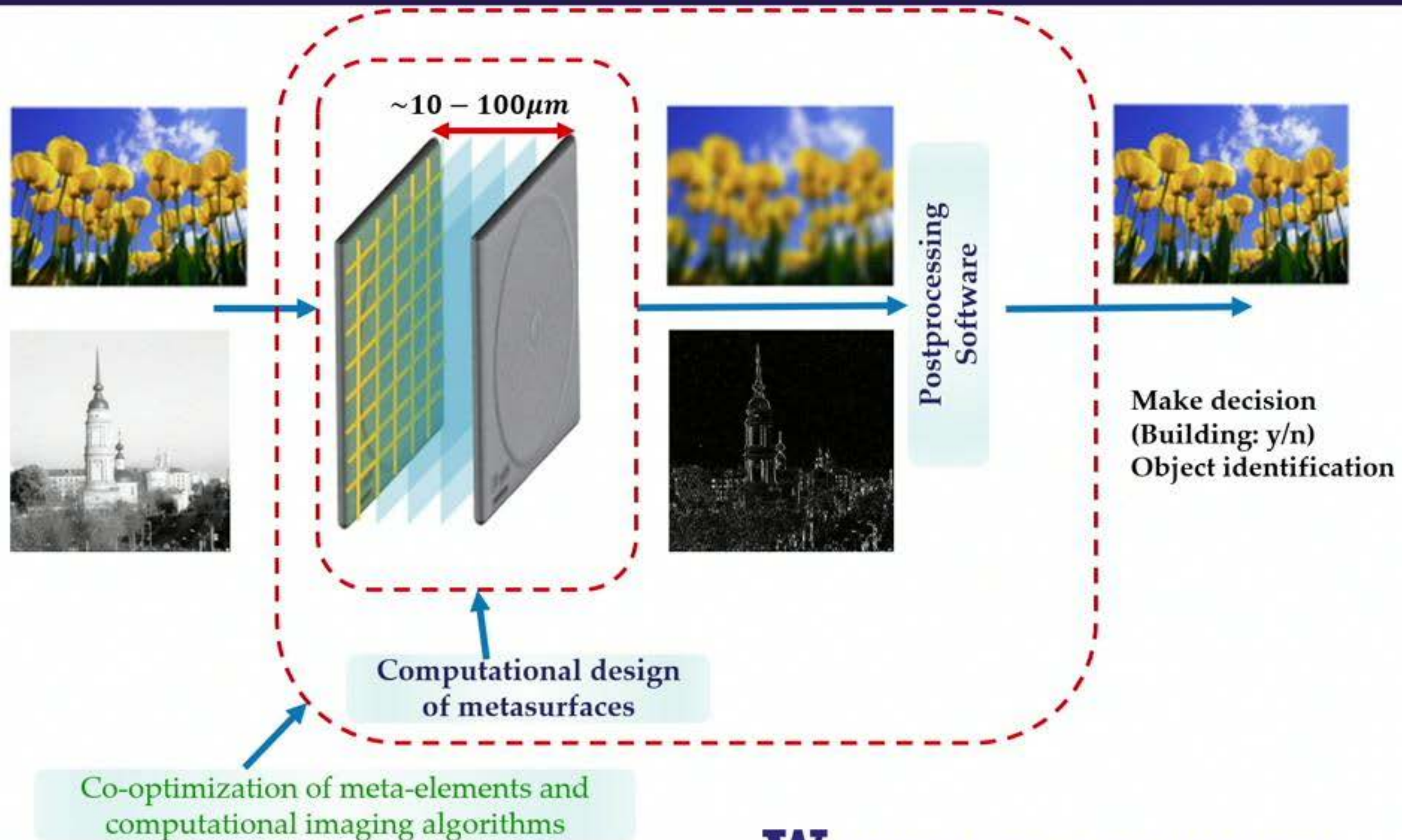
Optics and computational algorithm co-optimization

62



Optics and computational algorithm co-optimization

62



1. Single element metasurfaces

1. Design process
2. Chromatic aberration

2. Towards metasurface optical systems

1. Tunable devices, aberration correction
2. Large area fabrication

3. Inverse design and optimization of metasurfaces

1. Sphere based diffractive optics
2. Local phase method

Acknowledgements

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NOISE: Nano Optoelectronic Integrated System Engineering



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Lorezno Pattelli

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Google
Samsung
Facebook
Amazon

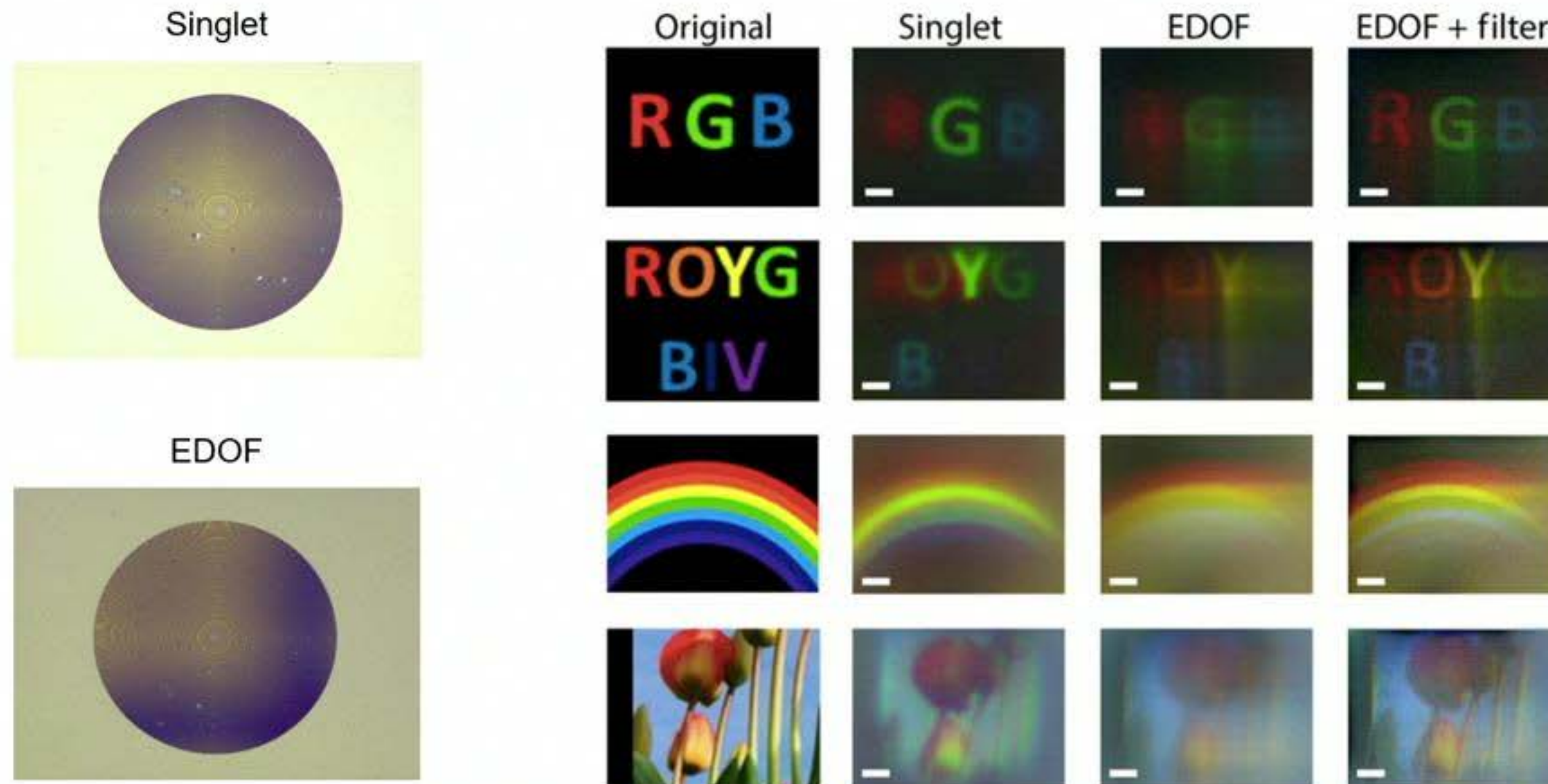


National Nanotechnology
Coordinated Infrastructure

W UNIVERSITY of WASHINGTON

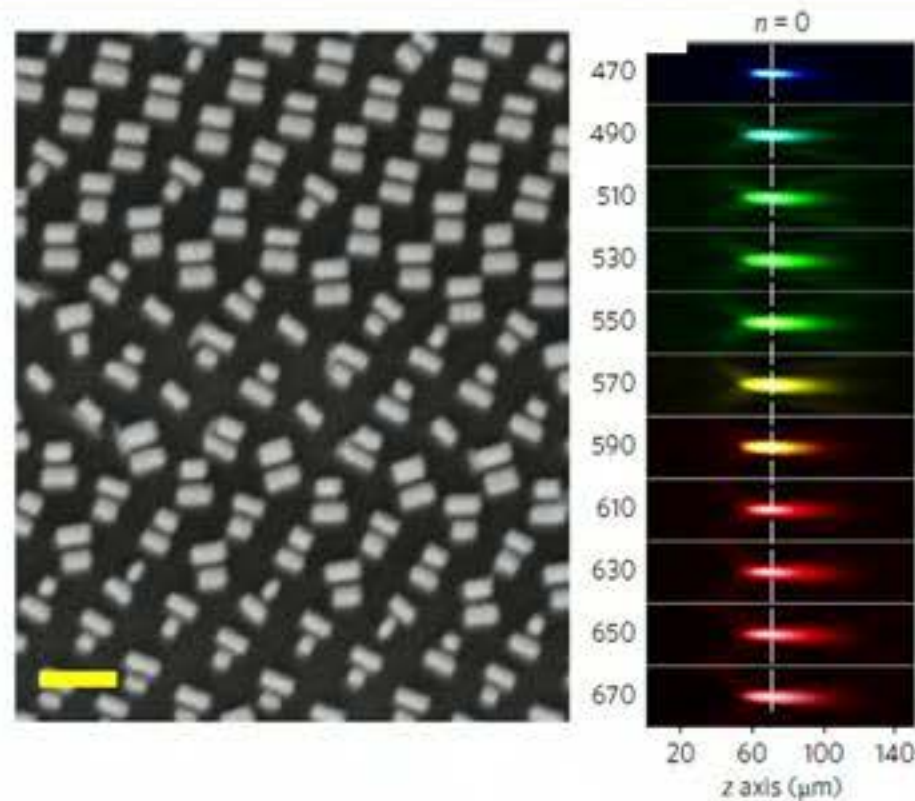
Computational imaging approach

28

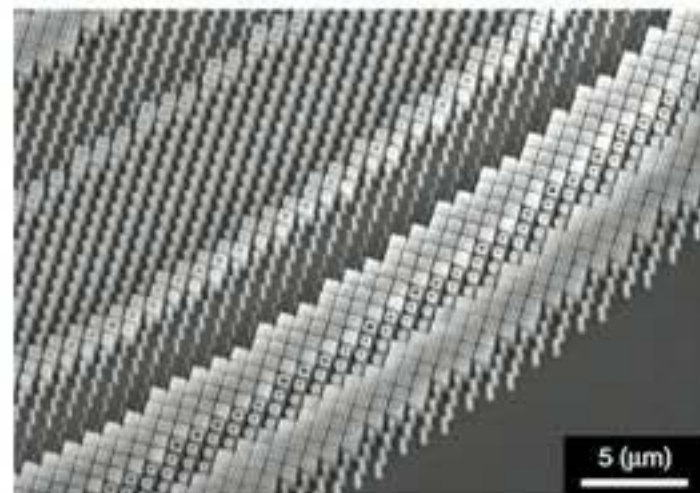


Correcting chromatic aberrations

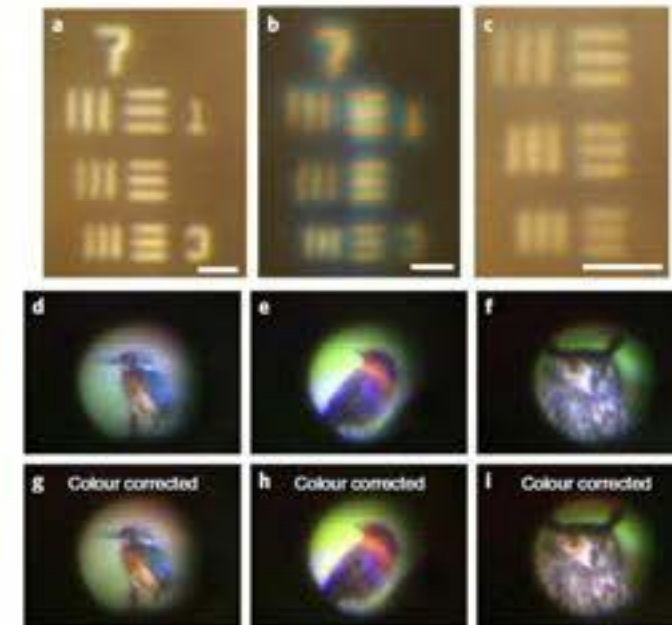
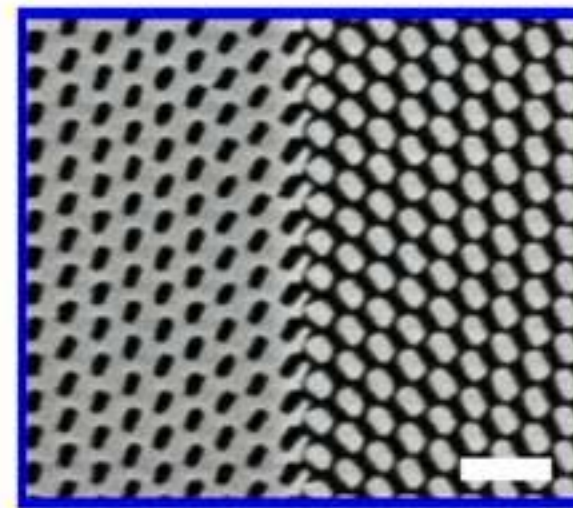
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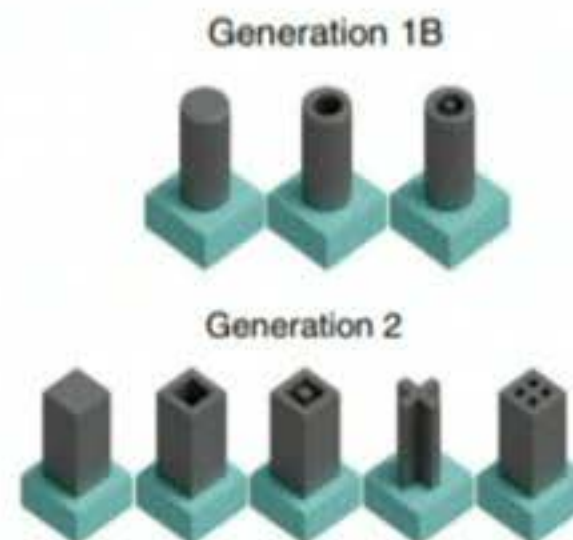
W. Chen et al, Nat. Nano. **13**, 220 (2018)



Shrestha et al. Light: Sci. and Appl. **7**, 95 (2018)

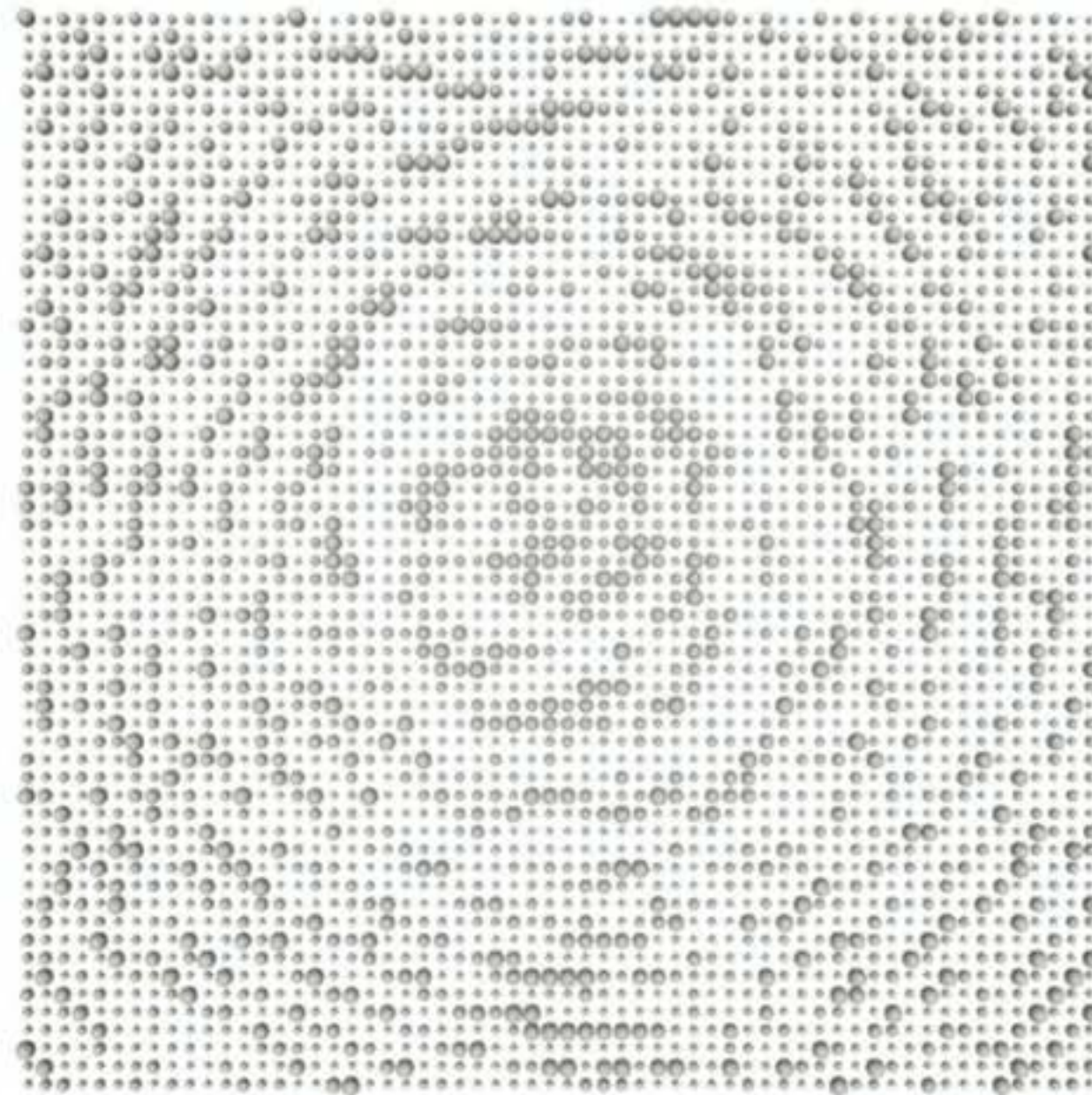


S. Wang et al, Nat. Nano. **13**, 227 (2018)



Radius output

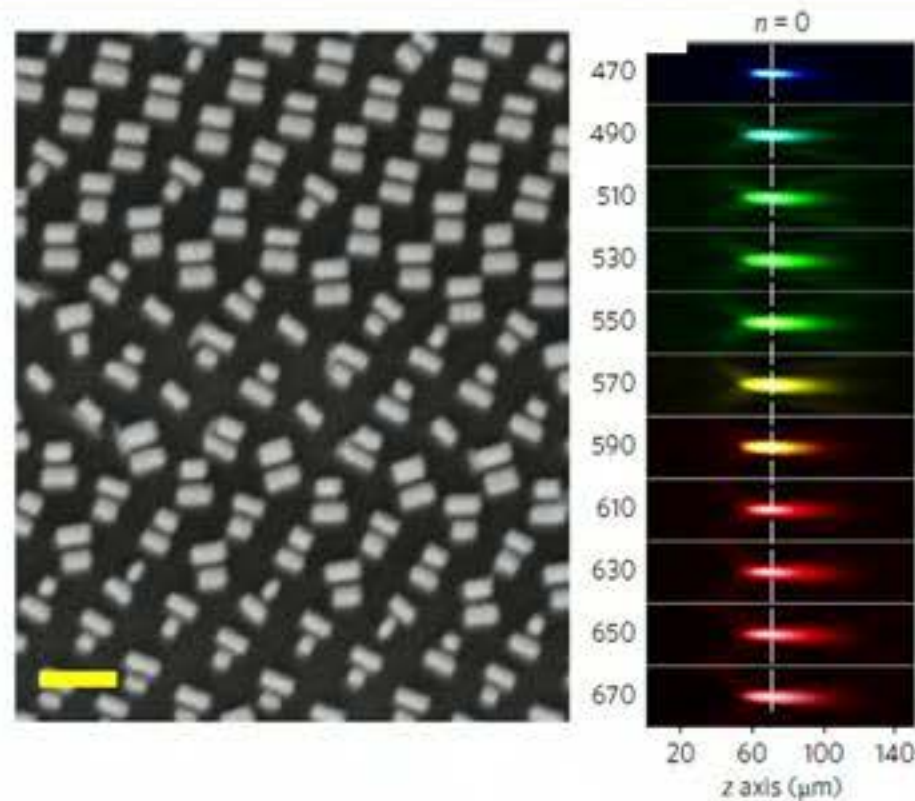
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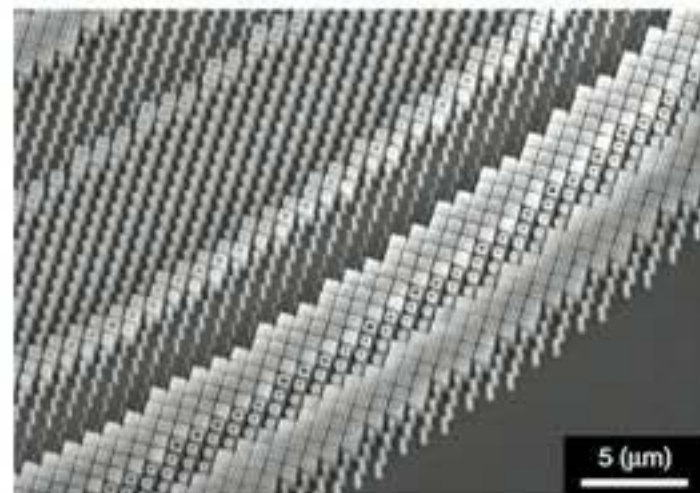
20 μm

Correcting chromatic aberrations

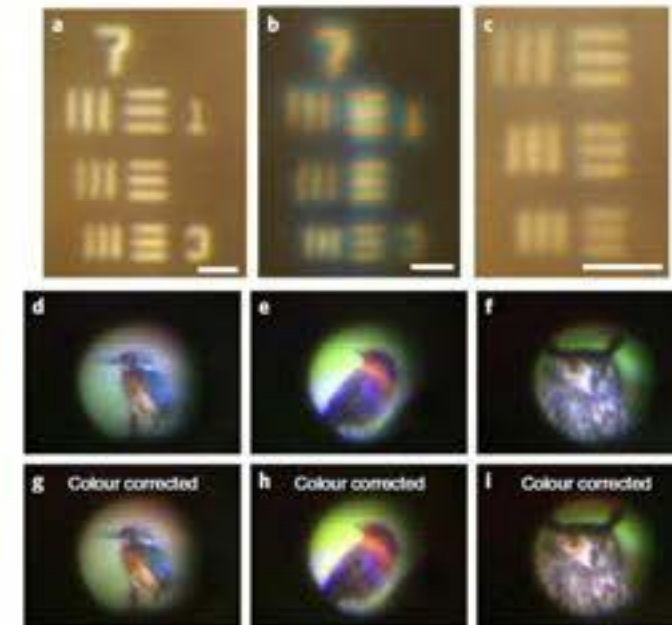
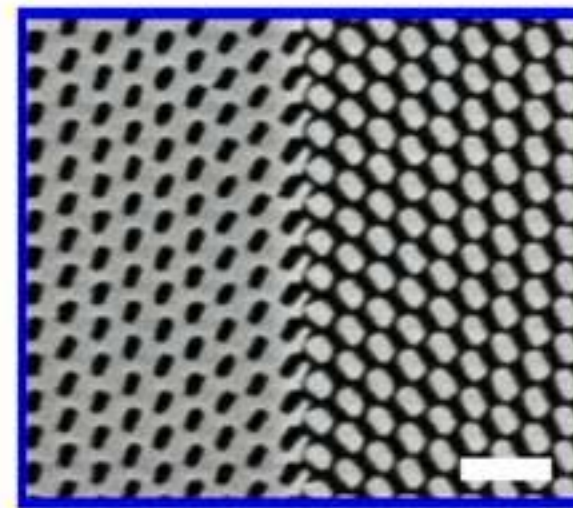
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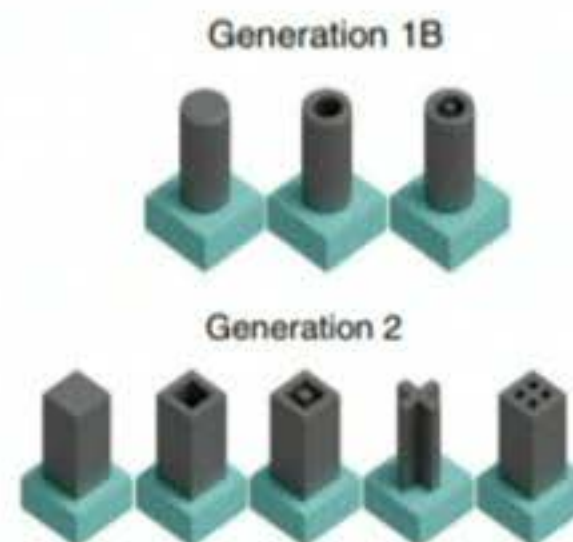
W. Chen et al, Nat. Nano. **13**, 220 (2018)

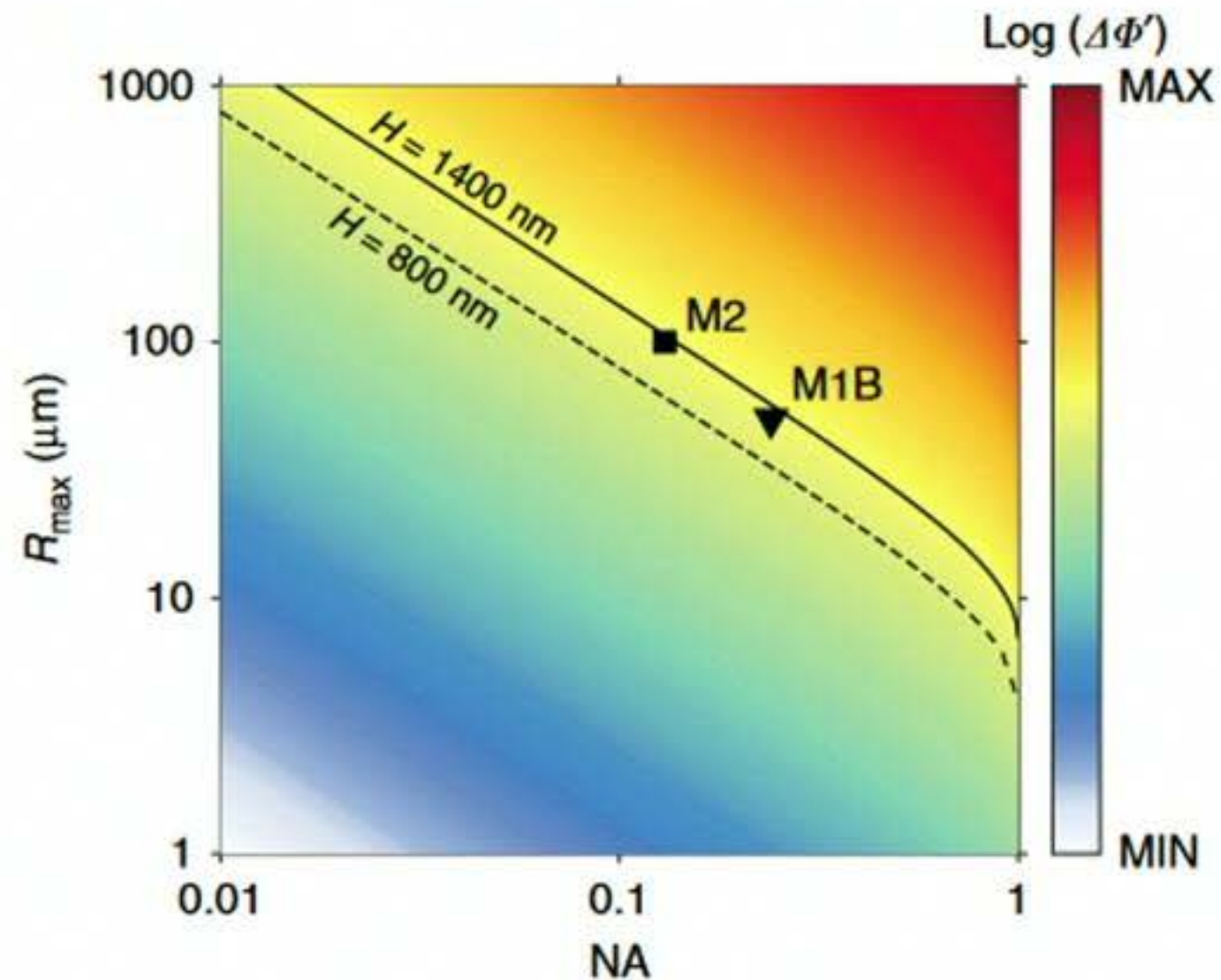


Shrestha et al. Light: Sci. and Appl. **7**, 95 (2018)



S. Wang et al, Nat. Nano. **13**, 227 (2018)



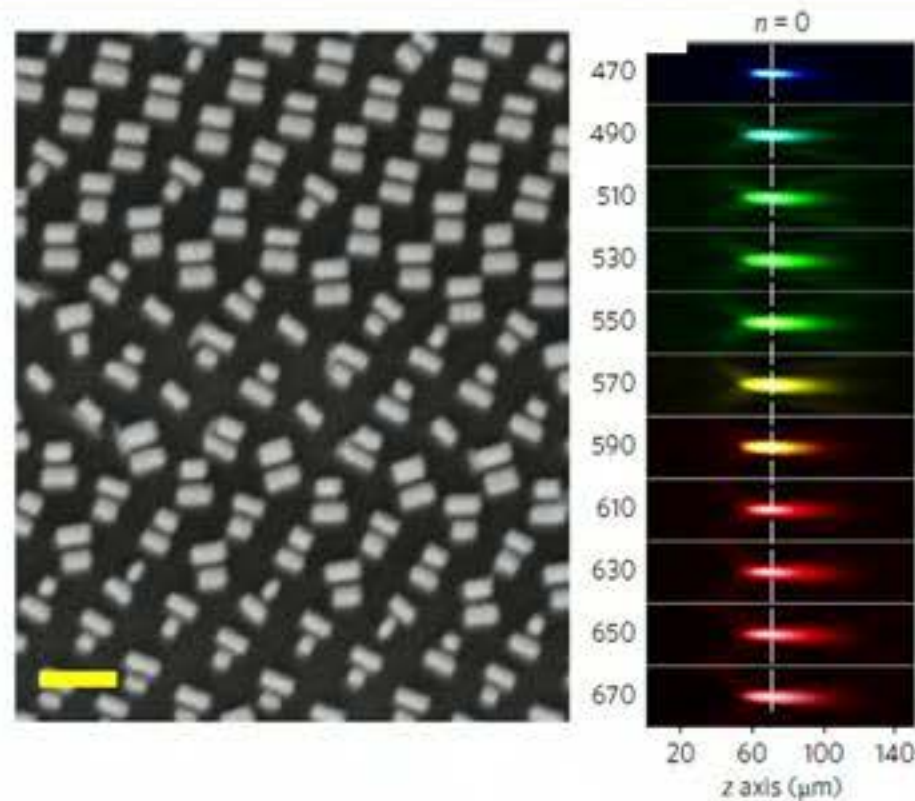


$$R_{\max} = \frac{\Delta\Phi'}{\Delta\omega \left(\frac{1}{NA} - \sqrt{\frac{1}{NA^2} - 1} \right)}$$

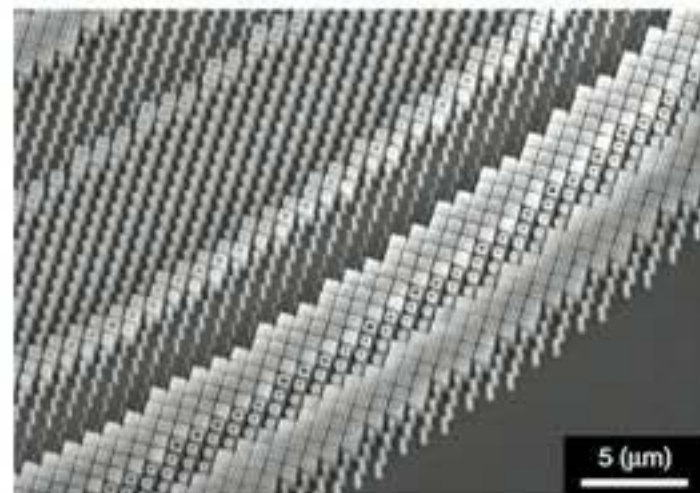
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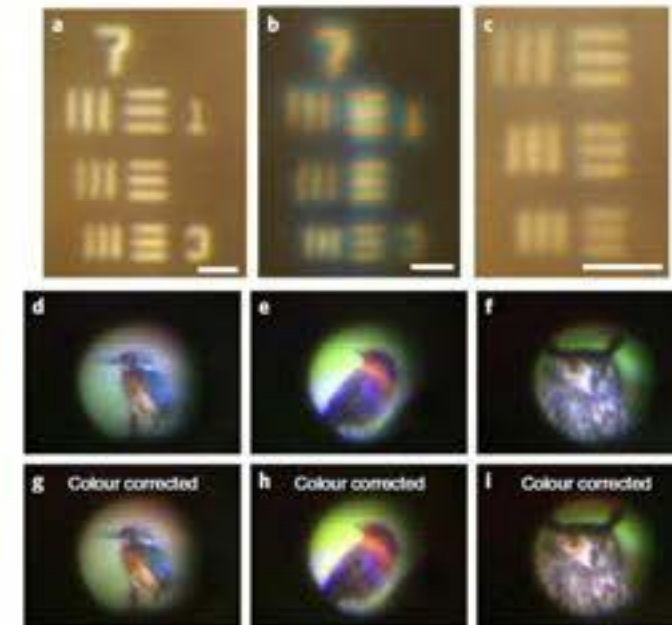
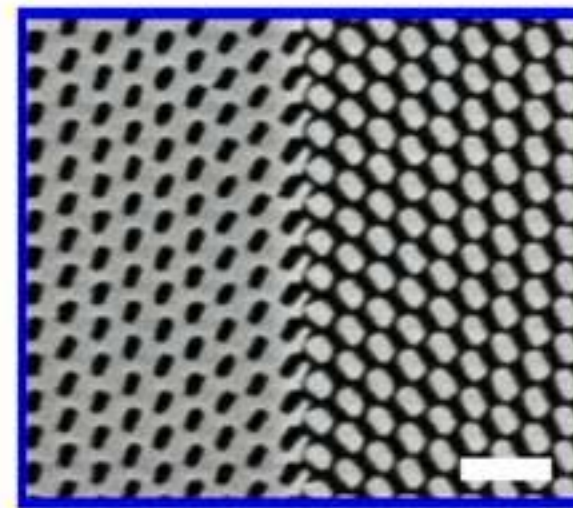
25



W. Chen et al, Nat. Nano. **13**, 220 (2018)



Shrestha et al. Light: Sci. and Appl. **7**, 95 (2018)



S. Wang et al, Nat. Nano. **13**, 227 (2018)

